# Stress-Density Model Validation: Free-Field Liquefaction Analysis Using OpenSees

## Introduction

- Numerical liquefaction analyses require verified and validated constitutive models.
- Complexity of simulating liquefactioninduced phenomena, emphasises the need to enhance current models' performance and/or to develop new constitutive models.
- Stress-density [1,2] (S-D) is a constitutive model that has been recently verified and implemented in the finite element platform, OpenSees.
- This study, as the first effort to validate the stress-density model against centrifuge tests in OpenSees, encapsulates the 1D site response results.
- PM4Sand [3] is a widely used constitutive model that we also used in this study for comparison.

### Method

- Results of two centrifuge tests [4,5] (~140 sensors, 55g in a 9 meters radius machine) are used for validation.
- Both tests have similar plans. The key variation is that the relative density of the liquefiable layer decreased from 50% in test T4.5-50 to 40% in test T4.6-40. Other changes are structural.
- Calibration of the model (Figure 1) intended to simulate the experimental liquefaction triggering curve for the (Nevada) sand, which comprises two important layers in the centrifuge tests.

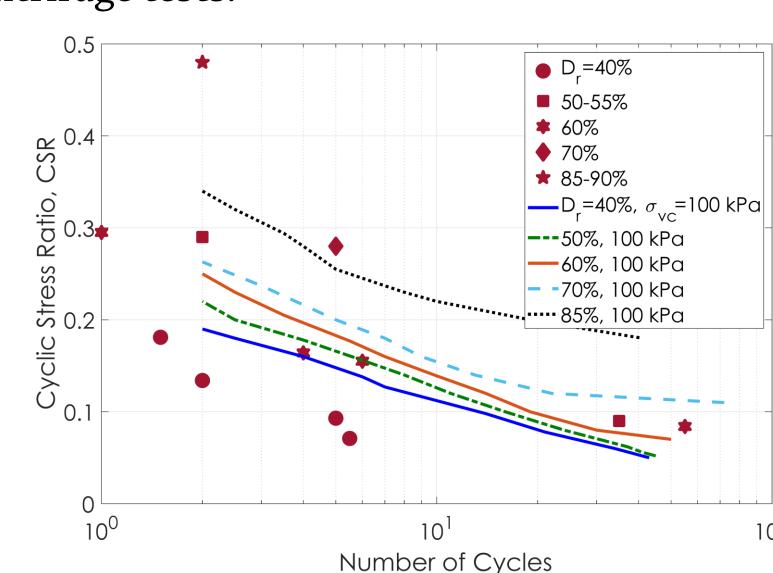


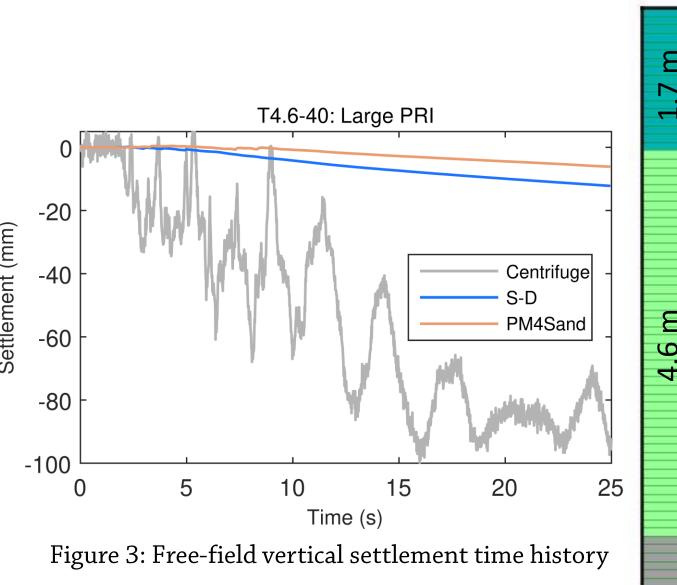
Figure 1: Relation between the number of cycles required to reach liquefaction (double-amplitude shear strain of 3%) and cyclic shear stress ratio (CSR) in numerical simulations (lines) and CSS experiments (markers)

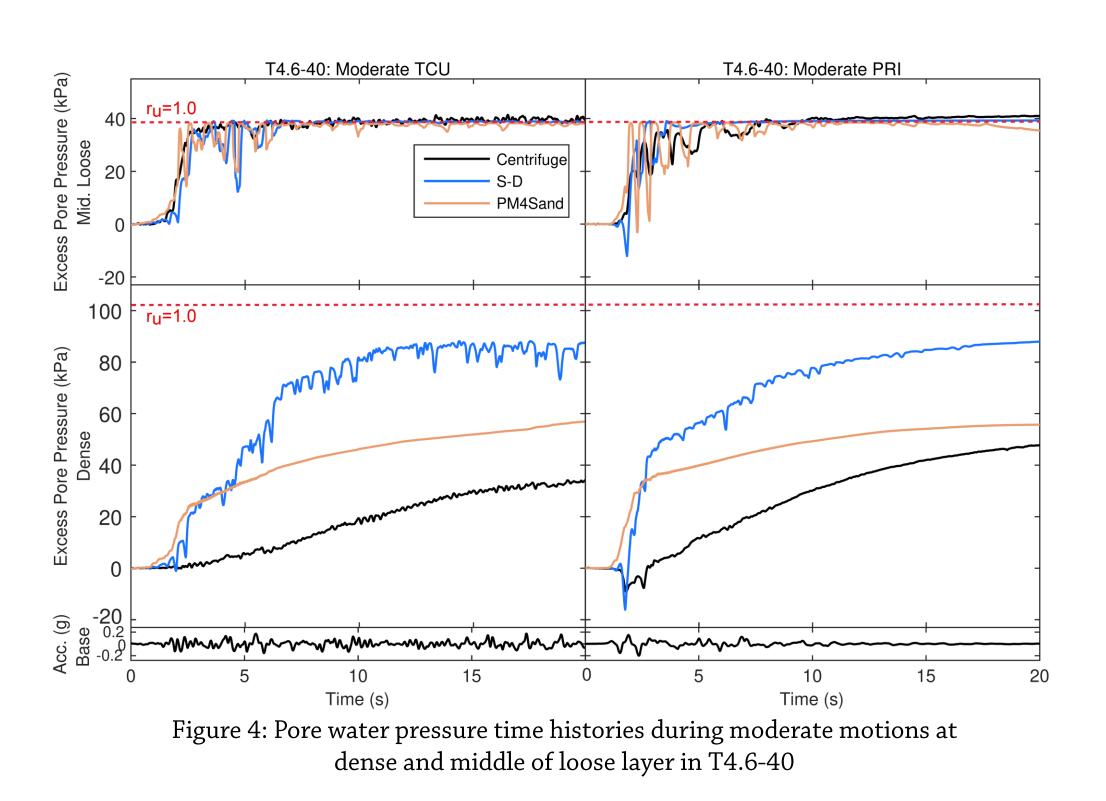
### Modelling

- We performed one-dimensional effective stress analysis using OpenSees.
- Figure 2 (depicted in the *Results* section below) illustrates the schematic 1D model for the T4.6-40. The T4.5-50 profile is very similar to T4.6-40, which is not presented for brevity.
- Mesh sensitivity analysis showed that an element size around 0.2 m provides reliability up to 10 Hz. However, to match the sensor locations in the centrifuge tests we used 0.1x0.1 mesh.
- The input motions applied to the bottom of the numerical model are the recorded motions at the base of the centrifuge container. Their names are: large PRI, moderate PRI, moderate TCU and small PRI.
- Rayleigh damping of 2% was applied at natural frequency of 1.88 Hz and third modal frequency of soil deposit (9.39 Hz).

# Results

Figure 3 shows that S-D PM4Sand models underrate the free-field settlement during the large PRI in the T4.6-40 🔋 approximately by a factor 5 of 7.5 and 13 after 25 \( \frac{1}{8} \) -60 respectively. seconds, models Constitutive normally fail to capture free-field settlements caused by partial drainage.





Centrifuge and simulations indicate liquefaction at the middle of the loose layer for both motions (Figure 4). At the dense layer the S-D model overpredicts the response by approaching the excess pore water pressure ratio  $(r_{11})$  to 0.8, which denotes a near-liquefaction state.

# T4.5-50: Moderate TCU T4.6-40: Moderate TCU Base Acc. T4.5-50: Moderate PRI Period (s)

Figure 5: Response spectra (5% damped) at surface during the Moderate PRI and Moderate TCU motions in T4.5-50 and T4.6-40

Figure 6 shows that during the large event, dilation spikes emerge in experiment and simulations. The overestimated pore water pressure in the dense layer that reflected from the single-element response of the S-D model support the large dilation spikes observed even in the middle of dense layer.

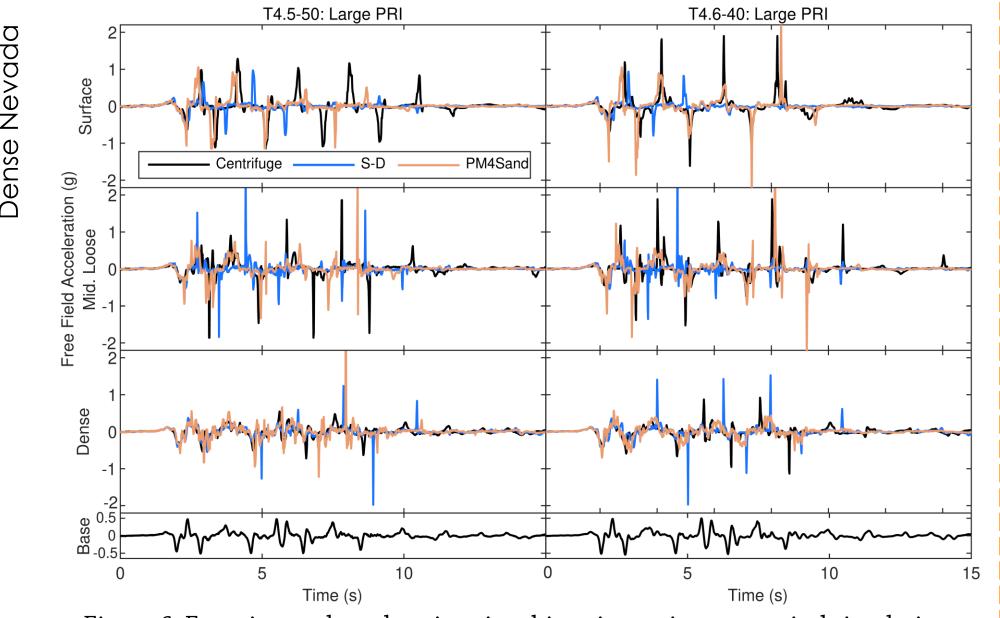


Figure 6: Experimental acceleration time histories against numerical simulations with S-D and PM4Sand models during the Large PRI motion in T4.5-50 and T4.6-40

- Figure 5 shows that during the moderate PRI event, the S-D model is in a reasonable agreement with the centrifuge for periods between 0.25 to 1.5 seconds.
- During the moderate TCU motion, the S-D model mostly overestimates the response except for periods longer than 2 seconds.
- Overestimation of response in highfrequency parts can be attributed to overestimation of dilation spikes by both models.

#### Conclusion

- The S-D model can reasonably predict the soil behaviour—acceleration, pore water pressure generation— in freefield site response analyses
- Looking at all events, the S-D model predicts the pore water pressure buildup pattern well in the liquefiable layer, while overpredicting that in the dense layer.
- The next step, which will follow the current study, is the validation of 2D models with structures that could lay the groundwork for using the S-D model in a wider area.

#### Acknowledgement

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[1] Cubrinovski, M. & Ishihara, K. 1998a. Modelling of Sand Behaviour Based on State Concept. Soils and Foundations, 38, 115-127. [2] Cubrinovski, M. & Ishihara, K. 1998b. State Concept and Modified Elastoplasticity for Sand Modelling. Soils and foundations, 38, 213-225.

[3] R. Boulanger, K. Ziotopoulou, PM4Sand (Version 3): A sand plasticity model for earthquake engineering applications, Center for Geotechnical Modeling Report No. UCD/CGM-15/01, Department of Civil and

Environmental Engineering, University of California, Davis, Calif, (2015). [4] J. Allmond, B.L. Kutter, J. Bray, C. Hayden, New Database for Foundation and Ground Performance in Liquefaction Experiments, Earthquake Spectra, 31 (2015) 2485-2509.

[5] J. Zupan, N. Trombetta, H. Puangnak, D. Paez, J. Bray, B. Kutter, T. Hutchinson, G. Fiegel, C. Bolisetti, A. Whittaker, Seismic performance assessment in dense urban environments: Centrifuge data report for test-5, University of California at Davis Center for Geotechnical Modeling Report No. UCD/CGMDR-XX/XX, Davis, CA, (2013).

[6] K. Arulmoli, K. Muraleetharan, M. Hossain, L. Fruth, Verification of liquefaction analysis by centrifuge studies laboratory testing program soil data, Technical Rep., The Earth Technology Corporation, Irvine, Calif, (1992). [7] A. Kammerer, J. Wu, J. Pestana, M. Riemer, R. Seed, Cyclic Simple Shear Testing of Nevada Sand for PEER Center: Project 2051999. Geotechnical Engineering Research Rep

Figure 2: 1D free-field model schematic



