

1 **Time vs light: A potentially useable light sum hybrid model to represent the**
2 **juvenile growth of Douglas-fir subject to varying levels of competition**

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8 **Abstract**

9
10 Substitution of potential useable light sum for time in a commonly used mensurational
11 equation resulted in a better fit to data from a complex vegetation management
12 experiment. The experiment involved Douglas fir as a crop species and a variety of
13 competing weed species. Site occupancy by weeds varied with time as control operations
14 were intermittently either included or excluded from treatments over a period of four
15 years. There were four randomized complete blocks of 8 weed control treatments.
16 Potentially useable light sum was estimated using measurements of radiation from a
17 meteorological station that were modified by coefficients representing the ability of the
18 crop plants to use light with varying soil water, vapour pressure deficit, and temperature.
19 Light sums were further reduced by estimated competition for light from weeds. Fits of
20 the model to individual plots within the experiment yielded coefficients that did not differ
21 significantly weed control treatments, suggesting that the model accounted for significant
22 variations in growth resource availability between treatments. Potentially useable light

sum equations provide an integrated link between traditional mensurational modeling and ecophysiological modeling.

Introduction

Forest scientists have long been aware of the importance of light (Zon, 1917), and many studies have explored the direct interception of light by competing vegetation (Cannell and Grace, 1993; Comeau et al., 1993; Yunusa et al., 1995; Richardson et al., 1996; Seo et al., 1997; Comeau et al., 1998; Richardson et al., 1999; Kimberley and Richardson, 2001; Watt et al., 2003a). Weeds also affect local growth resource availability, particularly soil water and nutrient supply (Mead et al., 1993; Richardson, 1993; Richardson et al., 1993; Yunusa et al., 1995; Richardson et al., 1996; Richardson et al., 1997; Kirongo et al., 2002; Richardson et al., 2002; Watt et al., 2003c; Watt et al., 2003a; Watt et al., 2003b; Watt et al., 2004).

Local microclimatic conditions modify crop growth by mediating light use. Net primary productivity (NPP) of a plant canopy has been found to be directly proportional to light interception (Monteith, 1977), and local microclimate affects the slope of the relationship between intercepted light and NPP. The 3-PG model explicitly represents this principle for forest crops by calculating soil water, vapour pressure deficit, temperature and fertility modifiers on use of intercepted photosynthetically active radiation (Landsberg and Waring, 1997). The 3-PG model can be expressed as:

$$NPP = \varepsilon \sum_{t=1}^T APAR_t \min\{f_{\theta} f_D\} f_T f_F f_S \quad (1)$$

2

3 Where NPP=net primary productivity, t= time interval (month), APAR=absorbed
4 photosynthetically active radiation, ε =maximum quantum efficiency for a species, f_{θ} =soil
5 water modifier (0-1), f_D =vapor pressure deficit modifier (0-1), f_T =temperature modifier
6 (0-1), f_F =frost modifier (0-1), f_S =senescence modifier (0-1). The model maintains a soil
7 water balance using soil depth, soil type, rainfall, temperature, LAI and the Penman-
8 Monteith equation for calculating evapotranspiration to calculate the soil water modifier.
9 Most modifiers are calculated using generally understood processes, such as the
10 logarithmic decline of stomatal conductance with increasing vapour pressure deficit. The
11 fertility modifier is simply a number chosen by the user.

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13 Once NPP has been estimated for a given month, the amount of photosynthate used for
14 respiration is calculated using a constant supplied by the user, and the rest is allocated to
15 foliage, stems or roots. Allocation coefficients are estimated from measurements of
16 allometry, assuming that lower fertility results in increased allocation to roots. The actual
17 proportions allocated to these pools depend on coefficients supplied by the user that make
18 allocation vary with tree diameter at breast height.

19

20 The 3-PG model has attracted plenty of interest, but it has a few characteristics that forest
21 mensurationists usually try to avoid. It is not path invariant (Clutter, 1963; Clutter et al.,
22 1983), and it has many estimated parameters so that it might be fitted to the same dataset
23 in a variety of ways and users need to fit parameters locally to sub-models so that the

1 model will represent any given species in a particular location. Carbon allocation is
2 derived from allometry, which may lead to slight biases in allocation, and estimating leaf
3 area index can be problematic. The senescence modifier is *ad hoc*, and reflects the fact
4 that senescence is poorly understood. In addition, it is highly recursive, so that errors
5 may propagate when dependent variables from one month's simulation are used as
6 independent variables during the next month.

7
8 Mensurational models are precisely estimated from growth data obtained from permanent
9 sample plots and often represent growth and yield very efficiently, but they are highly
10 abstract, and therefore they are not sensitive to changes in factors affecting growth such
11 as climate. Some models have been built that include effects of environmental factors
12 and management activities on juvenile crops (Mason and Whyte, 1997; Mason, 2001)
13 that have more desirable properties from a mensurationist's point of view. The
14 abstraction of these approaches limits their capability to represent a highly dynamic
15 system with changing weed and microclimatic influences. The equation used to represent
16 yield of juvenile tree crops is often (Belli and Ek, 1988; Mason and Whyte, 1997; Mason,
17 2001; McKay and Mason, 2001):

$$Y_T = Y_0 + \alpha T^\beta \quad (2)$$

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19
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21 Where Y_T = estimate of variable Y at time T , T =time in years, and α and β are estimated
22 parameters. Estimated parameters are sometimes linearly related to site, vegetation
23 management, site preparation, and seedling quality effects. Equation (2) allows for a

1 decline in relative growth rate that occurs as juvenile trees grow (Britt et al., 1991; South,
2 1991; Mason and Whyte, 1997; Mason, 2001; Kirongo and Mason, 2003).

3
4 The idea explored in this paper is that a synthesis of mensurational models and
5 physiological approaches like 3-PG can be built by directly substituting potentially used
6 radiation sum for time in mensurational equations such as equation (2). With such a
7 synthesis no attempt is made to directly measure APAR, nor is carbon allocation
8 explicitly represented. Yield equations used for juvenile trees and sigmoid equations
9 used for older crops implicitly represent effects of APAR and allocation on relative
10 growth rate. Using modifiers such as those in the 3-PG model to assess what proportion
11 of incoming light could potentially be used by plants if it were intercepted makes these
12 hybrid equations sensitive to changes in growth resource availability that may be
13 influenced by weeds, changing sites, or varying weather patterns from year to year.

14
15 The hypothesis formally tested during this study was that parameters of a potentially
16 useable light sum model fitted to the range of treatments in a powerful, complex weed
17 control experiment would not differ significantly between treatments. This test compared
18 estimates of growth resource availability in the fitted model with “class” level effects of
19 weed control treatments. Moreover, it was postulated that, as a contrast, a time-based
20 model fitted to individual plots within the same experiment *would* yield estimated
21 coefficients that differed significantly between weed control treatments.

22 23 **Methods**

Overview

The following model was fitted to ground-line diameter (GLD) measurements from a weed control experiment in Oregon:

$$Y_T = Y_0 + \alpha R_T^\beta$$

$$R_T = \sum_{t=1}^T R_t \min[f_\theta f_D] f_T f_{CI} \quad (3)$$

Where Y_T =GLD at time T , α and β are parameters estimated from the dataset, R_t =radiation in month t , R_T =potentially useable light sum, f_θ =soil water modifier (0-1), f_D =vapor pressure deficit modifier (0-1), f_T =temperature modifier (0-1), and f_{CI} =light competition modifier. This model is a blend of key sub-models from model 3-PG and a commonly used mensurational equation that avoids the need to directly estimate absorbed photosynthetically active radiation, does not require estimates of carbon allocation, and can be both fitted and used without recursion.

A Critical Period Threshold (CPT) experiment in Oregon was selected for the study. CPT studies have been used in forestry for evaluation of vegetation management schedules (Wagner et al., 1999), and they implicitly represent two-sided competition between crop trees and weeds with extreme variations in timing of weed and tree interactions. Modeling growth in such a study using traditional mensurational techniques would be difficult because mensurational methods do not explicitly represent effects of changing resource availability when they vary from year to year within plots.

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The selected experiment was at latitude 44°37' N and longitude 123°35' W in the Oregon coast mountain range, on an Apt clay soil at an elevation of 250 m, and was a species by competition factorial design with four randomized complete blocks (Rosner and Rose, 2006). The site was located on gentle slopes with two blocks on each of two aspects. Container-grown stock of four tree species were planted on the site, but only plots containing *Pseudotsuga menzeisii* were used for the study described here. Competition treatments included a range of annual weed control operations through five years:

OOOOO	OOTTT	OTTTT
TOOOO	TTOOO	TTTOO
TTTTO	TTTTT	

Where each letter represents a year, O=no weed control and T=weed control. Trees were planted at 3.1 x 3.1 m in late January of 2000, and each square plot contained 64 trees. The middle 36 trees were measured in each plot.

The ground-line diameter (GLD) and height of each tree was measured after planting, and each October thereafter. Weed species and % cover within 1 m of each tree were estimated every July by placing a frame around each tree that was divided into quadrants and ocularly estimating the % cover.

1 A soil pit was dug on the site during the winter of 2005/2006 following several days of
2 rain, and the depth of roots was measured. Soil cores were extracted using a 101.29 cm³
3 soil corer at six depths separated by 15 cm and beginning at 7.5 cm from the soil surface.
4 Gravimetric moisture content, dry bulk density and wet bulk density of each core were
5 measured in a laboratory. Dry bulk density ranged from 0.98 in the top sample to 1.14 at
6 82 cm below the soil surface. Gravimetric moisture content at field capacity was found
7 to be 0.4, and approximately 95% of roots were within 45 cm of the soil surface. Given
8 that the soil was clay, gravimetric moisture content at zero plant available water was
9 assumed to be 0.2, and this yielded a maximum available soil water (ASW) estimate of
10 180 mm and a minimum ASW of 90 mm.

11 *Weed cover*

12 The weed cover in each treatment varied in accordance with prescriptions until year
13 three, when a followup vegetation management operation was not conducted (Figure 1).
14 The missing followup operation did not detract from the study reported here, as the
15 measured % cover of weeds, not the nominal treatment schedule, was used to run the
16 water balance model.
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19 Leaf area index (LAI) was needed for both trees and weeds in each month in order to run
20 a water balance model. LAI of trees within 3.14 m² circles at each measurement time was
21 calculated from $GLD^2 \times \text{height}$ using an equation fitted to destructively sampled juvenile
22 Douglas fir trees (Shainsky and Radosevich, 1992). Weed LAI was calculated in two
23 ways: (1) by assuming that the 100% weed cover for the predominant grass and forbs on

the site was at an LAI of 3.5, and directly scaling LAI to % cover estimates; and (2) by assuming that individual weed species would reach maximum LAI values as those reported in the literature (Breuer et al., 2003) when they reached 100% cover and maximum reported heights for the species (Breuer et al., 2003). Heights were estimated for each competing life form and for each time since treatment by the person who conducted the weed surveys. The first of these methods would be more accessible to forest managers, while the second might be more accurate. LAI estimates for intervening months were estimated by multiplying the difference in LAI between two measurement dates by the following equation:

$$LAI_x = LAI_p + (LAI_N - LAI_p) \int_{X_p}^x \sin(x / 6 * \pi + 1) / 12 \quad (4)$$

Where x=month number (January=1, February=2, etc.) with negative numbers -1 and -2 for November or December, X_p = the previous October, and a shift in x of minus three to get periodicity of change in line with seasons. LAI_p and LAI_N were LAIs estimated from measurements in the previous and next October, respectively. This implied that little growth in LAI would occur over the winter months, and that most change would occur in the spring and early summer. Where vegetation management treatments had been applied the same equation allowed for a gradual change in weed LAI during early spring prior to the new weed % cover estimate in July. Resulting estimates of monthly leaf area index in each treatment are shown in Figure 7b.

Weather data

A tipping bucket rain gauge was established on the site during June 2000, as well as an electronic air temperature gauge (the instruments were supplied by Onset Computer Co.,

1 Bourne, Massachusetts, USA). Temperature was measured every hour from that point
2 on. The temperature record contained a few small gaps, and these plus rainfall estimates
3 between January and June 2000 were filled with measurements from a meteorological
4 station 50 km away at Corvallis run by the Oregon Climate Service, Department of
5 Oceanic and Atmospheric Sciences, Oregon State University. The Corvallis station was
6 at 90 m elevation. The study called for the use of monthly summaries of weather data,
7 and so the filling of gaps with data from a close meteorological station was deemed
8 reasonable. Comparisons of on-site weather measurements with those at the Corvallis
9 station during periods when both had data showed that monthly estimates were very
10 similar at both sites. Mean daily maximum, minimum and mean temperatures were
11 calculated for each month, as well as total monthly precipitation.

12
13 Monthly radiation estimates were obtained from the University of Oregon's Solar
14 Radiation Monitoring Laboratory on-line from <http://solardat.uoregon.edu/>. The Eugene
15 radiation station used was at latitude 44.05 N, longitude 123.07 W and at an elevation of
16 150 m.

17
18 Monthly weather and LAI estimates were assembled as related tables in a database, and
19 then a water balance model was run over the first four years of measurements in each
20 plot, using a monthly time step.

21
22 Monthly rainfall, mean temperature and mean daily radiation are shown in Figure 2. As
23 can be seen, the site was characterised by wet, cold winters and warm dry summers, with

extremes in radiation due to clouds and low sun angles during winter followed by clear skies and high sun angles during summer.

Modeling soil water

The water balance model was identical to that used in 3-PG (Landsberg and Waring, 1997) except that parameters required for the Penman Montith equation were weighted averages, with LAI estimates of weeds and trees used as weights. Individual parameter estimates used are shown in Table 1. The water balance modifier used for light sums was also identical to that used in the 3-PG model.

Vapour pressure deficit was estimated from mean daily maximum and minimum temperatures by assuming that vapour pressure deficit was 0.5 times the saturated vapour pressure at the maximum temperature minus saturated vapour pressure at the minimum temperature.

A VPD modifier was used that is identical to that used in the current version of the 3-PG model. It was represented as:

$$f_D = \exp(-0.05 * vpd) \quad (5)$$

Where vpd=vapor pressure deficit. This modifier was also used to calculate stomatal conductance from maximum stomatal conductance in the water balance model.

A temperature modifier, also identical to that used in the 3-PG model was based on the minimum, optimum and maximum temperatures for photosynthesis as:

$$f_T(T_a) = \left(\frac{T_a - T_{min}}{T_{opt} - T_{min}} \right) \left(\frac{T_{max} - T_a}{T_{max} - T_{opt}} \right)^{(T_{max} - T_{opt}) / (T_{opt} - T_{min})} \quad (6)$$

where $f_T = 0$ if $T_a \leq T_{min}$ or $T_{max} \leq T_a$, and T_{min} , T_{opt} and T_{max} were the minimum, optimum and maximum temperatures for net photosynthetic production.

Competition for light

Competition for light was estimated using the ratio of squares of weed and crop mean heights times the % cover of weeds as a competition index and the following equation to estimate light transmission to crop plants (Richardson et al., 1999):

$$CI = \frac{H_{weeds}^2}{H_{crop}^2} C$$

$$f_{CI} = 1 - (1 - \exp(-0.76 * CI))^{1.289} \quad (7)$$

Where f_{CI} =light competition modifier, CI=competition index, H=heights of weeds or crops as noted, and C=percentage cover of weeds.

Fitting the potentially useable light sum model

Potentially useable light sums (see equation 3) were then calculated for each month in each plot. Those sums that corresponded to times of tree measurement were extracted

1 from the table using a SAS (SAS-Institute-Inc., 2000) DATA step, and then model (3)
2 was fitted to measurements of GLD. PROC NLIN was used to fit the model to each plot,
3 and then the fitted coefficients, α and β , were subjected to analysis of variance using the
4 formal experimental design so that and significant differences between them could be
5 identified. The same within plot NLIN fitting procedure and subsequent analysis of
6 variance test was applied to model (2), using time as the principal independent variable,
7 to determine whether or not the experiment would yield significant differences between
8 coefficients when effects of weeds on growth resource availability were not explicitly
9 accounted for.

10
11 An overall model (3) was also fitted to all plots simultaneously. In this latter model
12 estimates of α and β were identical for all plots, unlike former implementations of
13 equation (2) (Mason, 1992; Mason and Whyte, 1997; Mason, 2001).

14
15 Residuals were graphed, and the normality of residuals was tested using PROC
16 UNIVARIATE in SAS using the “plot normal” options. This included a Shapiro Wilkes
17 test for deviation from normality.

19 **Results**

21 *Overview*

22 Figure 3 shows graphs of ground line diameter for all plot averages with either time or
23 potentially useable light sum on the x-axis. Ground line diameter was much more

1 correlated with potentially useable light sum than with time. Figure 3 shows the plot
2 against a light sum calculated using weed LAI values estimated from the second, more
3 complicated technique, however, results were similar for both methods of LAI
4 calculation.

6 *Observed and modeled GLD development*

7 Mean observed GLD development in the treatments reflected the highly variable
8 applications of vegetation management treatments (Figure 4). Treatments subjected to
9 early vegetation management and later weed infestation generally exhibited higher initial
10 growth trajectories but then lagged behind other treatments where vegetation
11 management was applied for more years. In some cases trajectories crossed each other.

12
13 Residuals from model (6) applied to all data simultaneously, and using the complex
14 measure of weed LAI, were within ± 10 , had a root mean square error of 30.1, and
15 exhibited very little heteroscedasticity (Figure 5). Residuals from this model were only
16 slightly skewed, and had a Shapiro-Wilkes W statistic of 0.966, which indicated that
17 residuals deviated slightly from a normal distribution ($P < 0.0027$). They exhibited very
18 little bias, however (Figure 5). Plots of mean treatment trajectories from the model are
19 shown in Figure 6. Using simple estimates of weed LAI (with 100% weed cover equal to
20 an LAI of 3.5) resulted in a small increase in the root mean square error to 30.4.

21 Removing the light competition modifier meant that the root mean square error of the
22 more complex LAI estimation model increased to 30.9, indicating that light competition

was relatively minor compared to competition for water. The final yield equation for model (3) using values of computed potentially useable light was:

$$GLD_T = GLD_0 + 1.0298(R_T / 1000)^{1.6475} \quad (8)$$

Standard errors estimated coefficients (α and β of model (3)) were 0.0826 and 0.0377 respectively.

Comparison of overall fit with individual plot fits

Results of the analyses of variance of the coefficients of the PULSE model (3) fitted to each plot showed that neither the α nor the β coefficients differed significantly between weed control treatments ($P < 0.54$ and $P < 0.25$). By contrast the time-based model (2) yielded coefficients for each plot that were significantly different between weed control treatments ($P < 0.0003$ and $P < 0.0001$).

Discussion

A potentially useable light sum equation (PULSE) model accounted for very dynamic changes in growth patterns in the experiment described here with a very simple mensurational equation. Increasing plant size, access to site resources, and changing carbon allocation were implicit in the equation, and so estimates of absorbed photosynthetically active radiation, carbon allocation, and a recursive model structure

1 were not required. As coefficients for this model did not differ significantly between
2 weed control treatments, we can assume that the model accounted for critical differences
3 in growth resource availability brought about by the treatments. The result was a model
4 form that forest managers could reasonably access, understand and use. Weather inputs
5 for management use are now readily available on the internet (e.g.: see
6 <http://www.daymet.org>), and if LAI can be effectively estimated from simple measures of
7 plants, such as stem measurements or % plant cover, then using these techniques for
8 mensurational models will be easy. The analysis presented here showed that simple
9 measures were almost as effective as more complicated LAI estimation procedures based
10 on reported LAI maxima for individual weed species. If meteorological data are
11 provided as web services in the format of SOAP or Microsoft's .NET, then required
12 model inputs will be seamlessly integrated with model software. GIS layers might be
13 used to provide estimates of soils type as well as maximum and minimum ASW required
14 for the water balance model.

15
16 Leaf area indices are required for a water balance model. New optical tools such as the
17 LAI2000 (Licor Ltd.) make LAI measurement much less costly, and managers should
18 consider measuring LAI routinely in permanent sample plots so that models of LAI
19 development for particular species and stand structures can be created.

20
21 Fitting a standard statistical model to the development of GLD with time in this
22 experiment would have been difficult. High levels of variation in weed site occupancy
23 and changing site influences with time within the same plots would a necessitate an

1 analysis of change in GLD from year to year, and the resulting model would not reflect
2 site influences to the degree that model (6) did. Moreover, a purely statistical model
3 would have been excessively local, and would not have provided much insight into the
4 processes involved. For example, Figure 7a shows available soil water deficit plotted by
5 treatment against time.

6
7 Model coefficients presented here are not intended to be applied generally to young
8 stands of Douglas fir. This is a methods paper, and more intensive measurements of site
9 and plant parameters would be required in order to fit a more generalisable model. The
10 ease with which light competition was accommodated in the model represents a clear
11 advantage of this hybrid modeling approach.

12
13 Nutritional fertility of soil is not included in the model, nor is it properly accounted for in
14 3-PG. Identification of fertility modifiers for different soils, and research that reveals
15 why these fertility modifiers apply in specific situations is an urgent need.

16
17 Explicit estimation of absorbed photosynthetically active radiation (APAR) would be an
18 improvement over this technique in circumstances where maximum LAI is influenced by
19 management factors such as fertilization (Amateis et al., 2000; Ducey and Allen, 2001;
20 Allen et al., 2002; Albaugh et al., 2003; Westfall et al., 2004). In the study described
21 here, however, discontinuous tree canopies made estimations of APAR difficult. If forest
22 managers begin routinely estimating LAI by using either handheld optical devices or

remote sensing then mensurational models that employ used light sums will become feasible.

The idea that time is equivalent to potentially useable or used radiation sums might be applied to growth and yield modeling with difference equations. Having separate light sums for primary and secondary growth in order to account for their different phenologies may offer flexible models that account for differences in tree form caused by seasonal differences in climate. This topic will be addressed in a future paper.

The methodology described here offers researchers and managers a synthesis between mensurational and physiological modeling techniques that will facilitate the inclusion of research findings into operational models, and may provide managers with more site-specific estimates of the effects of management activities in forests. Specifically representing growth resource limitations in models clarifies how these limitations might be reduced and growth rates thereby increased.

Conclusions

A potentially useable light sum model of ground line diameter development for four years after planting was fitted to individual plots within a complex weed control experiment.

The fits yielded coefficients that did not differ significantly between weed control treatments. A time-based model fitted to the same data yielded parameter estimates that did vary significantly between treatments.

An overall model fitted to the experiment (equation 3) had 95% of residuals between +4 and -4 mm.

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8

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1 Table 1 – Parameter used in modifier models

2

Modifier	Parameter	Value	Units	Reference
Water balance	Max stomatal conductance - trees	0.018	m/sec	(Coops and Waring, 2001)
	Max stomatal conductance - weeds	0.018*	m/sec	
	LAI for maximum canopy conductance	3.33		J.J. landsberg, pers. comm.
	Boundary layer conductance - trees	0.2	m/sec	(Landsberg and Waring, 1997)
	Boundary layer conductance - weeds	0.25*	m/sec	
	Intercept of net radiation relation - trees	-90	watts/m ²	J.J. Landsberg, pers. comm..
	Slope of net radiation relation - trees	0.8		J.J. Landsberg, pers. comm..
	Intercept of net radiation relation - weeds	-90	watts/m ²	
	Slope of net radiation relation - weeds	0.65		Inferred from relative albedos of forest and grassland (McNaughton and Jarvis, 1983)
	Maximum available soil water	180	mm	This study
	Minimum available soil water	90	mm	This study
	LAI for maximum rainfall interception	4		J.J. Landsberg pers. comm..
Temperature	Maximum temperature for photosynthesis	40	°C	(Lewis et al., 1999)
	Optimum temperature for photosynthesis	20	°C	(Lewis et al., 1999)
	Minimum temperature for photosynthesis	-2	°C	(Lewis et al., 1999)
	Exponential decay parameter	-0.5		(Landsberg and Waring, 1997)
Vapour pressure deficit				
Light competition	M1	-0.760		(Richardson et al., 1999)
	M2	1.289		(Richardson et al., 1999)

3 *Estimates for simple LAI estimation only. Estimates of these parameters varied as LAIs
 4 of different species varied within plots (Breuer et al., 2003) for the second LAI
 5 estimation procedure.

Figure captions

Figure 1 – Percent weed cover by year and treatment. When weed species overtopped each other, then cover could exceed 100%.

Figure 2 – Monthly rainfall, radiation and mean temperature during the period of the study

Figure 3 – Plots of plot mean ground line diameter against time (top) and potentially useable light sum (bottom)

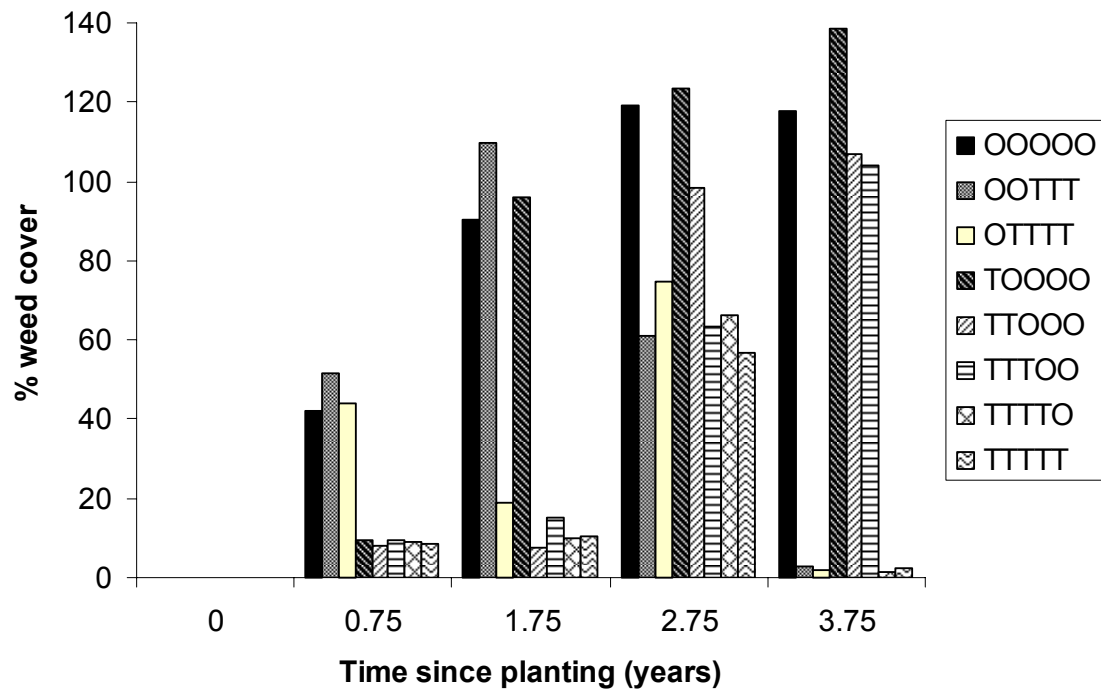
Figure 4 – Ground line diameter by vegetation management treatment

Figure 5 –Residual vs predicted ground line diameter for the potentially useable light sum model

Figure 6 – Monthly plot of modelled ground line diameter by treatment using the PULSE approach

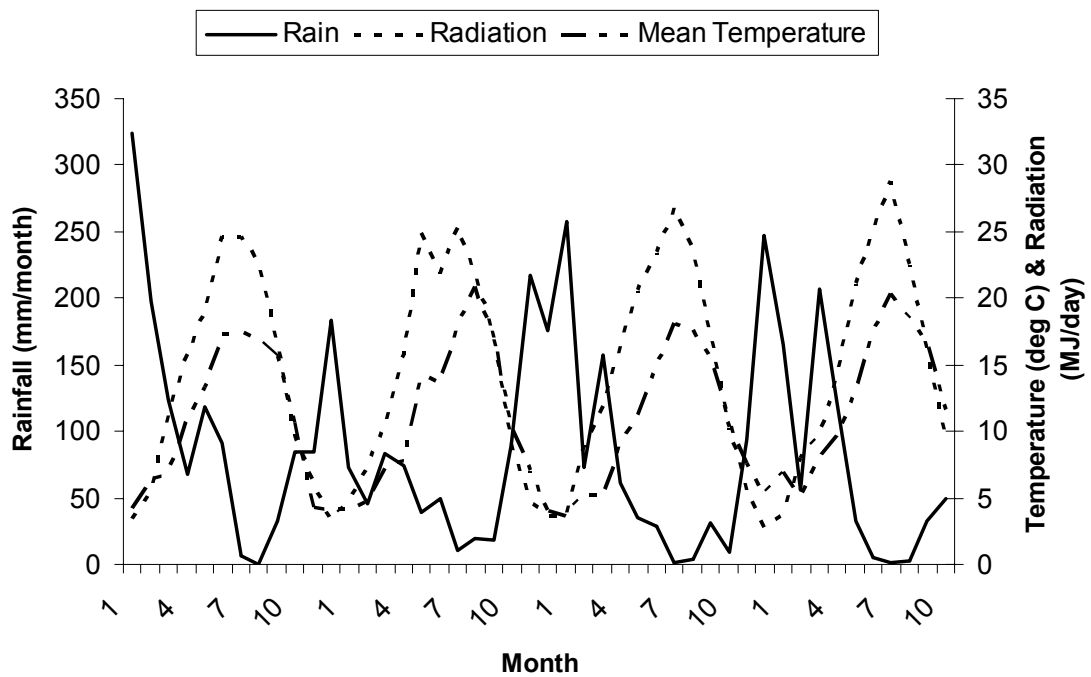
Figure 7 – Monthly available soil water deficit (top), and LAI by treatment (bottom)

1 Figure 1
2



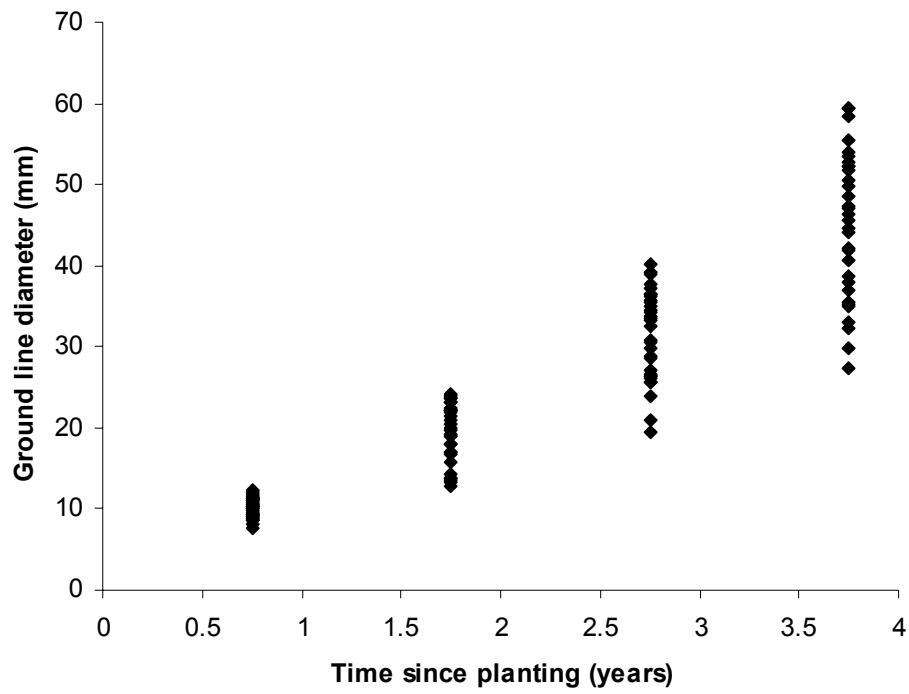
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1 Figure 2
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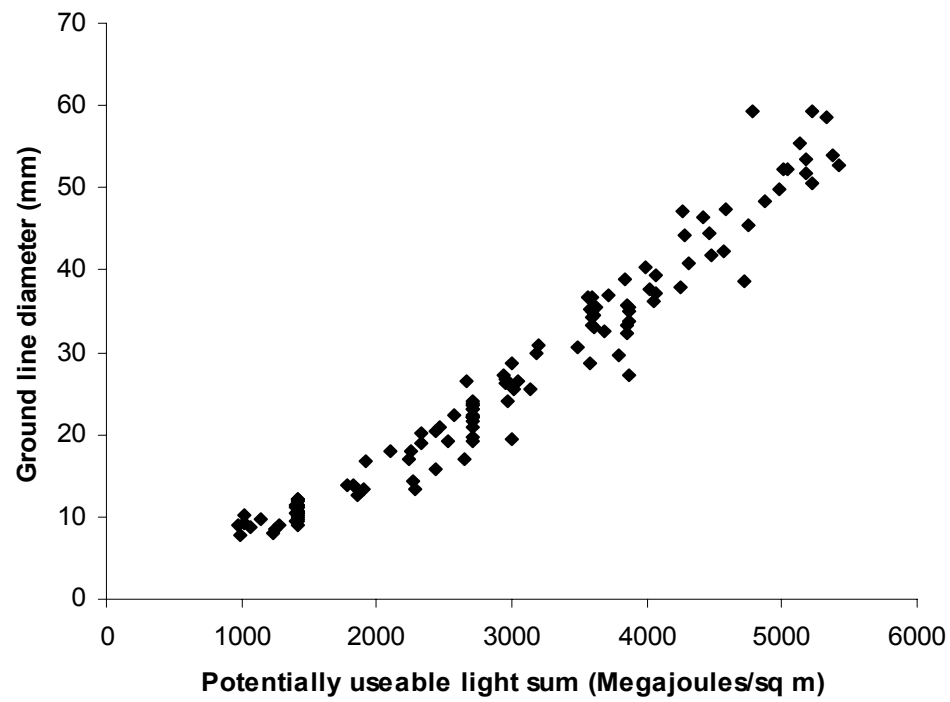


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1 Figure 3
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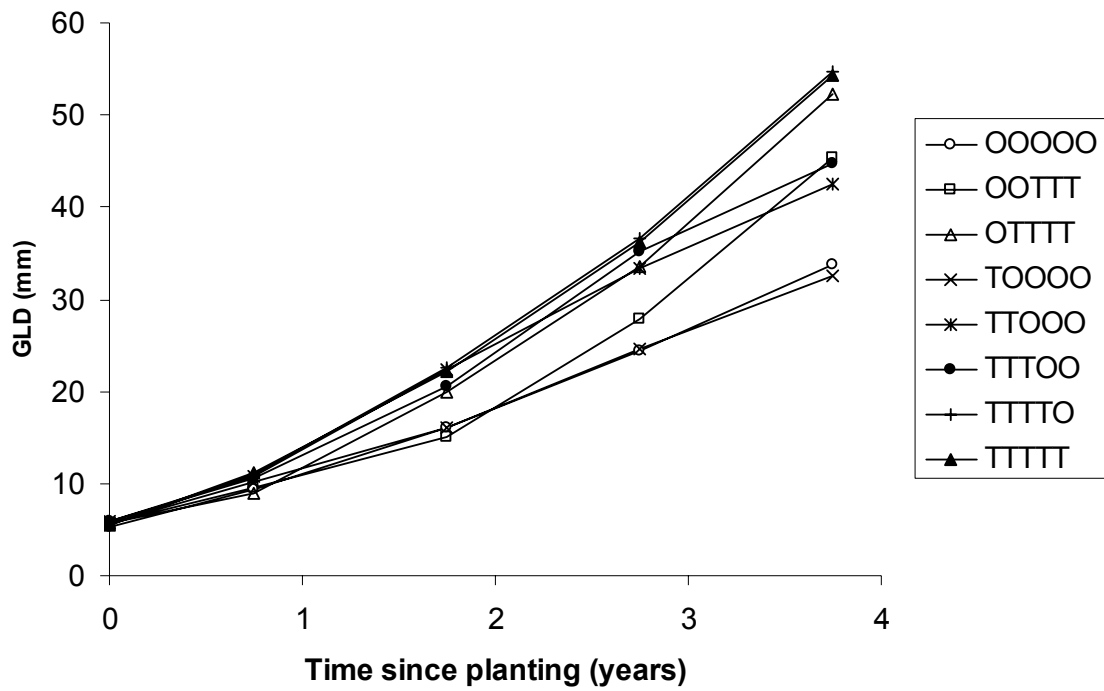
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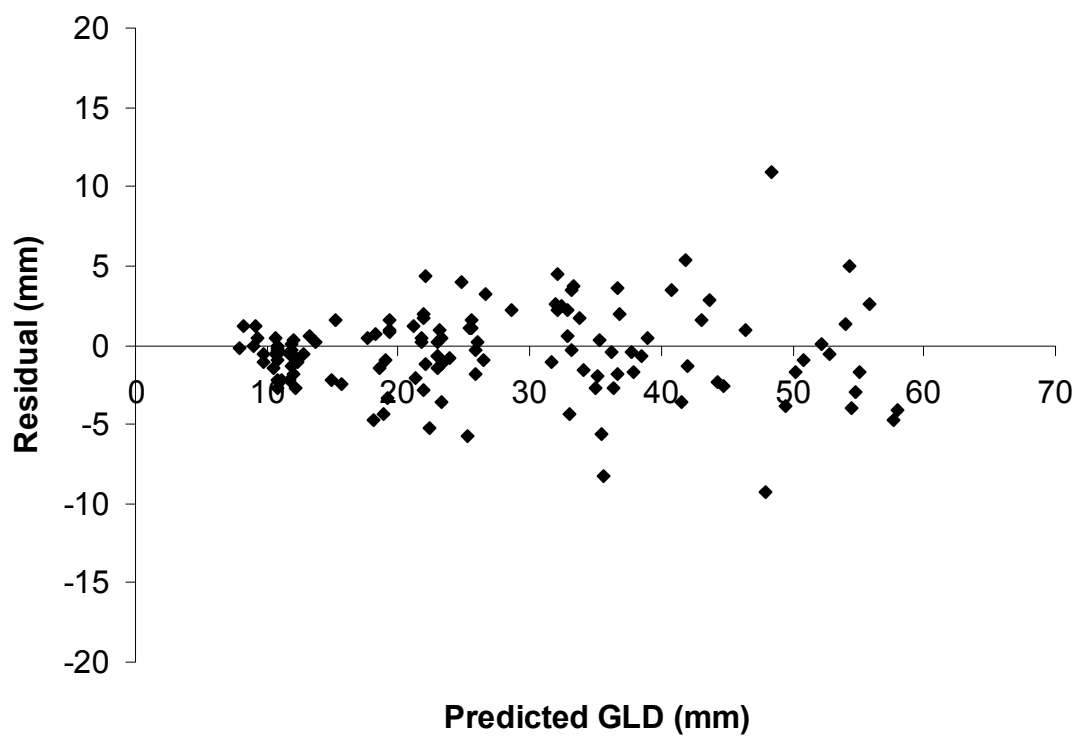
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Figure 4



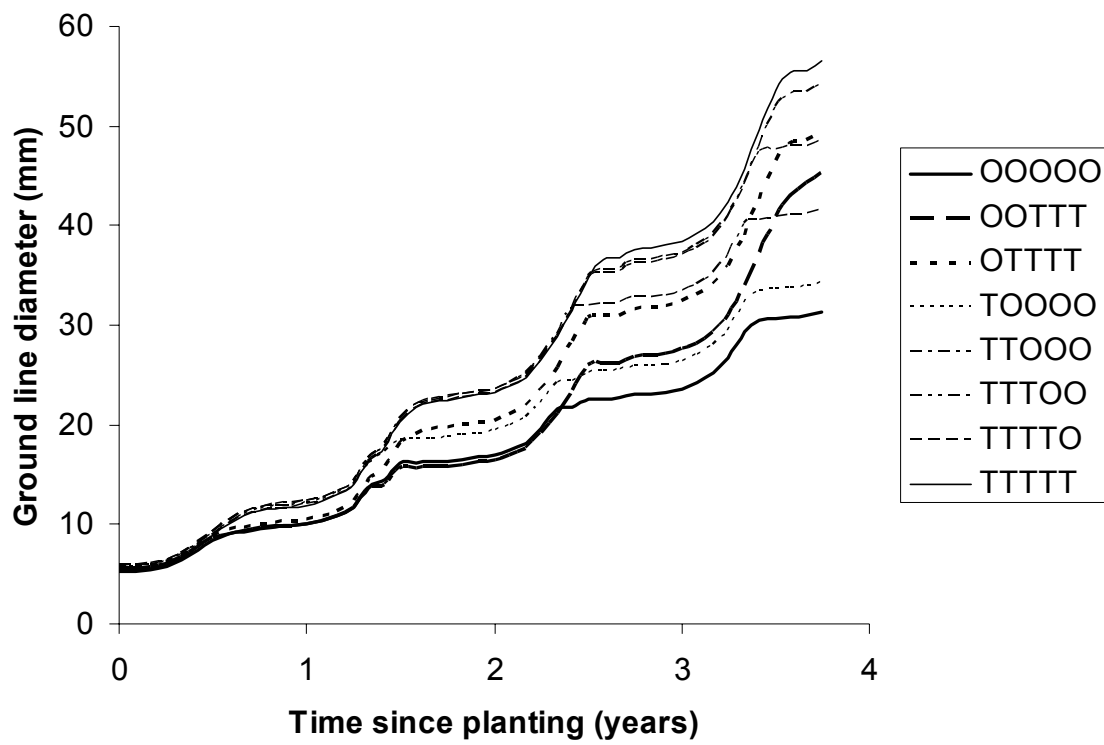
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1 Figure 5
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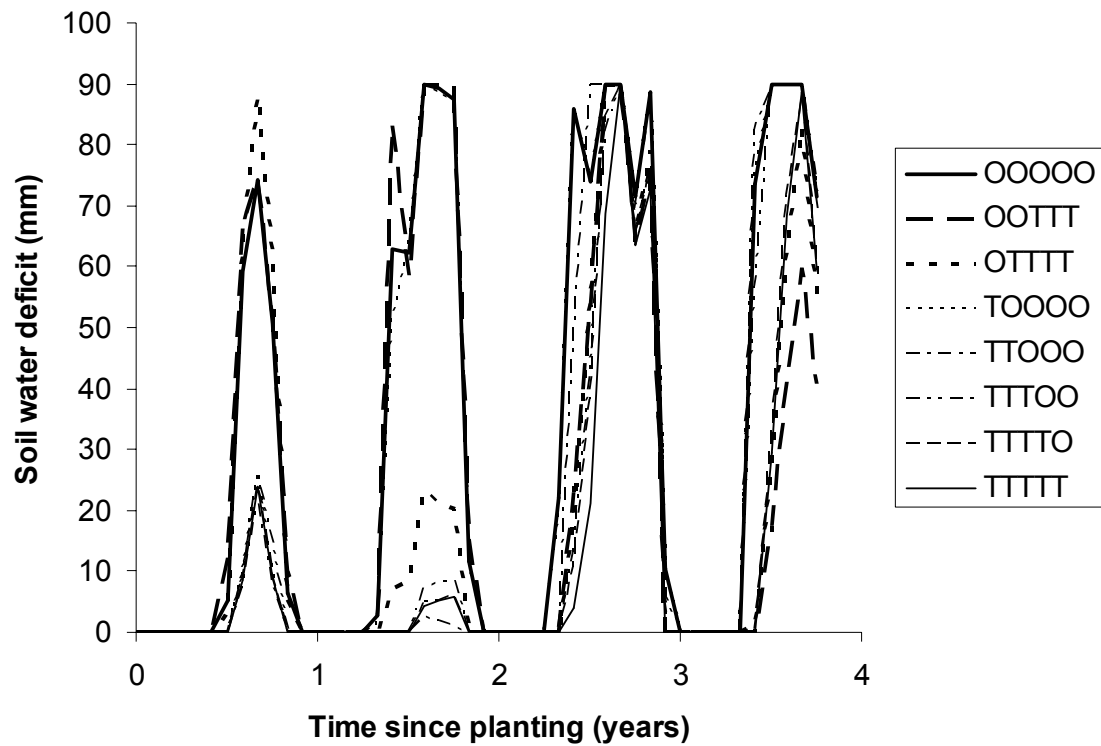
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1 Figure 6
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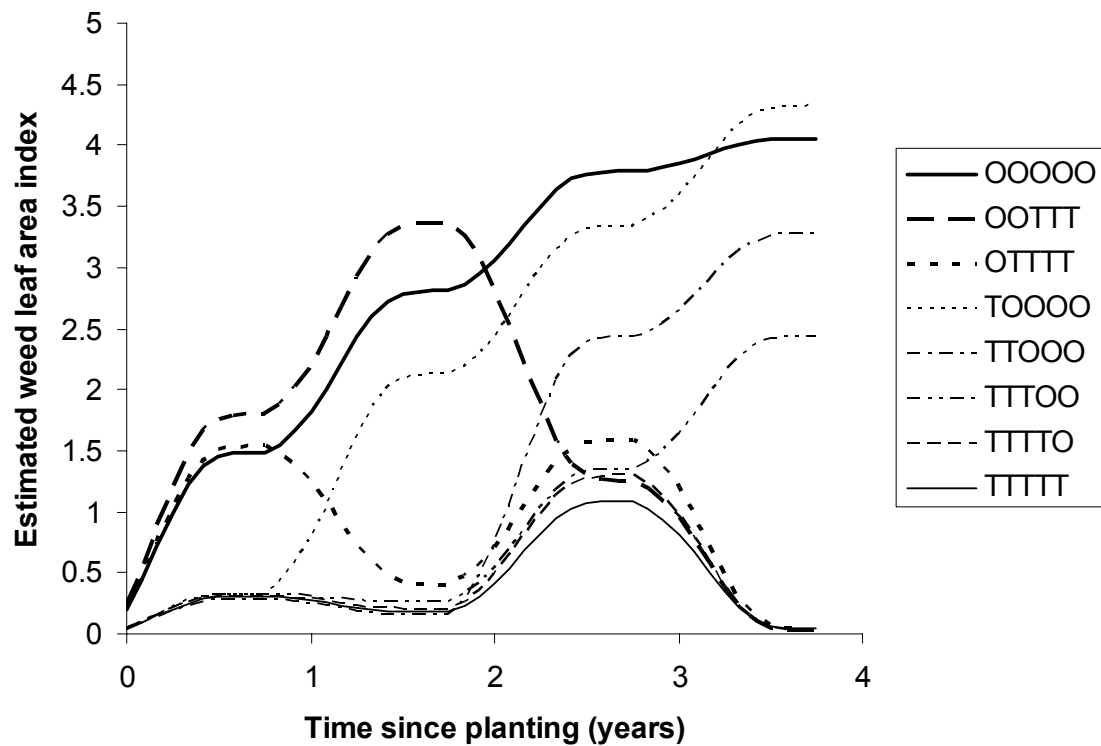


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1 Figure 7
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