A GA-BASED TRANSPORT MODAL CHOICE MODEL*

by Katia ANDRADE**, Kenetsu UCHIDA***, Seiichi KAGAYA***, Andre DANTAS**** and Alan NICHOLSON*****

1. Introduction
Application of soft computing techniques to transportation research has become very popular since the 70s, which formed a new category of travel behavior models sometimes called hybrid models. These models include neural networks, fuzzy logic and Genetic Algorithms (GA), and statistical methods. Hybrid models have been suggested for solving transportation problems in an attempt to explore the advantages of both methods, and here promising results have been found 1) 2). These techniques have been applied to various modeling problems such as: bicycle route choice behavior 3); modal choice model’s parameters and linguistic values estimation4); estimating household members’ transport modal choices5). However, these studies require complex decision structures and large computational processing for simulation. This limits the extent to which hybrid models can be applied in transport studies where there is a lack of time and resources.

This paper presents a hybrid transport modal choice model in which the genetic algorithm is applied for estimating parameters of a Multinomial Logit Model. The model has a simple decision structure which requires relatively modest computational capabilities and time to be estimated. Linear Utility Functions are defined for the transport modes which are included in the model structure as the fitness function. The objective function seeks to reduce the errors in the modal choice process. Moreover, the hybrid model incorporates distance as a spatial attribute variable for explaining commuters’ modal choices among automobile, bus, bicycle and walk modes. After this introduction section, a brief review on GA’s is presented. Section 3 introduces the Hybrid Transport Modal Choice Model structure, which is followed by the modeling results. Finally, Section 5 discusses this work’s findings and makes recommendations to further research.

2. Genetic Algorithms
Genetic Algorithms were initially suggested during the 70s6) as search technique used for approximating solutions in optimization problems. The GA’s are based on the evolution theory which considers that, in competitive scenarios, individuals with favorable traits are more likely to survive and reproduce as a result of the Natural Selection process 7). These algorithms are defined by three basic rules, in which the first is the Crossover, used for combining information from two or more individuals; the second is the Mutation, which generates new solutions from the current population, therefore allowing the exploration of new regions of the Search Space; and the third is the Selection of the fittest individuals, a process that ensures the continuing improvement of the candidate solutions 8). Presently, GA’s are widely used in solving problems on decision making, classification, and complex numerical optimization9), among other applications. In this context, it seems to be an adequate tool for use in transportation problems.

Amongst genetic algorithms, Real-Coded Genetic Algorithm (RCGA) is specifically applied to parameter estimation. The RCGA adopts a real coding of the optimization parameters. It includes a process called Real Biased Crossover, which produces two new individuals from their ancestors, where one of them is more similar to its “best” ancestor, i.e. the one presenting better value for the objective function10). This process ensures that there will be better individuals in the new generation, which does not happen for the so-called Simple Genetic Algorithm (SGA) in its basic form7). Table 1 summarizes the characteristics of the RCGA and its procedures.

3. Hybrid Transport Modal Choice Model Structure
The model employs the GA technique to conduct the modeling of the transport modal choice. In this model, GA’s main objective is to iteratively improve an initially random set of individuals9), which is formed by the choice among the automobile, bus, bicycle and walk modes. The procedures adopted for this search are the crossover among the selected good modal choices, and their further random mutation. In a constant-size population, only those individuals with high fitness are selected, whereas incorrectly predicted choices are dropped from the initial population. GA is able to find nearoptimal solutions for the investigated problem after a sufficient number of iterative applications of these two instruments 10).

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Table 1: RCGA characteristics and procedures

<table>
<thead>
<tr>
<th>Characteristics</th>
<th>Procedures</th>
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<tr>
<td>• Each parameter is described by a real number.</td>
<td>• Crossover: the population is divided in two parts, and the possibility of Biased crossover is verified (Probability of crossover equal to 0.8, with 50% of the crossings being biased ones).</td>
</tr>
<tr>
<td>• A valid interval is defined for parameter values.</td>
<td>• Mutation: the possibility of mutation for each individual is verified (Probability of mutation equal to 0.05).</td>
</tr>
<tr>
<td>• N random vectors are generated in the first stage of the algorithm.</td>
<td>• Evaluation: each individual is evaluated according to the objective function.</td>
</tr>
<tr>
<td>• The algorithm ends either by an imposed condition or by reaching the determined number of generation.</td>
<td>• Adjust Function or Fitness Function: the objective function is introduced in the adjusted function.</td>
</tr>
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(1) Model Input
The model input is composed by characteristics of the transport network and characteristics of a set of investigated commuters. The data used in this study was obtained from a data survey carried out in Christchurch, New Zealand. In this survey students and staff of the Canterbury University were targeted. Initially, several attribute variables obtained from the survey were analyzed so as to identify those which could be the most appropriate to model adequately the modal choices. This analysis was based on the extensively published literature about travel behavior models. Finally, travel time (TT), distance from household to the university (D), availability of parking place inside the university campus (P), availability of bus service (BS), and bicycle ownership (BO) were defined as the input attribute variables to the model. The distance between household and university was included in the model as a spatial variable, in an attempt of explaining the choices between motorized modes (automobile and bus) and non-motorized modes (bicycle and walk).

(2) Utility Functions
The fitness \( U \) is assumed as the linear modal Utility Functions. The fitness function quantifies the optimality of a solution or chromosome in a GA. In this study, the fitness functions were formulated as follows:

\[
U_{in} = \beta'_i + \beta_{TTi}TT_i + \beta_{Di}D_i + \beta_{BSi}BS_i + \beta_{Boi}BO_i, \\
\quad \forall i \in \{a : auto, b : bus , bc : bicycle, w : walk\}
\]

where \( \beta_{pi} = 0 \quad \forall \ i \neq a \), \( \beta_{BSi} = 0 \quad \forall \ i \neq b \), \( \beta_{Boi} = 0 \quad \forall \ i \neq bc \)

where \( U_{auto}, U_{bus}, U_{bicycle} \) and \( U_{walk} \) are the utilities of decision maker \( n \) for transport modes of automobile, bus, bicycle and walk, respectively; \( \beta'_i, \beta_{TTi}, \beta_{Di}, \beta_{BSi} \) and \( \beta_{Boi} \) are the parameters for alternative-specific constants for modes; \( \beta_{TTi}, \beta_{Di}, \beta_{BSi} \) and \( \beta_{Boi} \) are parameters for the measurable attribute variables of travel time, travel distance, parking at university, availability of bus service and bicycle ownership, specific to transport mode.

(3) Objective Function
The objective function to be minimized by the GA, with respect to \( \beta_{TTi}, \beta_{Di}, \beta_{BSi}, \beta_{Boi}, \beta_{TTbc}, \beta_{Di}, \beta_{Boi}, \beta_{TTw}, \beta_{Di}, \beta_{Boi} \), is the error \( E \) function, that is, the percent of wrong answers in the model estimation. The function \( E \) was formulated as:

\[
E = \frac{\sum_{n=1}^{N} e_n}{N},
\]

where \( N \) is the number of investigated samples (200 input-output data pairs were used during the training process); and \( e_n \) is the individual error (\( e_n = 0 \), if model output is equal to observed choice; and \( e_n = 1 \), otherwise).

(4) Characteristics of the RCGA
The conditions imposed to the real-coded genetic algorithm are summarized in Table 2.

Table 2: Calculation Conditions for the RCGA

<table>
<thead>
<tr>
<th>Condition</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population size</td>
<td>50</td>
</tr>
<tr>
<td>Number of function calls</td>
<td>10000</td>
</tr>
<tr>
<td>Mutation rate</td>
<td>0.05</td>
</tr>
<tr>
<td>Crossover rate</td>
<td>0.80</td>
</tr>
</tbody>
</table>
Model Estimation Probabilities
Multinomial Logit structure was applied for estimating choice probabilities. By following this structure, the probability of individual \( n \) selecting mode \( i \) from the choice set \( C_n \) can be written by Equation 3.

\[
P_{in} = \frac{1}{1 + \sum_{j \in C_n \land j \neq i} e^{\Delta U_{ijn}}} \quad (\forall j \neq i)
\]

where: \( \Delta U_{ijn} = (U_{in} - U_{jn}) \)

4. Results
The performance of the RCGA was initially measured by analyzing the average error across modal choices as shown in Figure 1. The performance analysis shows good behavior of the algorithm. Modal choices Error is equal to 27.5 percent in the initial iteration and reaches the minimum value of 16 percent after 4500 iterations, remaining constant after this point. The RCGA estimation parameters are summarized in Table 3, where all parameters have expected signs. The attribute variable distance is positive for motorized modes, whereas it is negative for non-motorized modes. This is in accordance with the survey results.

![Figure 1: Evolution of Error by Iterations](image)

Table 3: Parameter Estimation by the RCGA

<table>
<thead>
<tr>
<th>Mode</th>
<th>( \beta_i )</th>
<th>( \beta_{TTi} )</th>
<th>( \beta_{Di} )</th>
<th>( \beta_{P} )</th>
<th>( \beta_{BS} )</th>
<th>( \beta_{BO} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Auto</td>
<td>-0.4702</td>
<td>-0.7132</td>
<td>0.0501</td>
<td>1.2665</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bus</td>
<td>-5.9262</td>
<td>-0.5900</td>
<td>0.0747</td>
<td></td>
<td>2.2185</td>
<td></td>
</tr>
<tr>
<td>Bicycle</td>
<td>-1.1951</td>
<td>-0.8560</td>
<td>-0.0593</td>
<td></td>
<td></td>
<td>2.3146</td>
</tr>
<tr>
<td>Walk</td>
<td>-0.8575</td>
<td>-0.5100</td>
<td>-0.1457</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

A sensitivity analysis was performed so as to verify the influence of household distance to the working place in the modal choices (Figure 2). We focused on travelers’ behavior regarding motorized modes and non-motorized modes. As expected, the probability of selecting both automobile and bus increase with the distance. Additionally, it was observed that there is almost no variation on the probability of selecting bus mode up to a 20 Km distance. Figure 2 shows the probability of walking to the working place is very much influenced by the household distance. On the other hand, slight variation was observed in the probabilities of selecting bicycle mode, which might reflect that cycling does not compete directly with the other three modes. These sensitivity analysis results seem to reflect correctly the investigated scenario.
5. Discussion and Further Work

The Real-Coded Genetic Algorithm was used for estimating parameters to be used in a Multinomial Logit modeling framework. The fitness function was composed by linear utility functions of transport modes. The objective function was formulated so as to minimize the error across choices. The model displayed good performance by presenting a reasonable evolution of the error function across iterations and a final sixteen percent error in the simulation of modal choices in the validation data set. Additionally, the parameters presented appropriate signs. For example, the positive sign of the attribute variable availability of bus service (BS), suggests that improvements on the bus level of service would increase its use among commuters. Moreover, the sensitivity analysis suggests that the model is able to capture correctly variations in the characteristics of investigated travelers.

The modest data set and computational capability required for developing the model seem to be advantageous characteristics of the hybrid model. However, the simplicity of the model might result in losing accuracy. In this context, further investigation should be conducted. Testing other variables in the model could increase model reliability. Moreover, Maximum Likelihood could be used for parameter estimation. Additionally, Multinomial logit model with GA-base parameters could be compared with other simulation techniques in order to verify its accuracy. Finally, the model could be tested for different discrete choice problems.

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References