

OGLE-2017-BLG-0329L: A MICROLENSING BINARY CHARACTERIZED WITH DRAMATICALLY ENHANCED
PRECISION USING DATA FROM SPACE-BASED OBSERVATIONS

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ABSTRACT

Mass measurements of gravitational microlenses require one to determine the microlens parallax π_E , but precise π_E measurement, in many cases, is hampered due to the subtlety of the microlens-parallax signal combined with the difficulty of distinguishing the signal from those induced by other higher-order effects. In this work, we present the analysis of the binary-lens event OGLE-2017-BLG-0329, for which π_E is measured with a dramatically improved precision using additional data from space-based *Spitzer* observations. We find that while the parallax model based on the ground-based data cannot be distinguished from a zero- π_E model at 2σ level, the addition of the *Spitzer* data enables us to identify 2 classes of solutions, each composed of a pair of solutions according to the well-known ecliptic degeneracy. It is found that the space-based data reduce the measurement uncertainties of the north and east components of the microlens-parallax vector π_E by factors ~ 18 and ~ 4 , respectively. With the measured microlens parallax combined with the angular Einstein radius measured from the resolved caustic crossings, we find that the lens is composed of a binary with components masses of either $(M_1, M_2) \sim (1.1, 0.8) M_\odot$ or $\sim (0.4, 0.3) M_\odot$ according to the two solution classes. The first solution is significantly favored but the second cannot be securely ruled out based on the microlensing data alone. However, the degeneracy can be resolved from adaptive optics observations taken ~ 10 years after the event.

Subject headings: gravitational lensing: micro – binaries: general

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1. INTRODUCTION

Microlensing phenomena occur by the gravitational field of lensing objects regardless of their luminosity. Due to this nature, microlensing can, in principle, provide an important tool to determine the mass spectrum of Galactic objects based on samples that are unbiased by luminosity (Han & Gould 1995).

Construction of the mass spectrum requires one to determine the masses of individual lenses. For most microlensing events, the only observable related to the physical parameters of the lens is the Einstein timescale. However, the Einstein timescale is related to not only the lens mass but also the relative lens-source parallax, π_{rel} , and the proper motion, μ_{rel} , by

$$t_E = \frac{\theta_E}{\mu_{\text{rel}}}, \quad \theta_E = (\kappa M \pi_{\text{rel}})^{1/2}, \quad (1)$$

where θ_E is the angular Einstein radius, $\kappa = 4G/(c^2 \text{au}) \sim 8.14 \text{ mas}/M_\odot$, $\pi_{\text{rel}} = \text{au}(D_L^{-1} - D_S^{-1})$, and D_L and D_S denote the distances to the lens and source, respectively. As a result, the lens mass cannot be uniquely determined from the event timescale alone. For the unique determination of the lens mass, one needs to measure two additional quantities: the angular Einstein radius θ_E and the microlens-parallax π_E with which the mass and distance to the lens are determined by (Gould 2000)

$$M = \frac{\theta_E}{\kappa \pi_E}; \quad D_L = \frac{\text{au}}{\pi_E \theta_E + \pi_S} \quad (2)$$

where $\pi_S = \text{au}/D_S$.

The angular Einstein radius can be measured from deviations in lensing lightcurves affected by finite-source effects. Finite-source effects occur when a source star is located in the region within which the gradient of lensing magnification is significant and thus different parts of the source are differentially magnified. For a lensing event produced by a single mass, this corresponds to the very tiny region around the lens, and thus finite-source effects can be effectively detected only for a very small fraction of events for which the lens transits the surface of the source (Witt & Mao 1994; Nemiroff & Wickramasinghe 1994; Gould 1994). For events produced by binary lenses, on the other hand, the chance to

detect finite-source effects is relatively high because the lens systems form extended caustics around which the magnification gradient is high. Analysis of deviations affected by finite-source effects yields the normalized source radius ρ , which is defined as the ratio of the angular source radius θ_* to the angular Einstein radius. By estimating θ_* from external information of the source color, the angular Einstein radius is determined by $\theta_E = \theta_*/\rho$.

The microlens-parallax can be measured from deviations in lensing lightcurves caused by the positional change of an observer. In the single frame of Earth, such deviations occur due to the acceleration of Earth induced by the orbital motion: ‘‘annual microlens parallax’’ (Gould 1992). However, precise π_E measurement from the deviations induced by the annual microlens-parallax effect is difficult because the positional change of an observer during $\sim (O)10$ -day durations of typical lensing events is, in most cases, very minor. As a result, π_E measurements have been confined to a small fraction of all events, preferentially events with long timescales and/or events caused by relatively nearby lenses. For binary-lens events, π_E measurement becomes further complicated because the orbital motion of the binary lens produces deviations in lensing light curves similar to those induced by microlens-parallax effects (Batista et al. 2011; Skowron et al. 2011; Han et al. 2016).

Microlens parallaxes of lensing events can also be measured if events are simultaneously observed using ground-based telescopes and space-based satellite in a heliocentric orbit: ‘‘space-based microlens parallax’’ (Refsdal 1966; Gould 1994). For typical lensing events with physical Einstein radii of order au, the separation between Earth and a satellite can comprise a significant fraction of the Einstein radius. Then, the lensing lightcurves observed from the ground and from the satellite appear to be different due to the difference in the relative lens-source positions, and the comparison of the two lightcurves leads to the determination of π_E .

In this work, we present the analysis of the binary microlensing event OGLE-2017-BLG-0329 that was observed both from the ground and in space using the *Spitzer* telescope. We show that while the parallax model based on the ground-based data cannot be distinguished from a zero- π_E model, the addition of the *Spitzer* data leads to the firm identification of two classes of microlens-parallax solutions

2. OBSERVATIONS AND DATA

The microlensing event OGLE-2017-BLG-0329 occurred on a star located toward the Galactic bulge. The equatorial coordinates of the event are (RA, DEC)_{J2000} = (17:53:43.20, -32:55:27.4), which correspond to the Galactic coordinates (l, b) = ($-2.53^\circ, -3.54^\circ$). The baseline magnitude of the event before lensing magnification was $I_{\text{base}} \sim 15.84$.

Figure 1 shows the light curve of the event. The light curve is characterized by 3 peaks. The first smooth peak occurred at $\text{HJD}' = \text{HJD} - 2450000 \sim 7882$ and the other two sharp peaks occurred at $\text{HJD}' \sim 7900$ and 7927 . The smooth and sharp peaks are typical features that occur when a source approaches the cusp and passes over the fold of a binary-lens caustic, respectively. The event was already in progress before the 2017 microlensing season and lasted for more than 100 days.

The lensing event was observed from the ground by two microlensing surveys of the Optical Gravitational Lensing Experiment (OGLE: Udalski et al. 2015) and the Korea Microlensing Telescope Network (KMTNet: Kim et al. 2016).

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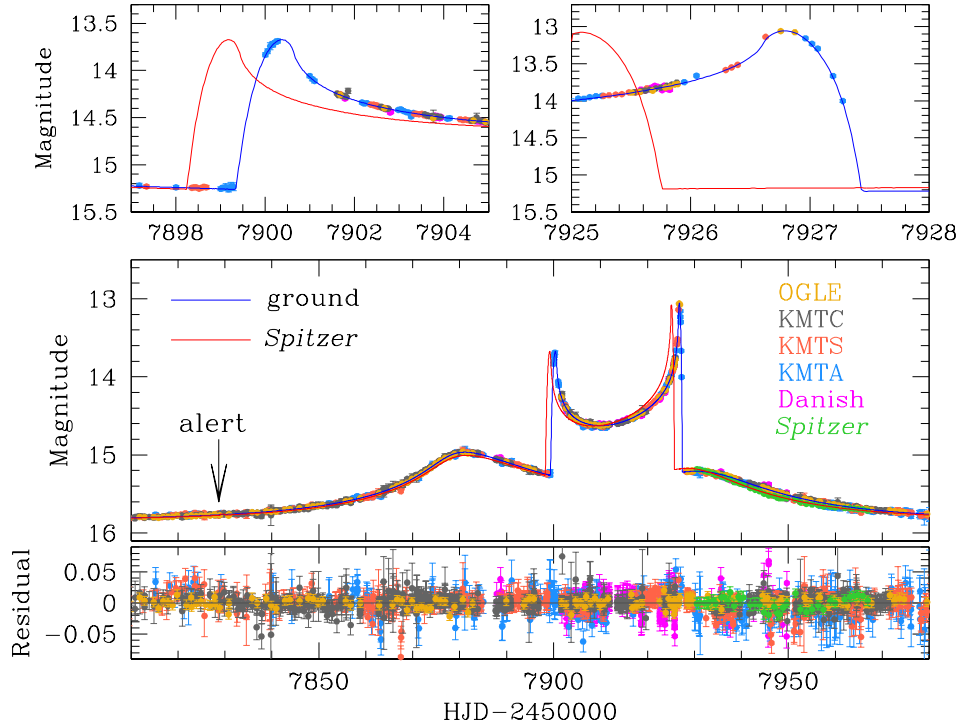


FIG. 1.— Light curve of OGLE-2017-BLG-0329. The blue and red curves superposed on the data points represent the best-fit model light curves for the ground and space-based data, respectively. The arrow designates the time when the event was alerted. The upper panels show the enlarged views of the caustic entrance (left panel) and exit (right panel) parts of the light curve.

OGLE observations of the event were conducted using the 1.3m telescope located at the Las Campanas Observatory in Chile. The OGLE survey first identified the event from its Early Warning System on 2017 March 14 ($\text{HJD}' = 7828.4$). KMTNet observations were carried out using 3 globally distributed 1.6m telescopes located at the Cerro Tololo Inter-American Observatory in Chile (KMTc), the South African Astronomical Observatory in South Africa (KMTs), and the Siding Spring Observatory in Australia (KMTA). The event was identified by KMTNet as BLG22K0103.001613. Observations by both surveys were conducted mainly in I band and some V -band images were obtained for the color measurement of the source star. The event was located in the OGLE BLG502 and KMTNet BLG22 fields, which were observed with cadences of 0.17/hr and 1/hr by the OGLE and KMTNet surveys, respectively. With the high cadence of the surveys, both the caustic entrance and exit were resolved. See the upper panels of Figure 1. Besides the survey experiments, the event was additionally observed from follow-up experiment conducted by the MiNDSTeP Collaboration during the period $7887.9 < \text{HJD}' < 7954.7$ using the 1.5m Danish Telescope at La Silla Observatory in Chile. Photometry of the data were conducted using the pipelines developed by the individual groups based on the difference imaging analysis method (Alard & Lupton 1998). Since the data sets were taken using different instruments and reduced based on different softwares, we normalize the error bars of the individual data sets using the method described in Yee et al. (2012).

The event was also observed in space. At the time that it was originally evaluated for *Spitzer* observations (2017 May 1; $\text{HJD}' = 7874$), it was believed to be a point-lens event, and hence the decision was made in accordance with the protocols of Yee et al. (2015), which are designed to obtain an

unbiased sample of events to probe the Galactic distribution of planets. The *Spitzer* team specified that the event should be observed provided that it reached $I < 15.65$ at $\text{HJD}' = 7924$, i.e., the time of the first upload. Since this requirement was met, these observations were initiated, and were ultimately conducted during the period 7930.5 – 7966.9 (~ 36.4 days), with both dates set essentially by the spacecraft’s Sun-angle restrictions. *Spitzer* images were taken in the $3.6 \mu\text{m}$ channel of the IRAC camera, and the data were reduced with a specially developed version of point response function photometry (Calchi Novati et al. 2015b).

3. ANALYSIS

OGLE-2017-BLG-0329 is of scientific importance because it may be possible to measure the microlens parallax not only from the ground-based data (annual microlens parallax) but also from the combined ground+space data (space-based microlens parallax). For this event, the chance to measure the annual microlens parallax is high due to its long timescale. Since the event was additionally observed by the *Spitzer* telescope, the microlens parallax can also be measured from the combined ground+space data. Therefore, the event provides a test bed in which one can check the consistency of the π_E values and compare the precision of π_E measurements by the individual methods. We note that there exist four cases for which ground-based π_E measurements have been confirmed by space-based data: OGLE-2014-BLG-0124 (Udalski et al. 2015), OGLE-2015-BLG-0196 (Han et al. 2017), OGLE-2016-BLG-0168 (Shin et al. 2017), and MOA-2015-BLG-020 (Wang et al. 2017).

3.1. Ground-based Data

TABLE 1
COMPARISON OF MODELS (GROUND-BASED DATA)

Model	χ^2	
	$u_0 > 0$ solution	$u_0 < 0$ solution
Standard	2392.1	-
Orbit	2338.2	-
Parallax	2356.8	2363.1
Orbit+Parallax	2336.1	2330.8

We first conduct analysis of the event based on the data obtained from ground-based observations. We start modeling the light curve under the approximation that the relative lens-source motion is rectilinear (“standard model”). For this modeling, one needs 7 principal lensing parameters. These parameters include the time of the closest source approach to a reference position of the binary lens, t_0 , the lens-source separation at that time, u_0 (impact parameter), the event timescale, t_E , the projected separation s (normalized to θ_E), and the mass ratio q between the binary-lens components, the angle between the source trajectory and the binary-lens axis, α (source trajectory angle), and the normalized source radius ρ . We choose the barycenter of the binary lens as the reference position of the lens.

Since both the caustic crossings of the light curve were resolved, we consider finite-source effects. Finite-source magnifications are computed using the ray-shooting method (Schneider & Weiss 1986; Kayser et al. 1986; Wambsgans 1997). In computing lensing magnifications, we consider the surface-brightness variation of the source star caused by limb darkening. For this, we model the surface brightness profile of the source star as $S \propto 1 - \Gamma(1 - 3\cos\phi/2)$, where Γ is the linear limb-darkening coefficient and ϕ is the angle between the line of sight toward the center of the source star and the normal to the surface of the source star. Based on the spectral type of the source star (see Section 4.1), we adopt $\Gamma_l = 0.53$.

To find the solution of the lensing parameters, we first conduct a grid search for the parameters $\log s$ and $\log q$, while the other parameters ($t_0, u_0, t_E, \rho, \alpha$) at each point on the $(\log s, \log q)$ plane are searched for by minimizing χ^2 using the Markov Chain Monte Carlo (MCMC) method. This first-round search yields local minima in the $(\log s, \log q)$ plane. For each local minimum, we then refine the solution by allowing all parameters to vary. We identify a global minimum by comparing χ^2 values of the individual local solutions. From this modeling, we find a unique solution of the event. According to this solution, the event was produced by a binary with a mass ratio between the components of $q \sim 0.7$ and a projected separation of $s \sim 1.4$. Due to the similar masses of the binary components and the proximity of the separation to unity, the caustic forms a single big closed curve (resonant caustic).

Since the event can be subject to higher-order effects due to its long timescale, we conduct additional modeling considering two such effects. In the “parallax model” and “lens-orbital model”, we separately consider the microlens-parallax and lens-orbital effects, respectively. We also conduct modeling by simultaneously considering both higher-order effects (“orbit+parallax model”). Consideration of the microlens-parallax effects requires to include 2 additional parameters of $\pi_{E,N}$ and $\pi_{E,E}$, which represent the north and east components of the microlens parallax vector π_E , projected on the sky in the north and east equatorial coordinates, respectively. Under the approximation that the positional change of the lens

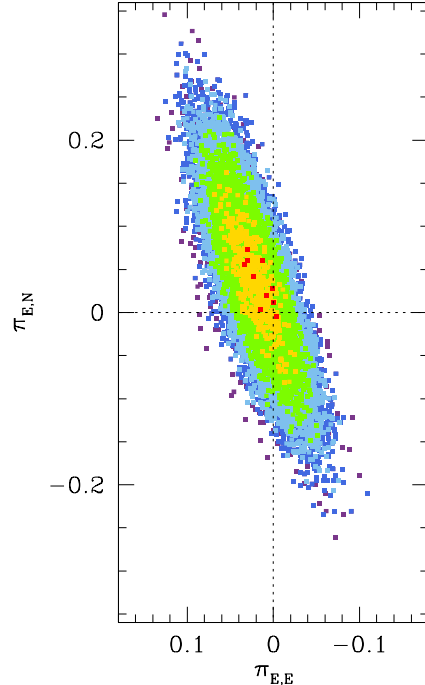


FIG. 2.— Distribution of $\Delta\chi^2$ in the $(\pi_{E,N}, \pi_{E,E})$ plane obtained from the analysis based on the ground-based data. Color coding indicates points in the MCMC chain within 1σ (red), 2σ (yellow), 3σ (green), 4σ (cyan), and 5σ (blue).

is small, the lens-orbital effects are described by two parameters ds/dt and $d\alpha/dt$, which represent the change rates of the binary separation and the source trajectory angle, respectively. For parallax solutions, it is known that there can exist a pair of degenerate solutions with $u_0 > 0$ and $u_0 < 0$ due to the mirror symmetry of the lens system geometry (Smith et al. 2003; Skowron et al. 2011). We check this so-called “ecliptic degeneracy” whenever we consider microlens-parallax effects in modeling. The lensing parameters of the two solutions resulting from the ecliptic degeneracy are approximately in the relations of $(u_0, \alpha, \pi_{E,N}, d\alpha/dt) \leftrightarrow -(u_0, \alpha, \pi_{E,N}, d\alpha/dt)$.

In Table 1, we present the goodness of the fits expressed in terms of χ^2 values for the individual tested models. From the comparison of χ^2 values, it is found that the model fit improves with the consideration of the higher-order effects. The improvement by the microlens-parallax and lens-orbital effects are $\chi^2 = 35.3$ and 53.9 , respectively. When both higher-order effects are simultaneously considered, on the other hand, it is found that the fit improvement is merely $\chi^2 = 7.4$ with respect to the orbital model. From the fact that (1) the fit improvement by the lens-orbital effect is bigger than the improvement by the microlens-parallax effect and (2) the further improvement from the orbital model by additionally considering the microlens-parallax effect is small, we judge that the dominant higher-order effect is the lens-orbital effect and the microlens-parallax effect is relatively small.

The weakness of the microlens-parallax effect can also be seen in Figure 2, where we present the $\Delta\chi^2$ distribution in the $(\pi_{E,N}, \pi_{E,E})$ plane obtained from the modeling considering both microlens-lens and lens-orbital effects. It shows that the model is consistent with the zero- π_E model by $\Delta\chi^2 \lesssim 4$. For the validation of the weak microlens-parallax interpre-

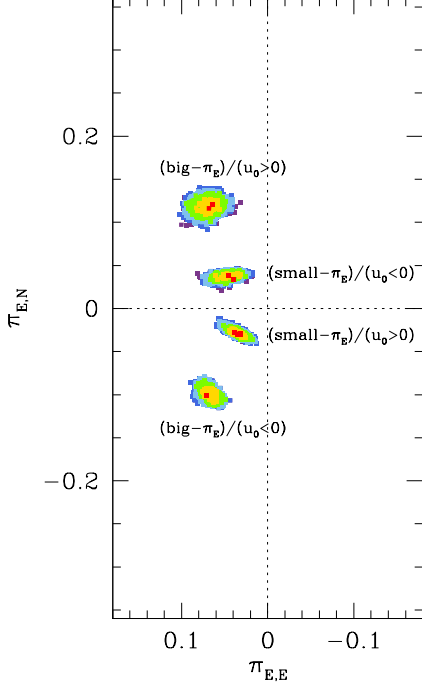


FIG. 3.— Distribution of $\Delta\chi^2$ in the $(\pi_{E,N}, \pi_{E,E})$ plane obtained from the analysis based on the ground+*Spitzer* data. Color coding is same as in Fig. 2. The local minima indicate the positions of the 4 degenerate solutions.

tation, the lens parameters resulting from the orbit+parallax model should be physically permitted. For this, we estimate the ranges of the lens mass ($M = M_1 + M_2$) and the projected kinetic-to-potential energy ratio, which is computed by

$$\left(\frac{\text{KE}}{\text{PE}}\right)_\perp = \frac{(a_\perp/\text{au})^3}{8\pi(M/M_\odot)} \left[\left(\frac{1}{s} \frac{ds}{dt} \text{yr}\right)^2 + \left(\frac{d\alpha}{dt} \text{yr}\right)^2 \right]. \quad (3)$$

We describe the procedure to measure the angular Einstein radius θ_E , which is needed to determine M and $(\text{KE}/\text{PE})_\perp$, in Section 4.1. We find that the ranges of the lens mass and the energy ratio are $0.9 \leq M/M_\odot \leq 4.6$ and $0.04 \leq (\text{KE}/\text{PE})_\perp \leq 0.1$, respectively. The estimated lens mass roughly corresponds to those of binaries composed of stars. The kinetic-to-potential energy ratio also meets the condition $(\text{KE}/\text{PE})_\perp < \text{KE}/\text{PE} < 1$, that is required for the binary lens to be a gravitationally bound system. Therefore, the solution based on the ground-based data is physically permitted, although the range of the estimated lens mass is very wide due to the large uncertainty of the measured π_E .

3.2. Additional Space-based Data

Knowing the difficulty of secure π_E measurement based on only the ground-based data, we test the possibility of π_E measurement with the additional data obtained from *Spitzer* observations. To compute lensing magnifications seen from the *Spitzer* telescope, one needs the position and the distance to the satellite. The position of the *Spitzer* telescope was in the ranges of $110^\circ \lesssim \text{RA} \lesssim 194^\circ$ and $-7^\circ \lesssim \text{DEC} \lesssim 21^\circ$ and the distance was in the range of $1.566 \lesssim d_{\text{sat}}/\text{au} \lesssim 1.584$ during the 2017 bulge season.

The *Spitzer* data partially covered the event light curve. Furthermore, they do not cover major features such as those produced by caustic crossings. See the *Spitzer* data presented

in Figure 1. In such a case, it is known that external information of the color between the passbands used for observations from Earth and from the *Spitzer* telescope can be useful in finding a correct model (Yee et al. 2015; Shin et al. 2017). We, therefore, apply a color constraint with the measured instrumental color of $I-L = 2.33 \pm 0.012$. The color constraint is imposed by giving penalty χ^2 defined in Eq. (2) of Shin et al. (2017).

For single-lensing events observed both from Earth and from a satellite, it is known that there exist four sets of degenerate solutions (Refsdal 1966; Gould 1994). This degeneracy among these solutions, referred to as $(+, +)$, $(-, -)$, $(+, -)$, and $(-, +)$ solutions, arises due to the ambiguity in the signs of the lens-source impact parameters as seen from Earth (the former sign in the parenthesis) and from the satellite (the latter sign in the parenthesis). In many case of binary-lens events, this four-fold degeneracy reduces into a two-fold degeneracy (Han et al. 2017) due to the lack of lensing magnification symmetry. The remaining two degenerate solutions, $(+, +)$ and $(-, -)$ solutions, are caused by the mirror symmetry of the source trajectory with respect to the binary axis, and thus the degeneracy corresponds to the ‘ecliptic degeneracy’. Besides the known types, binary events can be subject to various other types of degeneracy.

In order to check the existence of degenerate solutions, we explore the space of the lensing parameters using two methods. First, we conduct a grid search over the $(\pi_{E,N}, \pi_{E,E})$ plane. Second, we search for local solutions using a downhill approach from various starting points that are obtained from the analysis based on the ground-based data. From these searches, we identify 2 classes of solutions, in which each class is composed of 2 solutions arising from the ecliptic degeneracy.

In Figure 3, we present the locations of the local solutions in the $(\pi_{E,N}, \pi_{E,E})$ plane. It is found that one pair of solutions have $\pi_E = (\pi_{E,N}^2 + \pi_{E,E}^2)^{1/2} \gtrsim 0.1$ (‘big- π_E ’ solutions) and the other pair have $\pi_E \lesssim 0.1$ (‘small- π_E ’ solutions). For each pair, the lensing parameters of the two degenerate solutions are approximately in the relation of $(u_0, \alpha, \pi_{E,N}, d\alpha/dt) \leftrightarrow -(u_0, \alpha, \pi_{E,N}, d\alpha/dt)$, and thus we refer to the solutions as $u_0 < 0$ and $u_0 > 0$ solutions. We note that although the higher-order parameters $(\pi_{E,N}, \pi_{E,E}, ds/dt, d\alpha/dt)$ of these degenerate solutions are different from one another, the other lensing parameters are similar because they are mostly determined from the ground-based data. By comparing the ranges of the $\Delta\chi^2$ distributions with and without the *Spitzer* data, one finds that the uncertainties of the determined microlens-parallax parameters are greatly reduced with the use of the *Spitzer* data.

In Table 2, we list the lensing parameters of the 4 degenerate solutions along with their χ^2 values. We find that the $(\text{small-}\pi_E)/(u_0 < 0)$ solution is preferred over the other solutions for two major reasons. First, the $(\text{small-}\pi_E)/(u_0 < 0)$ solution provides a better fit to the observed data than the other solutions by $11.3 < \Delta\chi^2 < 25.3$. Second, the small- π_E solutions are preferred over the big- π_E solution according to the ‘Rich argument’ (Calchi Novati et al. 2015a), which states that, other factors being equal, small parallax solutions are preferred over large ones by a probability factor $(\pi_{E,\text{big}}/\pi_{E,\text{small}})^2 \gtrsim 6$. Although the $(\text{small-}\pi_E)/(u_0 < 0)$ solution is favored, one cannot completely rule out the other degenerate solutions. We, therefore, discuss the methods that can firmly resolve the degeneracy in Section 5. Also presented in Table 2 are the fluxes of the source, $f_{S,I}$, and the blend, $f_{B,I}$,

TABLE 2
BEST-FIT PARAMETERS (WITH *Spitzer* DATA)

Parameter	Small π_E		Big π_E	
	$u_0 < 0$	$u_0 > 0$	$u_0 < 0$	$u_0 > 0$
χ^2	2373.1 (3.1)	2398.4 (12.7)	2395.1 (5.2)	2384.4 (1.7)
t_0 (HJD')	7904.908 ± 0.098	7904.885 ± 0.106	7904.873 ± 0.057	7905.071 ± 0.057
u_0	-0.151 ± 0.002	0.152 ± 0.002	-0.151 ± 0.001	0.149 ± 0.001
t_E (days)	41.73 ± 0.06	41.73 ± 0.05	41.71 ± 0.04	41.64 ± 0.04
s	1.438 ± 0.002	1.438 ± 0.002	1.440 ± 0.001	1.438 ± 0.001
q	0.704 ± 0.005	0.702 ± 0.006	0.701 ± 0.002	0.712 ± 0.003
α (rad)	-0.642 ± 0.001	0.642 ± 0.001	-0.648 ± 0.001	0.647 ± 0.001
ρ (10^{-3})	8.76 ± 0.07	8.69 ± 0.07	8.68 ± 0.05	8.78 ± 0.06
$\pi_{E,N}$	0.034 ± 0.003	-0.030 ± 0.004	-0.100 ± 0.006	0.121 ± 0.007
$\pi_{E,E}$	0.040 ± 0.009	0.031 ± 0.007	0.070 ± 0.007	0.065 ± 0.009
ds/dt (yr^{-1})	0.215 ± 0.058	0.197 ± 0.059	0.122 ± 0.013	0.175 ± 0.021
$d\alpha/dt$ (yr^{-1})	-0.165 ± 0.031	0.158 ± 0.030	-0.168 ± 0.020	0.009 ± 0.019
$f_{S,I}$	7.35	7.36	7.37	7.35
$f_{b,I}$	-0.06	-0.07	-0.08	-0.06

NOTE. — The values in the parenthesis of the χ^2 line represent the penalty χ^2 values given by the color constraint. See more details in section 3.2. HJD' = HJD - 2450000.

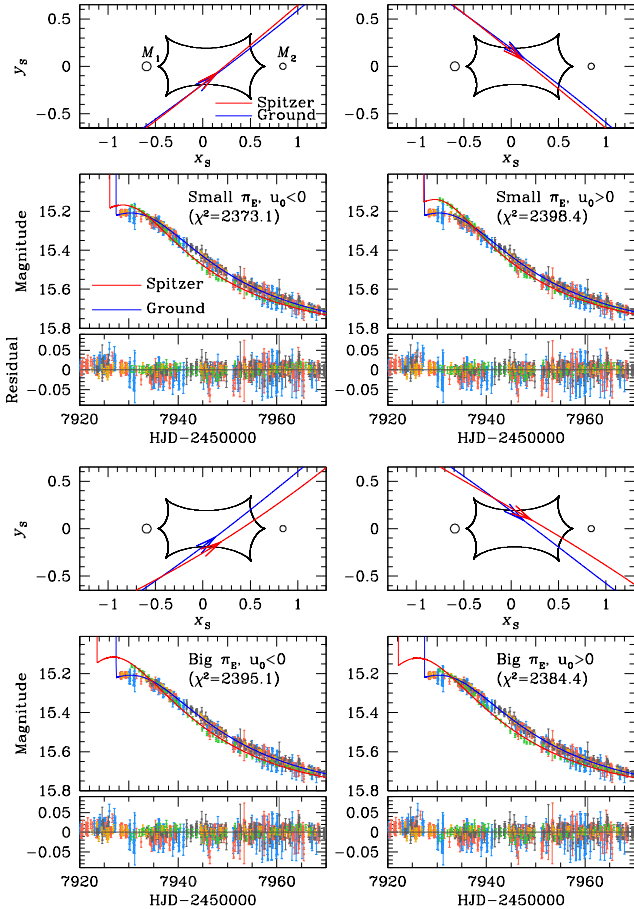


FIG. 4.— The lens system geometry and the portion of the light curve in the vicinity of the *Spitzer* data for the 4 degenerate solutions. For each lens system geometry, the source trajectories seen from Earth and the *Spitzer* telescope are marked by blue and red curves (with arrows). The cuspy closed curve represents the caustic. The coordinates are centered at the barycenter of the binary lens. The blue and red curves superposed on the data points represent the model light curves for the ground and *Spitzer* data, respectively.

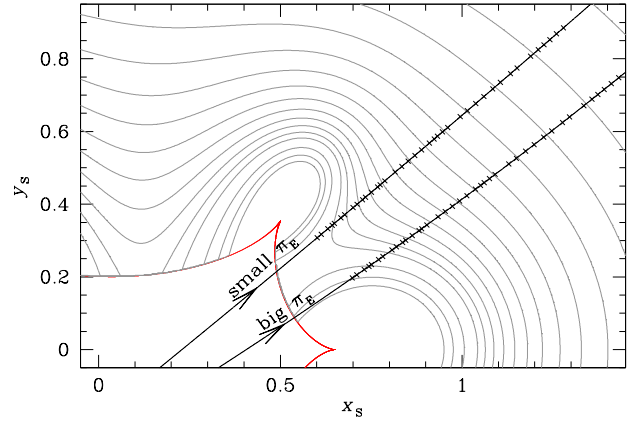


FIG. 5.— Contour map of lensing magnification in the outer region of the caustic. Contours are drawn at every $\Delta A = 0.05$ step from $A = 1.1$ to $A = 2.0$. The lines with arrows represent the source trajectories of the small- π_E and big- π_E solutions from the *Spitzer* telescope. The crosses on each trajectory represent the expected positions of the source when *Spitzer* data were taken.

estimated based on the OGLE data. The small $f_{b,I}$ indicates that the blend flux is small. We note that the small negative blending is quite common for point-spread-function photometry in crowded fields (Park et al. 2004).

In Figure 4, we present the lens-system geometry of the 4 degenerate solutions. For each geometry, we present the source trajectories with respect to the lens components (small empty dots marked by M_1 and M_2) and the caustic (cuspy closed curve). For each geometry, the source trajectories seen from Earth and the *Spitzer* telescope are marked by blue and red curves (with arrows), respectively. We also present the portion of the light curve in the vicinity of the *Spitzer* data and the model light curve.

As mentioned, the degeneracy between the $u_0 < 0$ and $u_0 > 0$ solutions is caused by the mirror symmetry of the lens system geometry. On the other hand, the degeneracy between the small- π_E and big- π_E solutions is caused by the difference in the source trajectory angles seen from the *Spitzer* telescope. For the small- π_E solution, the source trajectory angle as seen from the *Spitzer* telescope is bigger than the angle of the source trajectory seen from the ground. In contrast, the

Spitzer trajectory angle of the big- π_E solution is smaller than the angle of the ground trajectory. We note that the latter degeneracy is different from the degeneracy between (+, +) and (+, -) solutions because both ground and satellite trajectories pass on the same side with respect to the barycenter of the binary lens. Such a degeneracy is not previously known.

In order to further investigate the cause of the degeneracy between the small- π_E and big- π_E solutions, in Figure 5, we present the magnification contours in the outer region of the caustic. On the contour map, we plot the *Spitzer* source trajectories of the two degenerate solutions. From the map, it is found that the magnification patterns along the source trajectories of the two degenerate solutions are similar to each other, suggesting that the degeneracy is caused by the symmetry of magnification pattern in the outer region of the caustic. We note that the degeneracy could have been resolved if the caustic exit part of the light curve had been covered by *Spitzer* data because the times of the caustic exit (seen from the *Spitzer* telescope) expected from the two degenerate solutions are different from each other. We find that the caustic-exit times for the small- π_E solutions are in the range of 7926 (for $u_0 < 0$) \lesssim HJD' \lesssim 7928 (for $u_0 > 0$). On the other hand, the range for the big- π_E solutions is 7922 (for $u_0 < 0$) \lesssim HJD' \lesssim 7924 (for $u_0 > 0$). With the ~ 4 day time gap between the caustic-crossing times of the small- π_E and big- π_E solutions, the degeneracy could have been easily lifted. In conclusion, we find that the new type of degeneracy is caused by the partial symmetry of the magnification pattern outside the caustic combined with the fragmentary coverage of the *Spitzer* data.

From the comparison of the analyses conducted with and without the space-based data, we find two important results.

1. First, while the microlens parallax cannot be securely determined based on only the ground-based data, the addition of the *Spitzer* data enables us to clearly identify two classes of microlens-parallax solutions. The degeneracy is either intrinsic to lensing systems ($u_0 < 0$ versus $u_0 > 0$ degeneracy) or due to the combination of the partial symmetry of magnification pattern combined with the fragmentary *Spitzer* coverage of the event (small- π_E versus big- π_E degeneracy).
2. Second, the space-based data greatly improve the precision of the π_E measurement. We find that the measurement uncertainties of the north and east components of π_E are reduced by factors ~ 18 and ~ 4 , respectively, with the use of the *Spitzer* data. Since the lens mass is directly proportional to $1/\pi_E$, the uncertainty of the mass measurement reduces by the same factors.

4. PHYSICAL LENS PARAMETERS

4.1. Source Star and Angular Einstein Radius

For the unique determination of the lens mass and distance, one needs to estimate the angular Einstein radius in addition to the microlens parallax. Since the angular Einstein radius is determined by $\theta_E = \theta_*/\rho$, it is required to estimate the angular radius of the source star.

We estimate θ_* from the dereddened color $(V-I)_0$ and brightness I_0 of the source. In order to derive $(V-I)_0$ from the instrumental color-magnitude diagram, we use the method of Yoo et al. (2004), which uses the centroid of red giant clump (RGC) as a reference. In Figure 6, we present the loca-

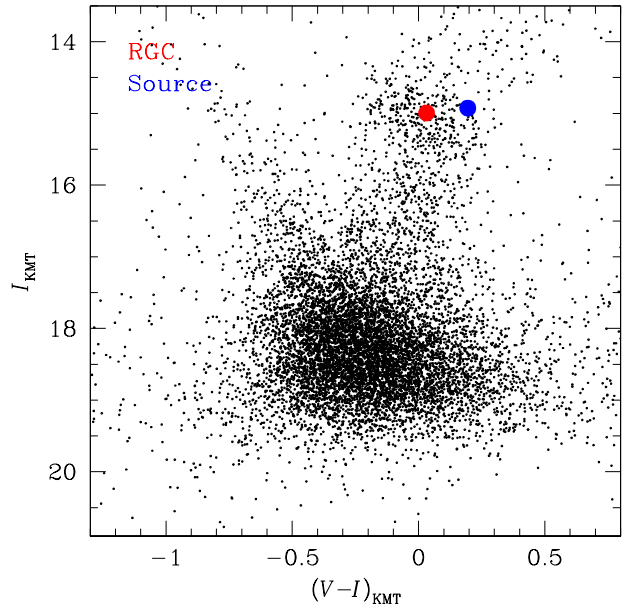


FIG. 6.— Location of the source with respect to the centroid of red giant clump (RGC) in the instrumental color-magnitude diagram.

tion of the source and the RGC centroid in the instrumental color-magnitude diagram constructed from the I - and V -band DoPHOT photometry of the KMTC data set. It is found that the offsets in color and brightness of the source with respect to the RGC centroid are $\Delta(V-I, I) = (0.16, -0.07)$. With the known dereddened color and magnitude of RGC centroid, $(V-I, I)_{\text{RGC}} = (1.06, 14.5)$ (Bensby et al. 2011; Nataf et al. 2013), we find that the dereddened color and brightness of the source star are $(V-I, I)_0 = (V-I, I)_{\text{RGC}} + \Delta(V-I, I) = (1.22 \pm 0.07, 14.48 \pm 0.09)$. This indicates that the source is a K-type giant star. Using the color-color relation provided by Bessell & Brett (1988), we convert $V-I$ into $V-K$. Using the relation between $V-K$ and the surface brightness (Kervella et al. 2004), we estimate the angular source radius. The estimated angular source radius is $\theta_* = 6.9 \pm 0.6 \mu\text{as}$. Combined with value of ρ , we estimate that the angular Einstein radius of the lens system is

$$\theta_E = 0.79 \pm 0.06 \text{ mas.} \quad (4)$$

With the measured angular Einstein radius, the relative lens-source proper motion is estimated by

$$\mu = 6.89 \pm 0.56 \text{ mas yr}^{-1}. \quad (5)$$

4.2. Lens Parameters

With the measured microlens parallax and the angular Einstein radius, we estimate the mass and distance to the lens using the relations in Equation (2). In Table 3, we list the determined physical parameters, including masses of the primary, M_1 , and the companion, M_2 , the distance to the lens, D_L , and the projected separation between the lens components, $a_\perp = sD_L\theta_E$, for the individual degenerate lensing solutions. To check the physical validity of the parameters, we also present the ratio between the projected potential energy to the kinetic energy, i.e., $(\text{KE}/\text{PE})_\perp$.

Due to the difference in the microlens-parallax values between the small- π_E and big- π_E solution classes, the estimated lens masses and distances for the two classes of solutions are

TABLE 3
PHYSICAL LENS PARAMETERS

Parameter	Small π_E		Big π_E	
	$u_0 < 0$	$u_0 > 0$	$u_0 < 0$	$u_0 > 0$
$M_1 (M_\odot)$	1.09 ± 0.15	1.33 ± 0.21	0.47 ± 0.04	0.41 ± 0.04
$M_2 (M_\odot)$	0.77 ± 0.11	0.93 ± 0.15	0.33 ± 0.03	0.29 ± 0.03
D_L (kpc)	6.38 ± 0.79	6.66 ± 0.86	4.69 ± 0.45	4.48 ± 0.42
a_\perp (au)	7.20 ± 0.89	7.59 ± 0.98	5.35 ± 0.52	5.04 ± 0.47
$(KE/PE)_\perp$	0.12 ± 0.02	0.12 ± 0.02	0.09 ± 0.01	0.04 ± 0.01
ψ (deg)	51	132	141	32

TABLE 4
EXPECTED LENS BRIGHTNESS

Solution	u_0	Lens		Source	
		I_L	H_L	I_S	H_S
Small π_E	$u_0 < 0$	18.8	17.0	15.8	13.5
	$u_0 > 0$	17.7	16.5	-	-
Big π_E	$u_0 < 0$	21.5	18.7	-	-
	$u_0 > 0$	22.1	19.1	-	-

substantially different from each other. On the other hand, the physical parameters for the pair of the $u_0 > 0$ and $u_0 < 0$ solutions are similar to each other. We find that the masses of the primary and companion are $1.1 \lesssim M_1/M_\odot \lesssim 1.3$ and $0.8 \lesssim M_2/M_\odot \lesssim 0.9$ for the small- π_E solutions. For the big- π_E solutions, the masses of the lens components are $0.4 \lesssim M_1/M_\odot \lesssim 0.5$ and $M_2 \sim 0.3 M_\odot$. The estimated distances to the lens are $7.2 \lesssim D_L/\text{kpc} \lesssim 7.6$ and $5.0 \lesssim D_L/\text{kpc} \lesssim 5.4$ according to the small- π_E and big- π_E solutions, respectively.

5. RESOLVING DEGENERACY

5.1. Lens Brightness

The estimated masses of the lens for the small- π_E and big- π_E solutions are considerably different due to the difference in the measured microlens-parallax values. Then, if the lens-source can be resolved from future high-resolution imaging observations, the degeneracy can be resolved from the lens brightness.

If the proposed follow-up high-resolution observations are conducted, the observations will likely be conducted in the near-IR band. We, therefore, estimate the H -band magnitudes of the source and lens. From the dereddened I -band magnitude $I_0 \sim 14.5$, the dereddened H -band source magnitude of the source is $H_0 \sim 13.1$ (Bessell & Brett 1988). The V -band extinction of $A_V \sim 2.6$ in combination with the extinction ratio (A_H/A_V) ~ 0.108 (Nishiyama et al. 2008) toward the bulge field yields the H -band extinction of $A_H \sim 0.28$. Then, the apparent H -band magnitude of the source is $H_S = H_0 + A_H \sim 13.4$. We compute the lens brightness based on the mass and distance under the assumption that the lens and source experience the same amount of extinction. In Table 4, we present the expected combined (primary plus companion) I - and H -band magnitudes of the lens and source. The brightness of the lens varies depending on the solution. For the small- π_E solutions, the apparent H -band magnitude of the lens is $H_L \sim 16.5 - 17.0$. For the big- π_E solutions, on the other hand, the expected H -band lens brightness is $H_L \sim 18.7 - 19.1$.

According to the estimated I -band lens brightness, the lens-to-source flux ratio for the (small- π_E)/($u_0 > 0$) solution is $f_{L,I}/f_{S,I} \sim 17\%$. Since the light from the lens contributes to blended light, then, this ratio is too big to be consistent with the small amount of the measured blended flux, even considering the uncertainties of the lens mass and distance. There-

fore, the solution is unlikely to be the correct solution not only because of its worst χ^2 value among the degenerate solutions but also because of the limits on blended light. The lens-to-source flux ratio for the (small- π_E)/($u_0 < 0$) is about 6%, but with the lens mass and distance at the 1σ (2σ) level, the ratio is $\sim 2\%$ (1%), which is consistent with the blending.

5.2. Relative Lens-source Proper Motion

The degeneracy between $u_0 < 0$ and $u_0 > 0$ solutions can also be lifted once the lens and source are resolved. The relative lens-source proper motion vector is related to t_E , θ_E , and $(\pi_{E,N}, \pi_{E,E})$ by

$$\boldsymbol{\mu} = (\mu_N, \mu_E) = \left(\frac{\theta_E \pi_{E,N}}{t_E \pi_E}, \frac{\theta_E \pi_{E,E}}{t_E \pi_E} \right). \quad (6)$$

For the pair of the degenerate solutions with $u_0 < 0$ and $u_0 > 0$, the north components of $\boldsymbol{\pi}_E$ have opposite signs. This implies that the relative motion vectors of the two degenerate solutions are directed in substantially different directions and thus the degeneracy can be resolved from the lens motion with respect to the source.

The heliocentric lens-source proper motion is $\boldsymbol{\mu}_{\text{helio}} \sim 7 \text{ mas yr}^{-1}$, which is about what is expected for a disk lens. In this case, the expected direction of $\boldsymbol{\mu}_{\text{helio}}$ (i.e., the direction of Galactic rotation $\psi \sim 30^\circ$) is roughly 30° East of North. In Table 3, we list the orientation angles ψ of $\boldsymbol{\mu}_{\text{helio}}$, as measured from North to East, corresponding to the individual solutions. The heliocentric proper motion is related to the geocentric proper motion $\boldsymbol{\mu}_{\text{geo}}$ by

$$\boldsymbol{\mu}_{\text{helio}} = \boldsymbol{\mu}_{\text{geo}} + \mathbf{v}_{\oplus, \perp} \frac{\pi_{\text{rel}}}{\text{au}}, \quad (7)$$

where $\mathbf{v}_{\oplus, \perp}$ represents the projected Earth motion at t_0 . One finds that the expected direction $\boldsymbol{\mu}_{\text{helio}}$ is consistent with the (small- π_E)/($u_0 < 0$) and the (big- π_E)/($u_0 > 0$) solutions but inconsistent with the others.

From Keck adaptive optics observations, Batista et al. (2015) resolved the lens from the source ~ 8.2 years after the event OGLE-2005-BLG-169, for which the relative lens-source proper motion is $\mu \sim 7.4 \text{ mas yr}^{-1}$. The estimated proper motion of OGLE-2017-BLG-0329 ($\mu \sim 6.9 \text{ mas yr}^{-1}$) is similar to that of OGLE-2005-BLG-169. Considering the large lens/source flux ratio, the lens-source resolution by Keck observations will take ~ 10 years, which is somewhat longer than the time for OGLE-2005-BLG-169. We note that GMT/TMT/ELT, which will have better resolution than Keck, may be available before Keck can resolve the event and thus the time for follow-up observations can be shortened.

6. CONCLUSION

We presented the analysis of the binary microlensing event OGLE-2017-BLG-0329, which was observed both from the

ground and in space using the *Spitzer* telescope. We found that the parallax model based on the ground-based data could not be distinguished from a zero- π_E model at 2σ level. However, with the use of the additional *Spitzer* data, we could identify 2 classes of microlens-parallax solutions, each composed of a pair of solutions according to the well-known ecliptic degeneracy. We also found that the space-based data helped to greatly reduce the measurement uncertainties of the microlens-parallax vector π_E . With the measured microlens parallax combined with the angular Einstein radius measured from the resolved caustics, we found that the lens was composed of a binary with components masses of either $(M_1, M_2) \sim (1.1, 0.8) M_\odot$ or $\sim (0.4, 0.3) M_\odot$ according to the two solution classes. The degeneracy among the solution would be resolved from adaptive optics observations taken ~ 10 years after the event.

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