TCP BEHAVIOR IN QUALITY OF SERVICE NETWORKS

by

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A thesis submitted in conformity with the requirements for the degree of Doctor of Philosophy Department of Electrical and Computer Engineering University of Canterbury

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Abstract

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Best effort networks fail to deliver the level of service emerging Internet applications demand. As a result many networks are being transformed to Quality of Service (QoS) networks, of which most are Differentiated Services (DiffServ) networks. While the deployment of such networks has been feasible, it is extremely difficult to overhaul the transport layer protocols such as Transmission Control Protocol (TCP) running on hundreds of millions of end nodes around the world. TCP, which has been designed to run on a best effort network, perform poorly in a DiffServ network. It fails to deliver the performance guarantees expected of DiffServ. In this thesis we investigate two aspects of TCP performance in a DiffServ network unaccounted for in previous studies. We develop a deterministic model of TCP that intrinsically captures flow aggregation, a key component of DiffServ. The other important aspect of TCP considered in this thesis is its' transient behavior. Using our deterministic model we derive a classical control system model of TCP applicable in a DiffServ network.

Performance issues of TCP can potentially inhibit the adoption of DiffServ. A DiffServ network commonly use token buckets, that are placed at the edge of the network, to mark packets according to their conformance to Service Level Agreements (SLA). We propose two token bucket variants designed to mitigate TCP issues present in a DiffServ network. Our first proposal incorporates a packet queue alongside the token bucket. The other proposal introduces a feedback controller around the token bucket. We validate both analytically and experimentally the performance of the proposed token buckets. By confining our changes to the token bucket we avoid any changes at end-nodes. The proposed token buckets can also be incrementally deployed.

Most part of the Internet still remains as a best effort network. However, most nodes run various QoS functions locally. We look at one such important QoS function, i.e. the ability to survive against flows that are non-responsive to congestion, the equivalent of a Denial of Service (DoS) attack. We analyze existing techniques and propose improvements.

Dedication

For my family, who offered me unconditional love and support throughout the course of this thesis. I would like to dedicate this thesis in the loving memory of my father.

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Chapter 1

Introduction

1.1 Motivation

The migration of a raft of diverse applications in recent years has transformed the Internet to a convergent network carrying triple play services of voice, video and data. In large measure, this has been realised due to the deployment of Quality of Service (QoS) architectures such as Integrated Services (IntServ) [21], Differentiated Services (DiffServ) [19] and more recently Multi Protocol Label Switching (MPLS) [84]. Users, who increasingly rely on the Internet for communication needs, seek guaranteed service levels. Service providers, on the other hand, increase profitability with an assortment of higher margin differentiated services. As a result, the last few years have seen a widespread deployment of QoS networks. Given the decentralised nature of the Internet protocols and the lack of signaling within the network, no single node can exert absolute control over the entire communication path. For example, nodes in the network core, routers and switches, have only loose control over the rate of packet transmission of end devices. Therefore, guaranteeing specific levels of service for Internet applications has become a challenging task.

The Internet carries traffic belonging to many different applications that have diverse

requirements. There has been a proliferation of fixed bandwidth and delay sensitive realtime applications that deploy aggressive transport layer protocols; e.g. Voice over IP (VoIP), Video on Demand (VoD), Internet Protocol Television (IPTV). They clutter the bandwidth space and can potentially deprive mission-critical business applications of the necessary bandwidth to maintain application performance. Increasingly these applications rely on services that provide minimum guaranteed bandwidths. However, providing per-flow service guarantees is not scalable in a large network like the Internet. Aggregation of flows at the network edge and processing the aggregates in the network core as done in DiffServ has, however, gained popularity. DiffServ has defined the Assured Forwarding (AF) Per-Hop-Behavior (PHB) [43] for applications that require guaranteed minimum bandwidths. Though a certain bandwidth is guaranteed, in most cases applications are allowed access to the full network bandwidth to make efficient use of the available network bandwidth. In either case, limiting the bandwidth at the guaranteed minimum bandwidth level or allowing expansion up to the available network capacity, routers use network congestion events such as dropping packets or marking the Explicit Congestion Notification (ECN) [81], [39] bit to regulate the rate of packets transmission at the edge of the network. Congestion reactive protocols at the transport layer such as Transmission Control Protocol (TCP) help end nodes regulate the rate because of these congestion events in the network core. Due to the lack of precise feedback available on the level of congestion, as in the Internet, end nodes take drastic preventive action in response to congestion events. TCP infers incipient congestion through ECN, duplicate acknowledgments or timeouts and in turn varies the congestion window, which is the allowed number of unacknowledged packets in transit across the network. Most implementations of TCP increase the congestion window by one per round trip time in the absence of any congestion notifications but otherwise attempt to ease congestion by

capable routers at the edge of the network embed code points in the packets to indicate

halving the congestion window. To achieve guaranteed minimum bandwidths, DiffServ

compliance to SLAs. Routers in the network core handle packets according to this code point. Packets that are in-profile are less likely to be dropped or marked compared to out-of-profile packets. Despite the use of a marking scheme, due to the complex way TCP reacts to congestion, TCP flow aggregates often fall short of guaranteed bandwidths in realistic network scenarios.

This weakness of TCP has been an impediment for the successful deployment of DiffServ. This has motivated several studies that have explored ways to overcome this limitation. However, proposed algorithms, as our analysis shows, either distort Diff-Serv functionality or impose major changes across the Internet including end nodes. This dissertation presents two new packet markers that eliminate these limitations while effectively enabling TCP flow aggregates to reach contract rates. Their performance is validated both theoretically and experimentally. The DiffServ induced code point change in the IP header effectively alters TCP dynamics. Many studies have characterized, to varying degrees, the steady state throughput of a Diffserv controlled TCP aggregate. Studying the transient behavior, which hasn't so far been dealt with in any previous work, is equally important. For example, the ability to represent dynamics in a control system model allows analysis-based guidelines for choosing optimal parameters of DiffServ elements, such as packet markers. We develop from first principles a model of a DiffServ controlled TCP flow aggregate in an over-provisioned network, providing insights to both the transient and steady state behavior. We represent this in a control system model and as a practical application use it to derive optimal parameter values of one of the proposed markers.

Though QoS networks such as DiffServ networks are fast gaining popularity, most of the Internet still provides a best effort service. It is vital that nodes of a best effort network run QoS functions. One such important QoS function is survival in the presence of congestion non-responsive flows. Buffer acceptance techniques are designed to perform that functionality. This dissertation proposes a new buffer acceptance algorithm

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that also behaves as a penalty box, which promotes conformance to a bandwidth used by a TCP flow. Buffer acceptance algorithms look more attractive as they bear less overhead compared to packet scheduling algorithms. Previously proposed algorithms rely on various statistical measurements such as buffer occupancy and packet drop history to identify misbehaving flows. We investigate their effectiveness. Our analysis shows that buffer occupancy or packet drop history can distort the bandwidth share estimation of a flow. This motivates our alternative approach.

The summary of the main contributions of this thesis can be stated as:

- Develop a model of TCP that intrinsically captures DiffServ flow aggregation. This allows us to accurately measure the effect that the number of flows per aggregate imparts on TCP throughput.
- Analyze convergence properties of the aggregate TCP congestion window size in wide-ranging conditions. This provides insights to TCP congestion window's oscillatory behavior.
- Study both the transient and steady state TCP behavior. We represent DiffServ controlled TCP dynamics in a classical control system model. It allows use of standard techniques to analyze various mechanisms and propose improvements to algorithms as well as analysis-backed guidelines for choosing parameters of the algorithms.
- Derive more complete expressions for excess bandwidth distribution in terms of number of flows per aggregate, RTT, contract rate, and token bucket size.
- Investigate the benefits of using a packet queue at the token bucket to improve TCP performance in a DiffServ network. We show that the required size of the token bucket grows exponentially with the contract rate, whereas a packet queue needs to be only linearly proportional to the contract rate to prevent TCP flow aggregates falling short of contract rates.

- Propose improvements to a proposed feedback controller around the token bucket. We show that its performance can be drastically improved by comparing the rate of only in-profile packet transmissions to the contract rate as opposed to using the total rate of packet transmissions. This modification also simplifies network dynamics. It allows us to develop a network model in which standard techniques are applied for choosing optimal Proportional Integral (PI) controller parameters of the feedback controller.
- Identify limitations in current algorithms designed to protect TCP flows from congestion non-responsive flows. We show that the use of buffer occupancy as a means of detecting misbehaving flows as done in previously proposed techniques can limit TCP throughput. We also show that the use of packet drop history does not form an accurate measure of bandwidth share when packets are of different sizes.
- Propose an algorithm that accurately estimates bandwidth share of flows and incorporates mechanisms that encourage conformance to the throughput of an idealized TCP flow.

1.2 Thesis Outline

The structure of the thesis is as follows:

Chapter 2 presents background material. We review the Internet, QoS architectures, and TCP.

Chapter 3 introduces our deterministic model of TCP [10] applicable in a DiffServ network. We study both the steady state and transient TCP behavior. The chapter concludes with simulation studies that validate the developed model.

Chapter 4 presents our proposed mechanisms that are designed to mitigate TCP issues faced with in a DiffServ network. The first mechanism, TBQ [6, 7], introduces a packet queue along-side the token bucket. The second mechanism, CARM [9], is an

enhanced version of a proposed feedback controller around the token bucket. We also present an analytical design of the feedback controller [11]. The Chapter includes results of simulation studies that evaluate the proposed mechanisms.

A simple technique, PQM [8], that can potentially protect TCP flows from congestion non-responsive flows is presented in Chapter 5.

Finally Chapter 6 presents the overall conclusions.

1.3 Publication List

Our research outcomes appear in the following publications.

- S. Athuraliya and H. Sirisena. An enhanced token bucket marker for DiffServ networks. International Journal of Wireless and Optical Communications, 2(1):99– 114, June 2004.
- S. Athuraliya and H. Sirisena. An enhanced token bucket marker for Diffserv networks. In *Proc. of IEEE ICON*, volume 2, pages 559–565, Singapore, November 2004.
- S. Athuraliya and H. Sirisena. PQM: Protective queue mangement of TCP flows. In *Proc. of IEEE HSNMC*, pages 213–223, Toulouse, France, 2004. Springer LNCS 3079.
- S. Athuraliya and H. Sirisena. Active rate management in DiffServ. *IEEE Com*munications Letters, 10(6):501–503, June 2006.
- S. Athuraliya and H. Sirisena. Excess bandwidth distribution in DiffServ networks. In *Proc. of IEEE IPCCC*, pages 119–126, Phoenix, USA, April 2006.
- S. Athuraliya and H. Sirisena. Controller design for TCP rate management in QoS networks. In Proc. of IEEE BROADNETS, Raleigh, USA, September 2007.

Chapter 2

Background

2.1 Internet - Historical Perspective

The current Internet has its roots in the Advanced Research Projects Agency Network (ARPANET), an experimental data network funded by the United States Defence Advanced Research Projects Agency (DARPA) in the early 1960s. An important goal was to build a robust network that could endure large-scale catastrophes. Therefore ARPANET's main strengths were robustness and survivability, including the capability to withstand losses of large portions of the underlying network. To achieve this, the ARPANET was built on the datagram model, where each individual packet is forwarded independently to its destination. Three schools of thought exist with regard to the origin of the datagram concept. The researchers, Leonard Kleinrock at Massachusetts Institute of Technology (MIT) (1961-1967), Donald Davies and Roger Scantlebury at National Physical Laboratory (NPL) (1964-1967) and Paul Baran at RAND (1962-1965) had all proposed the datagram concept in parallel without any of the researchers knowing about the other's work. However, Leonard Kleinrock's work was the most influential on the subsequent development of ARPANET.

At its inception ARPANET used an early version of the Network Control Proto-

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col (NCP) [28], which is a host-to-host communication protocol. Later TCP [76] was introduced for cross-network connections. Fragmentation and reassembly of messages, formerly done by node computers on the network, became the responsibility of host computers. TCP was faster, easier to use, and less expensive to implement than NCP. In 1978 IP [75] was added to TCP to take over the routing functionality. The TCP/IP protocol suite became ARPANET's networking protocol of choice and gradually replaced NCP. ARPAnet and its growing number of affiliated networks became known as the Internet.

For many years, the Internet was primarily used by scientists for networking research and for exchanging information between each other. Remote access [79, 52], file transfer [80], and e-mail [78, 77] were among the most popular applications. The World Wide Web (WWW), however, has fundamentally changed the Internet landscape. It is now the world's largest public network. New applications, such as video conferencing, Web searching, electronic media, discussion boards, and Internet telephony are being developed at an unprecedented speed. E-commerce is revolutionizing the way we do business. Advances in Virtual Private Network (VPN) technologies have enabled on-demand secure connectivity anywhere anytime.

The datagram model inherently provides only a best effort packet delivery service and that has been adequate for traditional Internet applications such as remote access, file transfer and email. However, a majority of emerging applications demand stringent guarantees on bandwidth, packet loss, latency and jitter that a best effort packet delivery service cannot deliver. This has motivated the development of mechanisms capable of providing service guarantees in a network such as the Internet built on the datagram model. IntServ [21] and DiffServ [19] represent two major initiatives of the Internet Engineering Task Force (IETF) in this regard.

2.2 Quality of Service Architectures

2.2.1 Intserv

The IntServ model was the first major initiative. It proposed two service classes to augment best effort Service. They are:

- 1. Guaranteed Service (GS) [86] for applications requiring a fixed delay bound,
- Controlled Load Service (CLS) [99] for applications requiring reliable and enhanced best effort service.

The philosophy of this model is that "there is an inescapable requirement for routers to be able to reserve resources in order to provide special QoS for specific user packet streams, or flows. This in turn requires flow-specific state in the routers" [21]. RSVP [20] was invented as a signaling protocol for applications to reserve resources.

The sender sends a PATH Message to the receiver specifying the characteristics of the traffic. Every intermediate router along the path forwards the PATH Message to the next hop determined by the routing protocol. Upon receiving a PATH Message, the receiver responds with a RESV Message to request resources for the flow. Every intermediate router along the path can reject or accept the request of the RESV Message. If the request is rejected, the router will send an error message to the receiver, and the signaling process will terminate. If the request is accepted, link bandwidth and buffer space are allocated for the flow and the related flow state information will be installed in the router. IntServ is implemented by four components: the signaling protocol (e.g. RSVP), the admission control routine, the classifier and the packet scheduler. Applications requiring GS or CLS must set up the paths and reserve resources before transmitting their data. The admission control routines will decide whether a request for resources can be granted. When a router receives a packet, the classifier will perform a Multi-Field (MF) classification and put the packet in a specific queue based on the classification result. The packet scheduler will

then schedule the packet accordingly to meet its QoS requirements. The IntServ/RSVP architecture is influenced by the work of Ferrari et al. [34]. It represents a fundamental change to the current Internet architecture, which is founded on the concept that all flow related state information should be in the end systems [26]. The problems with IntServ are:

- The amount of state information increases proportionally with the number of flows. This places a huge storage and processing overhead on the routers. Therefore, this architecture does not scale well in the Internet core.
- 2. The requirement on routers is high. All routers must implement RSVP, admission control, MF classification and packet scheduling.
- 3. Ubiquitous deployment is required for Guaranteed Service. Incremental deployment of CLS is possible by deploying CLS and RSVP functionality at the bottleneck nodes of a domain and tunneling the RSVP messages over other part of the domain.
- 4. Resource reservation requires the support of accounting and settlement between different service providers. Since those who request reservation have to pay for such services, any reservations must be authorized, authenticated, and accounted. Such supporting infrastructures simply do not exist in the Internet.
- Every device along the path of a packet, including the end systems such as servers and PCs, need to be fully aware of RSVP and capable of signaling the required QoS.
- 6. Reservations in each device along the path are "soft", which means they need to be refreshed periodically, thereby adding to the traffic on the network and increasing the chance that the reservation may time out if refresh packets are lost.
- 7. Maintaining soft-states in each router, combined with admission control at each

hop and increased memory requirements to support a large number of reservations, adds to the complexity of each network node along the path.

The IntServ architecture, developed prior to the emergence of the World Wide Web, focused primarily on long-lasting and delay-sensitive applications. Today web-based applications dominate the Internet, and much of the Web traffic comprises short-lived transactions. Although per-flow reservation makes sense for long-lasting sessions, such as video conferencing, it is not appropriate for Web traffic. The overheads for setting up a reservation for each session are simply too high and, as a result, IntServ never gained wide acceptance. However, the ideas, concepts, and mechanisms developed in IntServ found their ways into later work on QoS. For example, CLS has influenced the development of DiffServ, and a similar resource reservation capability has been incorporated into MPLS for bandwidth guarantees over traffic trunks in the backbones.

2.2.2 DiffServ

DiffServ provides a scalable QoS architecture. It aggregates flows at the edge and processes these aggregates in the core. In other words it pushes complexity to the edges of the network and keeps the forwarding path simple.

In order to deliver end-to-end QoS, this architecture (RFC-2475) has two major components, packet marking and Per Hop Behaviors (PHBs). A small bit-pattern in each packet, in the IPv4 Type of Service (ToS) octet or the IPv6 [31] traffic class octet, is used to mark a packet to receive a particular PHB at each network node. A common understanding about the use and interpretation of this bit-pattern is required for inter-domain use, multi-vendor interoperability, and consistent reasoning about expected aggregate behaviors in a network. Thus, the DiffServ working group has standardized a common layout for a six-bit field of both octets, called the Differentiated Services Code Point (DSCP).

The PHBs standardized so far are as follows:

- Default behavior: here the DSCP value is zero and the service to be expected is exactly today's default Internet service with congestion and loss completely uncontrolled.
- Class Selector behavior [18]: here seven DSCP values run from 001000 to 111000 and are specified to select from these seven behaviors, each of which has a higher probability of timely forwarding than its predecessor. The default behavior plus the class selectors exactly mirror the original eight IP Precedence values.
- Expedited Forwarding (EF) behavior [29]: the recommended DSCP value is 101110 and the behavior is defined as being such that the departure rate of EF traffic must equal or exceed a configurable rate. EF is intended to allow the creation of real-time services with a configured throughput rate.
- Assured Forwarding (AF) behavior [43]: an AF behavior actually consists of three sub-behaviors; for convenience let them be denoted by AFx1, AFx2, and AFx3. When the network is congested, packets marked with the DSCP AFx1 have the lowest probability of being discarded by any router, and packets marked AFx3 have the highest such probability. Thus, within the AF class, differential drop probabilities are available, but otherwise the class behaves as a single PHB. The standard actually defines four independent AF classes. Quite complex service offerings can be constructed using AF behaviors, and much remains to be understood about them. However, AF PHB is most commonly used for providing bandwidth guarantees.

DiffServ carves out the whole network into domains. A DiffServ domain is a continuous set of nodes which support a common resource provisioning and PHB policy. It has a well defined boundary and there are two types of nodes associated with a Diff-Serv domain - Boundary nodes and Interior nodes. Boundary nodes connect the DiffServ cloud to other domains. Interior nodes are connected to other interior nodes or boundary nodes within the same DiffServ domain. A DiffServ domain is generally made up of an organization's intranet or an ISP, i.e. networks controlled by a single entity. DiffServ is extended across domains by SLAs between them.

Typically, the DiffServ boundary node performs traffic conditioning. A traffic conditioner performs MF classification on the incoming packets, aggregates them to pre-defined traffic classes, meters them to determine compliance to traffic parameters and determines whether the packet is in profile, or out of profile. It passes the result to a marker and shaper/dropper to trigger action for in/out-of-profile packets. Interior nodes map the DSCP of each packet into the set of PHB's and impart appropriate forwarding behavior.

A single-rate two-color token bucket marker represents the most basic DiffServ marker. Hereon, we refer to this as the classical token bucket. It marks packets green (in-profile) or red (out-of-profile). It has the traffic parameters Committed Information Rate (CIR) and its associated Committed Burst Size (CBS). The token bucket is filled with tokens at the rate of CIR and is capable of storing tokens up to the limit of CBS. Each arriving packet queries the token bucket. The packet is marked green if the token bucket has got at least the packet's size of tokens. Otherwise the packet is marked red. In addition to the classical token bucket the DiffServ working group has standardized three other types of markers; Single-Rate Three-Color Marker (SRTCM) [44], Two-Rate Three-Color Marker (TRTCM) [45], Time-Sliding-Window (TSW) [33]. The TRTCM marks packets green, yellow, or red based on two rates and two burst sizes and is useful when the peak rate needs to be enforced. The SRTCM marker also marks packets green, yellow or red. However, it is based on a single rate and two burst sizes and is useful when only burst size matters. Both these markers can operate in two modes, called color-blind and color-aware, that allow the new color to be dependent on its previous color. The SRTCM marker is configured by setting the mode and assigning values to three traffic parameters; CIR and its associated CBS, Extended Burst Size (EBS). On the other hand the TRTCM marker is configured by setting the mode and assigning values to four traffic



Figure 2.1: Color-Aware mode of SRTCM

parameters; Peak Information Rate (PIR) and its associated Peak Burst Size (PBS),CIR and its associated CBS. Figure 2.1 illustrates the operation of a color-aware SRTCM.

DiffServ enables scalable and coarse-grained QoS throughout the network but has some drawbacks. Some of the challenges for tomorrow and opportunities for enhancements and simplification are:

- Provisioning Unlike RSVP/IntServ, DiffServ needs to be provisioned. Setting up the various classes throughout the network requires knowledge of the applications and traffic statistics for aggregates of traffic on the network
- Loss of Granularity Even though QoS assurances are being made at the class level, it may be necessary to drill down to the flow-level to provide the requisite QoS. For example, although all Hyper Text Transfer Protocol (HTTP) traffic may have been classified as gold, and a bandwidth of 100Mbps assigned to it, there is no inherent mechanism to ensure that a single flow does not use up that allocated bandwidth.

- QoS and Routing One of the biggest drawbacks of both the IntServ and Diff-Serv models is the fact that signaling and provisioning happens separately from the routing process. There may exist a path other than the non-default Interior Gateway Protocol [IGP], such as Open Shortest Path First (OSPF) [67] and Intermediate System Intermediate System (IS-IS) [24] or Exterior Gateway Protocol [EGP], such as Border Gateway protocol (BGP-4) [82], path in the network that has the required resources, even when RSVP/DiffServ fails to find the resources. This is where Traffic Engineering (TE) and MPLS come into service. True QoS, with maximum network utilization, will arrive with the combination of traditional QoS and routing.
- TCP complexities TCP provides the mechanisms to signal hosts of congestion. It also defines the way hosts respond to congestion. TCP, which has been designed for a best effort service network, performs poorly in a DiffServ network. This is primarily because TCP remains unaware of the different levels of service tags each packet gets assigned in a DiffServ network. Internet traffic is predominantly TCP, and therefore performance issues of TCP in a DiffServ network can potentially inhibit the adoption of DiffServ. This is the central motivation of this thesis. In this thesis we investigate TCP performance issues in a DiffServ network and propose techniques to mitigate these issues.

2.3 Transmission Control Protocol

TCP builds on IP's best effort packet delivery service a reliable in-order byte stream transfer service for use by applications. It also implements congestion control, which prevents persistent network congestion. Congestion control mechanisms [50] were integrated after a series of congestion induced network problems in the late 1980s. Since then TCP congestion control has been one of the most active areas of computer networking research [89, 98]. Many refinements have been added [50, 62, 35], analytical models have been developed [63, 69, 3, 65, 61, 57, 59, 55], and comprehensive network simulations of TCP have been carried out [74, 1, 32].

The mechanisms introduced the notion of a sending window, which is the actual limit on the amount of outstanding data, and is computed as the minimum of the receiver window and a congestion window that is dynamically changed according to network conditions. The receiver window is advertised by the receiver and indicates the amount of buffer space available for packet reception. In the absence of explicit congestion notification from the network, TCP primarily relies on packet loss as an indication of network congestion. Thus, when TCP detects packet loss, it considers that the network is congested, and throttles its sending rate by decreasing the congestion window value. TCP considers two indications of packet loss. The first is the expiry of the retransmit timeout. The second indication is the receipt of multiple acknowledgments which carry the same sequence number. These acknowledgements are sent by the receiver when out-of-order segments arrive, and thereby indicate a gap in the received sequence space. Therefore, the receipt of several such acknowledgements constitutes a likely indication that packet loss has occurred. More precisely, the TCP sender considers that loss has occurred when at least 3 such acknowledgments are received, and retransmits the apparently lost segments. This procedure is called Fast Retransmit (FR). The requirement that a number of such acknowledgements be received is an attempt to filter out cases where temporary gaps result due to packet re-ordering.

Beginning transmission into a network with unknown conditions requires TCP to slowly probe the network to determine the available capacity, in order to avoid congesting the network with an inappropriately large burst of data. The slow start algorithm is used for this purpose at the beginning of a transfer, or after repairing loss detected by the retransmission timer. During periods where no packet loss is observed, TCP continuously increases the congestion window in order to determine whether a higher throughput can be achieved under the current network conditions. The rate of increase of the congestion window is exponential when a connection is started, where each new acknowledgment prompts the sender to increase the window size by one segment. However, it is slowed down to an additive increase when the window value exceeds a certain threshold. The exponential increase phase is called Slow Start (SS), while the additive increase phase is called Congestion Avoidance (CA). The threshold at which the transition happens is dynamically varied as the transfer progresses. More precisely, it is set to half the current congestion window size when packet loss is detected. When packet loss is detected, the congestion window size is decreased as well. Following a retransmit timeout, considered an indication of severe congestion, the window is reset to 1 segment.

When TCP's congestion control mechanisms were first implemented [50], the window size would be set to 1 segment following the reception of multiple acknowledgements of the same sequence number, similarly to following a retransmit timeout. This behavior has been changed in subsequent revisions of the mechanism, on the basis that a Fast Retransmit corresponds to a milder congestion indication than a retransmit timeout as it implies that packets are still leaving the network. In fact, TCP's congestion control mechanisms have evolved over time, as more became known about their behavior and performance in the network, resulting in the current TCP versions. The second version, called TCP Reno [2], differed from the first in terms of its behavior following a Fast Retransmit. Thus, instead of reducing the window to one segment, TCP Reno reduces it by half, resulting in a higher sending rate after the loss is recovered. The procedure followed to implement this change is called Fast Recovery. TCP enhancements like Selective Acknowledgement (SACK) [62] let the receiver notify exactly what has arrived and what has not. TCP Reno is known to generally not recover very efficiently from multiple losses in a single flight of packets [32] when the SACK option of TCP is not used. [35] proposed a set of modifications to address this problem.

A vast majority of TCP implementations adopt the above described mechanisms.

Internet links' speeds range from 56 Kbps dialup to 10 Gbps fiber-optic links. Links also differ greatly in other aspects such as bit error rate and propagation delay. The above described congestion control mechanisms fail to deliver a consistent level of performance under these wideranging conditions. [97, 54, 100, 22, 36, 83, 53, 17, 48] propose mechanisms that have been developed for use in these different contexts.

Chapter 3

Modeling TCP Behavior in a DiffServ Network

A DiffServ network is a complex system comprising packet meters, markers and queue management techniques. An accurate model of TCP is of great importance when dealing with such a complex system. It helps determine the performance expected of these networks. TCP in a best effort service network, in particular its congestion avoidance aspects, has been extensively studied and many analytical models have been developed, for example [63, 69, 3, 65, 61, 57, 59, 55]. For the most commonly used flavors of TCP [62, 2, 37, 51], congestion avoidance evolves around an Additive Increase and Multiplicative Decrease (AIMD) congestion window algorithm. Most models are centered on this AIMD congestion window behavior with refinements that capture other mechanisms of congestion control, namely slow start, timeout, fast retransmit, fast recovery and receiver limited window. Some of these models are extended in [102, 85, 14, 92, 13] to a DiffServ network.

At the edge of a DiffServ network, flows are aggregated and that makes it distinctly different from a best effort network. Inherently flow-based models developed for a best effort network fail to accurately capture this flow aggregation. This is a major limitation of currently proposed models of DiffServ controlled TCP. Moreover, these models are limited to studying the steady state behavior. We develop from first principles a dynamic model of a DiffServ controlled TCP flow aggregate and use it to analyse both the steady state and transient behavior.

In the next two sections we review currently proposed models of TCP in Best Effort and DiffServ networks. Section 3.3 lists our contributions. In section 3.4 we introduce the network model and preliminary derivations followed by analysis of convergence properties of the congestion window in section 3.5. Steady state and transient behaviors are studied in sections 3.6 and 3.7, respectively. Simulation studies are presented in section 3.8.

3.1 Related Work: TCP Behavior in a Best Effort Network

One of the first analytical models of TCP appears in [63]. They derive the stationary distribution of the congestion window size assuming losses of packets constitute an independent and identically distributed (iid) random variable. They use a fluid flow, continuous time approximation to the discrete time process. The congestion avoidance mechanism they model is idealized in the sense that the effects of TCP timeout or a receiver limited window are ignored. They show that if every packet is lost with a probability p, assumed to be small, then the average window size and long range throughput are of the order of $1/\sqrt{p}$.

[69] develops a more complete analytical characterization of TCP throughput that also captures the behavior of TCP's fast retransmit, timeout and receiver limited window. They derive the following expression for the steady state throughput, r,

$$r = \min\left(\frac{W_{max}}{RTT}, \frac{1}{RTT\sqrt{\frac{2bp}{3}} + T_O \min\left(1, 3\sqrt{\frac{3bp}{8}}\right)p\left(1 + 32p^2\right)}\right)$$

where p is the packet loss probability, b is the number of packets that are acknowledged by a received TCP ACK packet, RTT is the average round trip time and T_O is the TCP timeout value.

A TCP throughput model under a more generalized loss model is developed in [3]. A random process, only assumed to be stationary, characterizes the packet loss. This allows them to account for any correlation and any distribution of inter-loss times.

Assuming loss events arriving at the source as a Poisson stream, [65] models the window size behavior as a Poisson counter driven stochastic differential equation. They also use a fluid flow, continuous time approximation to the discrete time process as done in [63]. They extend this in [66, 47, 46] where the packet loss rate is made dependent on the data flow. Jump process driven stochastic differential equations are used to model the interactions of a set of TCP flows and Active Queue Management (AQM) routers in a network setting. This model relates the average value of key network variables. A simplified version of that model which ignores the TCP timeout mechanism is described by the following coupled, nonlinear differential equations:

$$\begin{aligned} \dot{W}(t) &= \frac{1}{R(t)} - \frac{W(t)W(t - R(t))}{2R(t - R(t))}p(t - R(t)), \\ \dot{q}(t) &= \frac{W(t)}{R(t)}N(t) - C, \end{aligned}$$

where \dot{x} denotes the time-derivative of x, W denotes the expected TCP window size in packets, q denotes the expected queue length in packets, $R(=\frac{q}{C}+T_p)$ denotes the roundtrip time, C denotes the link capacity, T_p denotes the propagation delay, N denotes the number of TCP sessions and p denotes the probability of packet mark/drop. In [47], these non-linear differential equations are transformed into a set of Ordinary Differential Equations described below, around the operating point (W_0, q_0, p_0).

$$\delta \dot{W}(t) = -\frac{2N}{R_0^2 C} \delta W(t) - \frac{R_0 C^2}{2N^2} \delta p(t - R_0),$$

$$\delta \dot{q}(t) = \frac{N}{R_0} \delta W(t) - \frac{1}{R_0} \delta q(t).$$

Where

$$\delta W = W - W_0,$$

$$\delta q = q - q_0,$$

$$\delta p = p - p_0,$$

$$W_0 = \frac{R_0 C}{N},$$

$$R_0 = \frac{q_0}{C} + T_p,$$

and T_p is the round trip propagation delay. They map this differential equation based system into a classical control system model. The control system model has been extensively used in wideranging applications, in particular, for analysis and design of enhanced AQM techniques.

Some other models of TCP include [61, 57, 59, 55].

3.2 Related Work: TCP Behavior in a DiffServ Network

DiffServ fundamentally changes the closed-loop TCP behavior. The packet loss model becomes more complicated as core routers treat each arriving packet according to its level of conformance. In the presence of congestion, out-of-profile packets are more likely to be dropped compared to in-profile packets. Basically this impacts both the transient and the steady state TCP throughput. The steady state throughput of a TCP flow in a DiffServ network is studied in [102, 85, 14, 92, 13]. These studies can be seen as extensions of TCP models developed in [63, 69, 3].

These throughput models are based around similar network models. They all consider DiffServ Assured Forwarding (AF) Per-Hop-Behavior (PHB). Figure 3.1 shows a typical DiffServ network model in which a sender gains access to the network core through an edge router which marks packets. We confine our study to a 2-color marking edge, and



Figure 3.1: A Simplified DiffServ Network Model

a two drop precedence core, a common DiffServ network scenario considered in all of the previous studies. If the sending rate of a flow conforms to its marking profile, the packets are marked in-profile (green) and otherwise out-of-profile (red). [102, 13] use a time sliced window estimator and [102, 92] use a token bucket marker at the edge. The time sliced window estimator is modeled by two parameters, contract rate, A, and the size of the estimation window, w_{len} . [102] uses a window size which is in the order of a Round Trip Time (RTT) and [13] uses an infinity sized estimation window producing a long-term rate estimate. The token bucket marker used in [85, 92] is parameterized by the contract rate, A, and the token bucket size, B. All of these studies, except for [92], primarily focus on a single TCP flow. [92] uses a single TCP aggregate consisting of nflows. The interference of other flows sharing the same bottleneck path is modeled by induced losses in the flow under study in the bottleneck path. It can be either an

- Over-provisioned path; a flow experiences no in-profile packet drops but experiences some OUT packet drops, or an
- Under-provisioned path; a flow fails to transmit any OUT packets either because every OUT packet is dropped or because the sending rate is less than the contract rate.

When a non-overlapping drop precedence is used in the network core, as illustrated in Figure 3.2, the in-profile (green) and out-of-profile (red) packet drop probabilities, p_g and p_r respectively, satisfy

- $p_g = 0, p_r > 0$ in an over-provisioned network path, and
- $p_g \ge 0, p_r = 1$ in an under-provisioned network path.

Within a non-overlapping drop precedence network core, the throughput of a TCP flow through an under-provisioned network path closely resembles that of a best effort network. We confine our study to an over-provisioned network. A well-engineered DiffServ network with proper admission control is most likely to operate in this regime. All of the studies assume that flows experience a constant RTT, T.

[102] derives fairly simple expressions for the bandwidth of a single connection, r, in an over-provisioned network assuming low drop probabilities and high contract rates.

$$r = \begin{cases} \frac{\left(A + \sqrt{A^2 + \frac{6}{p_r T^2}}\right)}{2} & A \le \frac{1}{T} \sqrt{\frac{2}{p_r}} \\ \frac{3A}{4} + \frac{3\sqrt{\frac{1}{p_r}}}{2\sqrt{2T}} & A \ge \frac{1}{T} \sqrt{\frac{2}{p_r}} \end{cases}$$
(3.1)

From the above equations it can be observed that;

- If A is greater than $3\frac{\sqrt{2/p_r}}{T}$, the flow cannot reach its contract rate.
- When a flow reserves relatively lower bandwidth $A < \frac{\sqrt{2/p_r}}{T}$ it always realizes at least its contract rate. As it contracts less bandwidth, it obtains more excess bandwidth. TCP's multiplicative decrease of sending rate after observing a packet drop results in a higher loss of bandwidth for flows with higher contract rates.
- As the probability of OUT packet drop decreases, the flows with smaller contract rates benefit more than the flows with larger contract rates.
- The realized bandwidth is observed to be inversely related to the RTT of the flow.
- For best-effort flows, A = 0. Hence, $r = \sqrt{6/p_r}/2T$.

• Excess bandwidth is not equally shared by flows with different contract rates.

[13] also presents an analytical model similar to [102], with the notable difference of using a long-term rate based time sliding window estimator and an idealized TCP window. This basically extends the TCP model in [63] to a DiffServ environment.

[85] considers the steady state throughput of a TCP flow when token bucket markers are used at the network edge, and as a result the model accounts for the important DiffServ network parameter token bucket size. Let B denote the token bucket size. For an over-provisioned network they derive the bandwidth as

$$r = \begin{cases} \frac{\left(A + \sqrt{A^2 + \frac{6}{p_r T^2}}\right)}{2} & A \le \frac{1}{T} \left(\sqrt{2\left(B + \frac{1}{p_r}\right)} + 2\sqrt{2B}\right) \\ \frac{3A}{4} + \frac{3\sqrt{B + \frac{1}{p_r}}}{2\sqrt{2T}} & A > \frac{1}{T} \left(\sqrt{2\left(B + \frac{1}{p_r}\right)} + 2\sqrt{2B}\right) \end{cases}$$
(3.2)

This reduces to equation (3.1) when B = 0 and therefore similar conclusions can be drawn. However, as the token bucket size is accounted for, they identify conditions under which the achieved rate is sensitive to the choice of the bucket size and, determine what profile rates are achievable and what are not. From their expressions for the bandwidth, it can be seen that the condition

$$A > \frac{1}{T} \left(\sqrt{2\left(B + \frac{1}{p_r}\right)} + 2\sqrt{2B} \right)$$

leads to the case where the achieved rate is influenced by the choice of bucket size. This condition refers to the case where the bucket size imposes a constraint, i.e., more tokens are generated than can be stored in the bucket. On the other hand, whenever

$$A \le \frac{1}{T} \left(\sqrt{2\left(B + \frac{1}{p_r}\right)} + 2\sqrt{2B} \right)$$

the achieved rate is not affected by the choice of bucket size.

[92] extends the work in [63] to derive the steady state throughput of a TCP aggregate with n flows when token bucket markers are deployed at the network edge. They derive



Figure 3.2: Non-Overlapping Drop Precedence Curves in a DiffServ Network

the bandwidth as

$$r = \begin{cases} \frac{\left(A + \sqrt{A^2 + \frac{6n^2}{p_r T^2}}\right)}{2} & A \le \frac{1}{T} \left(\sqrt{2\left(nB + \frac{n^2}{p_r}\right)} + 2\sqrt{2nB}\right) \\ \frac{3A}{4} + \frac{3\sqrt{nB + \frac{n^2}{p_r}}}{2\sqrt{2T}} & A > \frac{1}{T} \left(\sqrt{2\left(nB + \frac{n^2}{p_r}\right)} + 2\sqrt{2nB}\right) \end{cases}$$
(3.3)

Even though the above equation is for a flow aggregation, this model fails to accurately capture flow aggregation, which is central to DiffServ functionality. This is clearly evident as this equation (3.3) can be derived from the equation (3.2), by adding the rate of n separate flows with a contract rate equal to $\frac{A}{n}$ and a token bucket size of $\frac{B}{n}$.

[14] proposes a stochastic model of DiffServ controlled TCP based on a Markovian fluid approach. They build a framework within which different token bucket variants [101] are evaluated.

3.3 Our Contributions

All of the previous studies are limited to characterizing the steady state behavior. Another notable limitation is their primary focus being on a single TCP flow. As noted earlier the model in [92], although it derives the rate of a TCP flow aggregate, it fails to accurately capture flow aggregation.
We develop an analytical model from first principles and use it to analyse both the steady state and transient TCP throughput in an over-provisioned DiffServ network.

We make the following contributions;

- We develop a model that intrinsically captures DiffServ flow aggregation. This allows us to accurately measure the effect that the number of flows per aggregate imparts on TCP throughput.
- Analyze convergence properties of the aggregate TCP congestion window size in wide-ranging conditions. This provides insights to TCP congestion window's oscillatory behavior.
- Study both the transient and steady state TCP behavior. We represent DiffServ controlled TCP dynamics in a classical control system model. It allows use of standard techniques to analyze various mechanisms and propose improvements to algorithms as well as analysis-backed guidelines for choosing parameters of the algorithms.
- Derive more complete expressions for excess bandwidth distribution in terms of number of flows per aggregate, RTT, contract rate, and token bucket size.

3.4 The Network Model

In this section we introduce the network model. We consider a DiffServ network with two color token bucket markers at the edge and a two drop precedence core. We confine our study to an over-provisioned network.

The total congestion window size of aggregate a in the *i*th cycle is denoted by the variable $w_{a,i}$, where $i \in \mathbb{Z}^*$. Each packet drop marks the renewal of a cycle. $D_{a,i}$ denotes the drop in the window size in cycle (i), in response to a packet drop. B_i is the maximum number of tokens accumulated in the bucket. We call $W_a(=A_aT_a)$ the contract window



Figure 3.3: The Aggregate TCP Congestion Window.

size of the *a*th aggregate, where A_a is the contract rate and T_a the Round-Trip-Time (RTT) of flows belonging to that aggregate. Let $\check{w}_{a,i}$ and $\hat{w}_{a,i}$ denote the deviation of $w_{a,i}$ from W_a at the beginning and end of each cycle. The number of RTTs required for $w_{a,0}$ to reach $\hat{w}_{a,0}$ from W_a is denoted by $m_{a,0}$. For subsequent cycles $m_{a,i}$ denotes the number of RTTs per cycle. n_a denotes the number of flows of the *a*th aggregate and p_g and p_r denote, respectively, the in-profile and out-of-profile packet dropping probabilities at the core router. To simplify the analysis we make the following further assumptions.

- 1. Flows of each aggregate are TCP. We adopt an idealized TCP congestion avoidance behavior. Each flow simply increases the congestion window by one per RTT in the absence of any packet loss and halves the congestion window in response to a packet loss, without invoking slow start or fast retransmit/recovery mechanisms.
- 2. RTTs of all flows within an aggregate are equal and constant $(=T_a)$. Therefore the increment in the total congestion window per RTT of an aggregate is n_a .

- 3. The core router has non-overlapping packet dropping curves for green and red packets. This implies that $p_g = 0$ and $p_r \ge 0$ as the network is over-provisioned. We also assume that p_r does not change over time.
- 4. Each aggregate gets through the number $1/p_r$ of red packets before experiencing a packet loss. This is actually the mean number of red packet transmissions between consecutive packet losses [85]. If it is further assumed that packet drop events constitute a Poisson process, then the standard deviation of this number is $1/\sqrt{p_r} \ll 1/p_r$ for small p_r . This leads to our deterministic model.
- 5. $w_{a,i}$ is shared equally among flows within that aggregate. This assumption simplifies calculation of the reduction in $w_{a,i}$ in response to a packet loss.

If $w_{a,i}$ starts from below W_a ($\check{w}_{a,i} < 0$), during the period $w_{a,i} < W_a$ the token bucket generates more tokens than the number of packet arrivals. The token bucket stores up to B excess tokens before tokens get discarded. Cycle (i-1) in Figure 3.3 illustrates a TCP renewal cycle in which the token bucket overflows. When $w_{a,i} > W_a$, the rate of packet arrival exceeds the token generation rate, and therefore stored tokens are used. When the token bucket is exhausted, it starts marking packets out-of-profile. This behavior is represented by the following equations

$$\check{w}_{a,i-1} < 0,
\check{w}_{a,i-1}^2 = B + \frac{1}{p_r},$$
(3.4)

$$D_{a,i-1} = \frac{W_a + \hat{w}_{a,i-1}}{2n_a},$$

= $\frac{A_a T_a + \sqrt{2n_a (B + \frac{1}{p_r})}}{2n_a}.$ (3.5)

In some cycles, the number of accumulated excess tokens is less than the size of the token bucket. This prevents a token bucket overflow. The token bucket starts marking packets out-of-profile earlier as a full bucket of tokens is not available. Cycle (i + 1) in Figure 3.3 illustrates this situation. We have,

$$\begin{aligned}
\tilde{w}_{a,i+1} &< 0, \\
\frac{\hat{w}_{a,i+1}^2}{2n_a} &= B_{i+1} + \frac{1}{p_r}, \\
&= \frac{\check{w}_{a,i+1}^2}{2n_a} + \frac{1}{p_r}, \\
D_{a,i+1} &= \frac{W_a + \hat{w}_{a,i+1}}{2n_a}, \\
&= \frac{A_a T_a + \sqrt{\check{w}_{a,i+1}^2 + \frac{2n_a}{p_r}}}{2n_a}.
\end{aligned}$$
(3.6)
(3.7)

In some other situations, for example cycle (i) in Figure 3.3, the congestion window drop in response to a packet loss does not take the congestion window below W_a . No excess tokens are generated in this case. This can be represented by the following equations,

$$\begin{split}
\check{w}_{a,i} > 0, \\
\hat{w}_{a,i}^{2} = \frac{\check{w}_{a,i}^{2}}{2n_{a}} + \frac{1}{p_{r}}, \\
D = W_{a} + \hat{w}_{a,i-1}
\end{split}$$
(3.8)

$$D_{a,i} = \frac{N_a + w_{a,i-1}}{2n_a},$$

= $\frac{A_a T_a + \sqrt{\tilde{w}_{a,i}^2 + \frac{2n_a}{p_r}}}{2n_a}.$ (3.9)

3.5 Aggregate TCP Congestion Window Behavior

We first consider the TCP renewal cycle for i = 0. During each RTT, $w_{a,i}$ increases by n_a . Therefore, $\hat{w}_{a,0} = m_{a,0}n_a$. The number of packets generated in this cycle, for $w_{a,0} > W_a$ is equal to the total of in-profile packets generated at the contract rate, in-profile packets generated (= B) because of the tokens accumulated during $w_{a,0} \leq W_a$ and $1/p_r$ OUT packets. Therefore we have,

$$1/p_r + B = \frac{\hat{w}_{a,0}^2}{2n_a}.$$

Solving for $\hat{w}_{a,0}$ gives

$$\hat{w}_{a,0} = \sqrt{2n_a \left(\frac{1}{p_r} + B\right)}.\tag{3.10}$$

At the first packet loss, the drop of $w_{a,0}$ is equal to

$$D_{a,0} = \frac{A_a T_a + \sqrt{2n_a \left(\frac{1}{p_r} + B\right)}}{2n_a}.$$

Different behaviors of $w_{a,i}$ are produced depending on the size of this reduction in $w_{a,0}$.

3.5.1 Behavior 1

If the fall in the window in response to the first packet drop is at least the size of $\hat{w}_{a,0}$, the next renewal cycle starts from below W_a , i.e. $\check{w}_{a,1} < 0$. This requires,

$$\frac{A_a T_a}{2n_a} + \sqrt{\frac{1}{2n_a} \left(\frac{1}{p_r} + B\right)} \geq \sqrt{2n_a \left(\frac{1}{p_r} + B\right)},$$
$$A_a \geq \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)}}{T_a}.$$

We have,

$$\check{w}_{a,1} \leq 0,$$

$$= \left(1 - \frac{1}{2n_a}\right) \sqrt{2n_a \left(\frac{1}{p_r} + B\right)} - \frac{A_a T_a}{2n_a}$$

Excess tokens are generated in this TCP renewal cycle. If it leads to a token bucket overflow we have, $\hat{w}_{a,1} = \sqrt{2n_a\left(\frac{1}{p_r} + B\right)} = \hat{w}_{a,0}$. This results in $\hat{w}_{a,i} = \hat{w}_{a,0}$ for all *i*, i.e. the aggregate congestion window converges to a limit cycle as depicted in Figure 3.4. A token bucket overflow at the first renewal cycle requires,

$$\frac{\check{w}_{a,1}^2}{2n_a} \ge B$$

Therefore, we have

$$\frac{A_a T_a}{2n_a} - \left(1 - \frac{1}{2n_a}\right) \sqrt{2n_a \left(\frac{1}{p_r} + B\right)} \ge \sqrt{2n_a B}$$



Figure 3.4: The Aggregate TCP Congestion Window for A = 40000, $p_r = 0.2$, n = 20, B = 50, T = 0.1

$$A_a \ge \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)} + 2n_a \sqrt{2n_a B}}{T_a}.$$

3.5.2 Behavior 2

Failure to overflow the token bucket during the first TCP renewal cycle means that it accumulates $B_1 = \frac{\tilde{w}_{a,1}^2}{2n_a} < B$ excess tokens while $w_{a,1} \leq W_a$. In general, for cycle *i*, assuming it accumulates $B_i < B$ tokens while $w_{a,i} \leq W_a$, we have,

$$\hat{w}_{a,i}^2 = 2n_a \left(\frac{1}{p_r} + B_i\right).$$
(3.11)

Therefore,

$$\hat{w}_{a,i} \le \sqrt{2n_a \left(\frac{1}{p_r} + B\right)} = \hat{w}_{a,0} \quad \forall i.$$
(3.12)

•

We also have

$$\check{w}_{a,i}^2 = \hat{w}_{a,i}^2 - \frac{2n_a}{p_r}$$

An upper bound on $\check{w}_{a,i}$ can be derived using the inequality (3.12), i.e.

$$\check{w}_{a,i}^2 \leq \hat{w}_{a,0}^2 - \frac{2n_a}{p_r},
= 2n_a B \quad \forall i.$$
(3.13)

As the above inequality implies, the failure to overflow the token bucket in the first TCP renewal cycle prevents any subsequent token bucket overflows. We have,

$$\check{w}_{a,i} = \hat{w}_{a,i-1} \left(\frac{1}{2n_a} - 1 \right) + \frac{W_a}{2n_a},$$
(3.14)

$$\hat{w}_{a,i}^2 = \check{w}_{a,i}^2 + \frac{2n_a}{p_r}.$$
(3.15)

We can prove that the sequence $\hat{w}_{a,i}$ converges to a fixed point \hat{w}_a using the contraction mapping theorem. From the above equations we get,

$$\hat{w}_{a,i}^2 = \left[\hat{w}_{a,i-1}\left(1 - \frac{1}{2n_a}\right) - \frac{W_a}{2n_a}\right]^2 + \frac{2n_a}{p_r}.$$

Let

$$f(z) = \sqrt{\left[z\left(1 - \frac{1}{2n_a}\right) - \frac{W_a}{2n_a}\right]^2 + \frac{2n_a}{p_r}}$$

We have

$$f'(z) = \frac{2\left[z\left(1-\frac{1}{2n_a}\right)-\frac{W_a}{2n_a}\right](1-\frac{1}{2n_a})}{2\sqrt{\left[z\left(1-\frac{1}{2n_a}\right)-\frac{W_a}{2n_a}\right]^2+\frac{2n_a}{p_r}}}, \\ < \frac{\left[z\left(1-\frac{1}{2n_a}\right)-\frac{W_a}{2n_a}\right](1-\frac{1}{2n_a})}{\left[z\left(1-\frac{1}{2n_a}\right)-\frac{W_a}{2n_a}\right]}, \\ < 1.$$

Therefore, from the Mean Value Theorem [42] we have,

$$|\hat{w}_{a,i} - \hat{w}_{a,i-1}| < K |\hat{w}_{a,i-1} - \hat{w}_{a,i-2}|$$

where K < 1. It follows that $f : I \to I$ is a contraction and the contraction mapping theorem [42] establishes the convergence of the sequence $\hat{w}_{a,i}$. Therefore values of A_a ,

$$\frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)} + 2n_a \sqrt{2n_a B}}{T_a} > A_a > \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)}}{T_a}$$

lead to a congestion window trace as depicted in Figure 3.5.

3.5.3 Behavior 3

When

$$\frac{(2n_a-1)\sqrt{2n_a\left(\frac{1}{p_r}+B\right)}}{T_a} > A_a$$

the congestion window in the first TCP renewal cycle starts from above W_a . The congestion window in the following TCP renewal cycles depends on the size of $\hat{w}_{a,1}$. If $\hat{w}_{a,1} < \hat{w}_{a,0}$, we can prove that $\hat{w}_{a,i}$ is monotonically decreasing while $\check{w}_{a,i} \ge 0$. We have

$$\hat{w}_{a,1}^2 = \check{w}_{a,1}^2 + \frac{2n_a}{p_r}, \hat{w}_{a,0}^2 = 2n_a B + \frac{2n_a}{p_r}.$$



Figure 3.5: The Aggregate TCP Congestion Window for $A = 24000, p_r = 0.2, n = 20, B = 50, T = 0.1$



Figure 3.6: The Aggregate TCP Congestion Window for A = 16000, $p_r = 0.2$, n = 20, B = 50, T = 0.1



Figure 3.7: The Aggregate TCP Congestion Window for $A = 6000, p_r = 0.2, n = 20,$ B = 50, T = 0.1

Therefore, $\hat{w}_{a,1} < \hat{w}_{a,0}$ requires

$$\begin{split} &\sqrt{2n_aB} > & \check{w}_{a,1} \ge 0, \\ &\sqrt{2n_aB} > & \hat{w}_{a,0} - \frac{W_a + \hat{w}_{a,0}}{2n_a} \ge 0 \end{split}$$

Solving for A_a we get,

$$\frac{(2n_a-1)\sqrt{2n_a\left(\frac{1}{p_r}+B\right)}}{T_a} \ge A_a > \frac{(2n_a-1)\sqrt{2n_a\left(\frac{1}{p_r}+B\right)} - 2n_a\sqrt{2n_aB}}{T_a}.$$
 (3.16)

To prove that $\hat{w}_{a,i}$ is monotonically decreasing we use the principle of mathematical induction. We have the initial condition $\hat{w}_{a,1} < \hat{w}_{a,0}$. We now make the induction hypothesis, $\hat{w}_{a,k} \leq \hat{w}_{a,k-1}$. $\check{w}_{a,k}$ and $\check{w}_{a,k+1}$ are equal to,

$$\tilde{w}_{a,k} = \hat{w}_{a,k-1} \left(1 - \frac{1}{2n_a} \right) - \frac{W_a}{2n_a}, \\
\tilde{w}_{a,k+1} = \hat{w}_{a,k} \left(1 - \frac{1}{2n_a} \right) - \frac{W_a}{2n_a}.$$

Therefore,

$$\check{w}_{a,k+1} - \check{w}_{a,k} = (\hat{w}_{a,k} - \hat{w}_{a,k-1}) \left(1 - \frac{1}{2n_a}\right).$$

We have $\hat{w}_{a,k} \leq \hat{w}_{a,k-1}$ from the induction hypothesis, hence $\check{w}_{a,k+1} \leq \check{w}_{a,k}$ as the above equation implies. To prove $\hat{w}_{a,k+1} \leq \hat{w}_{a,k}$ we note that

$$\hat{w}_{a,i}^2 - \check{w}_{a,i}^2 = \frac{2n_a}{p_r}$$

 $\check{w}_{a,k+1} \leq \check{w}_{a,k}$ implies $\hat{w}_{a,k+1} \leq \hat{w}_{a,k}$. Then by induction we have that $\hat{w}_{a,i+1} \leq \hat{w}_{a,i} \forall i$. For some values of A_a within the above range, $\check{w}_{a,i}$ dips below W_a in its descent. This complicates the congestion window behavior. When the congestion window dips below W_a , the next TCP renewal cycle starts above the start of the previous TCP renewal cycle because of excess tokens generated while $w_{a,i} < W_a$. Therefore, this breaks the decrease in the congestion window. Let $\check{w}_a = \lim_{i\to\infty} \check{w}_{a,i}$ denote the equilibrium window size, Equation (3.21), which is equal to

$$\check{w}_a = \frac{-2n_a + (2n_a - 1)\sqrt{1 + \frac{2n_a(4n_a - 1)}{A_a^2 T_a^2 p_r}}}{A_a T_a(4n_a - 1)}.$$

For values of,

$$A_a \geq \frac{(2n_a - 1)\sqrt{\frac{2n_a}{p_r}}}{T_a}$$

we have $\check{w}_a \leq 0$ and the congestion window dips below the contract window size. Figures 3.6 and 3.7 show the congestion window traces for two values of A_a in this range,

$$\frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)}}{T_a} > A_a > \frac{(2n_a - 1)\sqrt{\frac{2n_a}{p_r}}}{T_a}.$$

3.5.4 Behavior 4

When

$$\frac{(2n_a - 1)\sqrt{\frac{2n_a}{p_r}}}{T_a} > A_a > \frac{(2n_a - 1)\sqrt{2n_a\left(\frac{1}{p_r} + B\right) - 2n_a\sqrt{2n_aB}}}{T_a}$$

the congestion window converges above W_a . The congestion window trace for a contract rate in this range is depicted in the Figure 3.8.

3.5.5 Behavior 5

For

$$\frac{(2n_a-1)\sqrt{2n_a\left(\frac{1}{p_r}+B\right)}-2n_a\sqrt{2n_aB}}{T_a} \ge A_a$$

we have

$$\hat{w}_{a,1} \ge \hat{w}_{a,0}.$$

We can prove that $\hat{w}_{a,i}$ converges by showing that the sequence $\hat{w}_{a,i}$ is bounded and monotonically increasing, which is sufficient for proving convergence [42]. We have that $\hat{w}_{a,i} \leq 1/p_r$. To prove that $\hat{w}_{a,i}$ is monotonically increasing we follow similar reasoning



Figure 3.8: The Aggregate TCP Congestion Window for $A = 4000, p_r = 0.2, n = 20,$ B = 50, T = 0.1



Figure 3.9: The Aggregate TCP Congestion Window for A = 500, $p_r = 0.2$, n = 20, B = 50, T = 0.1

to that presented in section 3.5.3. We have $\hat{w}_{a,1} > \hat{w}_{a,0}$. From the induction hypothesis we also have, $\hat{w}_{a,k} \ge \hat{w}_{a,k-1}$. Then for i = k, k+1, following from the analysis in section 3.5.3, we have,

$$\check{w}_{a,k+1} - \check{w}_{a,k} = (\hat{w}_{a,k} - \hat{w}_{a,k-1}) \left(1 - \frac{1}{2n_a} \right).$$

From the above $\hat{w}_{a,k} \ge \hat{w}_{a,k-1}$ implies that $\check{w}_{a,k+1} \ge \check{w}_{a,k}$. To prove $\hat{w}_{a,k+1} \ge \hat{w}_{a,k}$ we note that

$$\hat{w}_{a,i}^2 - \check{w}_{a,i}^2 = \frac{2n_a}{p_r}$$

Therefore $\check{w}_{a,k+1} \geq \check{w}_{a,k}$ implies $\hat{w}_{a,k+1} \geq \hat{w}_{a,k}$. Then by induction we have that $\hat{w}_{a,i+1} \geq \hat{w}_{a,i}$. Therefore the sequence $\hat{w}_{a,i}$ converges $\forall i$, i.e. $\lim_{i\to\infty} \hat{w}_{a,i} = \hat{w}_a$, $\check{w}_{a,i} = \check{w}_a$ and $w_{a,i} = w_a$. Figure 3.9 shows the window trace for a value of A_a in this range.

3.6 Steady State Behavior

Having established the convergence properties of $w_{a,i}$ we now consider the steady state behavior and derive the average rate of packet generation at steady state, r. Loss of tokens occurs only during the first behavior of the five different TCP congestion window behaviors considered above. For this particular congestion window behavior we have,

$$W_a + \check{w}_a = \left(1 - \frac{1}{2n_a}\right) (W_a + \hat{w}_a),$$
 (3.17)

$$B + \frac{1}{p_r} = \frac{\hat{w}_a^2}{2n_a}.$$
 (3.18)

Solving for \hat{w}_a , \check{w}_a we obtain,

$$\hat{w}_{a} = \sqrt{2n_{a}\left(B + \frac{1}{p_{r}}\right)},$$

$$\check{w}_{a} = \left(1 - \frac{1}{2n_{a}}\right)\sqrt{2n_{a}\left(B + \frac{1}{p_{r}}\right)} - \frac{W_{a}}{2n_{a}}.$$

Therefore,

$$w_{a} = W_{a} + \frac{\hat{w}_{a} + \check{w}_{a}}{2},$$

$$= \left(1 - \frac{1}{4n_{a}}\right) \left(A_{a}T_{a} + \sqrt{2n_{a}\left(B + \frac{1}{p_{r}}\right)}\right),$$

$$r = \frac{w_{a}}{T_{a}},$$

$$= \left(1 - \frac{1}{4n_{a}}\right) \left(A_{a} + \frac{\sqrt{2n_{a}\left(B + \frac{1}{p_{r}}\right)}}{T_{a}}\right),$$

$$m_{a} = \frac{\hat{w}_{a} - \check{w}_{a}}{n_{a}},$$

$$= \frac{1}{2n_{a}^{2}} \sqrt{2n_{a}\left(B + \frac{1}{p_{r}}\right)} + \frac{W_{a}}{2n_{a}^{2}}.$$

No tokens are lost for other values of the contract rate, given by

$$A_a \le \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)} + 2n_a \sqrt{2n_a B}}{T_a}.$$

We have,

$$W_a + \check{w}_a = \left(1 - \frac{1}{2n_a}\right) (W_a + \hat{w}_a),$$
 (3.19)

$$\frac{\check{w}_a^2}{2n_a} + \frac{1}{p_r} = \frac{\hat{w}_a^2}{2n_a}.$$
(3.20)

Solving the above we get,

$$\check{w}_a = \frac{-2n_a A_a T_a + (2n_a - 1)\sqrt{A_a^2 T_a^2 + \frac{2n_a (4n_a - 1)}{p_r}}}{(4n_a - 1)}, \qquad (3.21)$$

$$\hat{w}_a = \frac{-(2n_a - 1)A_a T_a + 2n_a \sqrt{A_a^2 T_a^2 + \frac{2n_a(4n_a - 1)}{p_r}}}{(4n_a - 1)}, \qquad (3.22)$$

$$w_a = \frac{A_a T_a + \sqrt{A_a^2 T_a^2 + \frac{2n_a(4n_a - 1)}{p_r}}}{2}, \qquad (3.23)$$

$$r = \frac{A_a + \sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}{2}, \qquad (3.24)$$

$$m_a = \frac{A_a T_a + \sqrt{A_a^2 T_a^2 + \frac{2n_a(4n_a - 1)}{p_r}}}{n_a(4n_a - 1)}.$$
(3.25)

The above expressions for the aggregate TCP rate can be summarised as,

$$r = \begin{cases} \frac{A_a + \sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}{2} & A_a \le \frac{(2n_a - 1)\sqrt{2n_a\left(\frac{1}{p_r} + B\right)} + 2n_a\sqrt{2n_aB}}{T_a} \\ \left(1 - \frac{1}{4n_a}\right)\left(A_a + \frac{\sqrt{2n_a\left(B + \frac{1}{p_r}\right)}}{T}\right) & A_a > \frac{(2n_a - 1)\sqrt{2n_a\left(\frac{1}{p_r} + B\right)} + 2n_a\sqrt{2n_aB}}{T_a} \end{cases}$$

For $n_a = 1$ this gives the same expression as in [85]. However, this deviates from that of [92] as we model flow aggregation differently. From the equations, it can be seen that the condition,

$$A_a > \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)} + 2n_a \sqrt{2n_a B}}{T_a},$$
(3.26)

leads to the case where the achieved rate is influenced by the choice of bucket size. If

$$B < \left(\frac{A_a}{n_a(4n_a - 1)}\right)^2 T_a - \frac{1}{p_r},\tag{3.27}$$

TCP cannot reach the contract rate. Equation (3.27) indicates that a higher number of flows per aggregate, lower RTT and lower contract rate can possibly compensate this.

On the other hand, when

$$A_{a} \leq \frac{(2n_{a}-1)\sqrt{2n_{a}\left(\frac{1}{p_{r}}+B\right)} + 2n_{a}\sqrt{2n_{a}B}}{T_{a}},$$
(3.28)

the achieved rate exceeds the contract rate. Let r_e denote the excess bandwidth, which is equal to

$$r_e = \frac{-A_a + \sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}{2}$$

Here we have,

$$\begin{split} \frac{\partial r_e}{\partial A_a} &= -0.5 + \frac{A_a}{2\sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}, \\ \frac{\partial r_e}{\partial n_a} &= \frac{(16n_a - 1)\sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}{p_r T_a^2}, \\ \frac{\partial r_e}{\partial T_a} &= \frac{-4n_a(4n_a - 1)\sqrt{A_a^2 + \frac{2n_a(4n_a - 1)}{p_r T_a^2}}}{p_r T_a^3} \end{split}$$

Therefore $-0.5 < \frac{\partial r_e}{\partial A_a} < 0$, $\frac{\partial r_e}{\partial n_a} > 0$, $\frac{\partial r_e}{\partial T_a} < 0$. Excess bandwidth distribution favors lower contract rate aggregates with many low delay connections. In practice a higher contract rate aggregate is expected to carry more flows and therefore may offset any disadvantage it inherits due to contract rate. Indeed, the effect of change in the number of flows is more dominant according to the above partial derivatives. Figure 3.10 illustrates the dependence of excess bandwidth distribution on contract rate, number of flows and RTT for different values of packet drop probability.

3.6.1 Multiple Packet Drops

The above analysis assumes that $1/p_r$ out-of-profile packets are transmitted between each packet drop. This basically ignores concurrent packet drops. However, in realistic network scenarios it is likely that packets belonging to multiple flows are dropped. This triggers multiple flow back-offs. We incorporate this in our model by simply increasing



Figure 3.10: The Effect of Network Parameters on TCP Excess Bandwidth

the drop in the congestion window proportional to the number of flows affected by one congestion epoch. Let h denote the number of flows affected. Therefore the steady state TCP throughput for the first congestion window behavior considered above, which fails to reach contract rates and is the most likely to experience concurrent packet drops due to its large congestion window, is equal to

$$r = \left(1 - \frac{h}{4n}\right) \left(A_a + \frac{\sqrt{2n_a \left(B + \frac{1}{p_r}\right)}}{T}\right).$$

This is true for contract rates given by,

$$A_a > \frac{(2n_a - h)\sqrt{2n_a\left(\frac{1}{p_r} + B\right)} + 2n_a\sqrt{2n_aB}}{T_ah}.$$

3.7 Transient Behavior

We use our deterministic model developed in the previous section to study TCP transient behavior. For simplicity we confine our study to the congestion window behaviors in which the TCP rate exceeds the contract rate. From equations (3.14),(3.15) we get

$$(2n_a\check{w}_{k+1} + W_a)^2 - (2n_a - 1)^2\check{w}_k^2 = (2n_a - 1)^2 \frac{2n_a}{p_r}.$$

Considering small perturbations in p_r , \check{w}_k and \check{w}_{k+1} from the steady state condition, we have,

$$\delta \check{w}_{k+1} = \frac{(2n_a - 1)^2 \check{w}_a}{2n_a (2n_a \check{w}_a + W_a)} \delta \check{w}_k - \frac{(2n_a - 1)^2}{2p_r^2 (2n_a \check{w}_a + W_a)} \delta p_r.$$
(3.29)

This is a first-order discrete-time system with a pole in the z-plane at

$$z_0 = \frac{(2n_a - 1)^2 \check{w}_a}{2n_a(2n_a\check{w} + W_a)}.$$

Substituting for \check{w}_a using (3.21) and simplifying, we get

$$z_{0} = \frac{-2n_{a}(2n_{a}-1) + (2n_{a}-1)^{2}\sqrt{1 + \frac{2n_{a}(4n_{a}-1)}{W_{a}^{2}p_{r}}}}{-2n_{a}(2n_{a}-1) + (2n_{a})^{2}\sqrt{1 + \frac{2n_{a}(4n_{a}-1)}{W_{a}^{2}p_{r}}}}$$

Mapping from the z-plane to the s-plane gives the corresponding continuous domain pole as

$$s_0 = \frac{1}{m_a T_a} \ln(z_0)$$

where m_a is given by (3.25). The time-constant, denoted by τ is

$$\tau = -\frac{1}{s_0} = -\frac{m_a T_a}{\ln(z_0)}.$$
(3.30)

For a TCP aggregate with one flow $(n_a = 1)$ without DiffServ Control $(W_a = 0)$, according to the above deterministic model we have

$$m_a = \sqrt{\frac{2}{3p_r}} = \frac{2}{3}w_a,$$

$$\tau = -\frac{2}{3}w_a\frac{T_a}{\ln(1/4)} = \frac{w_aT_a}{2.08}.$$

This differs slightly from the TCP time constant, $\tau = \frac{w_a T_a}{2}$, derived in [64] using a stochastic model of TCP.

 z_0 becomes zero when

$$A_a = \frac{(2n_a - 1)}{T_a} \sqrt{\frac{2n_a}{p_r}},$$

and $\tau \to 0$. This is the critical value of A_a in the condition (3.5.3) governing the transition in the window behavior from one to two.

Mapping the discrete-time equation (3.29) to the continuous domain, we obtain the continuous domain transfer function:

$$\frac{\delta \check{w}_a(s)}{\delta p_r(s)} = \frac{\check{g}_0}{s - s_0},\tag{3.31}$$

where

$$\check{g}_0 = -\frac{s_0 n_a (2n_a - 1)}{p_r^2 \sqrt{W_a^2 + \frac{2n_a (4n_a - 1)}{p_r}}}$$

Finally, the transfer function between the mean window size, w_a , and the out-of-profile packet dropping probability, p_r , can be found from equation (3.31) using equations (3.21) and (3.23) as

$$\frac{\delta w_a(s)}{\delta p_r(s)} = \frac{g_0}{s - s_0} \tag{3.32}$$

where

$$g_0 = -\frac{\check{g}_0(4n_a - 1)\left(1 + \sqrt{1 + \frac{2n_a(4n_a - 1)}{p_r W_a^2}}\right)}{2\left(-2n_a + (2n_a - 1)\sqrt{1 + \frac{2n_a(4n_a - 1)}{p_r W_a^2}}\right)}.$$

Equation (3.32) represents the generalisation of the TCP Reno model to TCP Reno with Token Bucket rate regulation. Note that previous studies [25] have used the unmodified TCP Reno transfer function in the DiffServ environment, which may have led to incorrect parameter choices.

3.8 Simulation Studies

In this section we present ns-2 simulation studies that validate the TCP model developed in the previous section.

We use a network topology, depicted in Figure 3.11, similar to the one used in [25]. TCP aggregates feed into a congested core with service differentiation ability. Each TCP flow is running FTP [80] over TCP SACK. The start times of the flows are uniformly distributed in [0,50] sec. The RED-In-Out (RIO) queue management technique [27] provides the differentiation ability at the core. It has minthresh_{in} = 150, maxthresh_{in} = 300, minthresh_{out} = 50, maxthresh_{out} = 250, maxprobability_{in} = 0.1, and maxprobability_{out} = 0.15. We use a packet size of 500 Bytes. Each edge has a token bucket with a depth of 500 packets.



Figure 3.11: Modeling TCP Behavior: Simulation Network Topology

3.8.1 Experiment 1

In this experiment we study the effect of contract rate on the aggregate TCP rate. We consider two TCP aggregates of which one aggregate has no contract rate. It emulates background traffic. We vary the contract rate of the DiffServ controlled TCP aggregate. Each aggregate consists of 30 flows. The propagation delays of access links are all uniform in the range [15-25] ms. For each value of the contract rate we select the core link capacity to provide 20 Mbps of excess bandwidth for background traffic. This minimizes any change in the packet drop probability at the congested core as the contract rate of the DiffServ controlled TCP aggregate is varied. Simulation results, average values computed over 10 iterations, are presented in Figure 3.12. The inability of TCP to reach contract rates is clearly evident. It fairly accurately predicts the TCP rate obtained through simulations, in particular for contract rates where the TCP rate exceeds the contract rate. For large values of the contract rate the simulation results follow increasing



Figure 3.12: Model predicted aggregate TCP Rate for Different Contract Rates

number of concurrent packet drops. This is expected. As the contract rate increases, the congestion window increases. This has the effect of more packet transmissions through the congested core for the same level of feedback delay, which is likely to trigger multiple packet drops.

3.8.2 Experiment 2

This studies the effect of number of flows per aggregate. We vary the number of flows of the TCP aggregate which is DiffServ controlled. Simulation results, average values computed over 10 iterations, are presented in Figure 3.13. As the model predicts, TCP fails to reach contract rates as the number of flows per aggregate decreases. Simulation results show a dip in the TCP throughput compared to model predictions for some values. Instability of RED Queue Management is a main reason, as these particular values correspond to increased oscillations of the instantaneous queue at the congested



Figure 3.13: Aggregate TCP Rate for Different Numbers of Flows per Aggregate

router.

3.8.3 Experiment 3

In this simulation study we consider three DiffServ controlled TCP aggregates. Unless otherwise specified each aggregate has a contract rate equal to 8 Mbps, and carries 30 TCP flows. The access links have a delay of 15 msec. We study the change in the rate of packet transmission as network parameters of the aggregates are changed. We perform four experiments each with a different set of aggregates. We plot the one second average rate of packet transmission seen at each edge. Simulation results are in Figure 3.14. According to the model token loss is absent for the chosen network parameters. We calculate p_r , assuming a fully utilized core link:

$$\sum_{i=1}^{3} \frac{A_i + \sqrt{A_i^2 + \frac{2n_i(4n_i - 1)}{p_r T_i^2}}}{2} = C$$

and compute the rate of packet transmission at each edge according to,

$$r_i = \frac{A_i + \sqrt{A_i^2 + \frac{2n_i(4n_i - 1)}{p_r T_i^2}}}{2}$$

First we set the contract rate of each aggregate such that, $A_1=4$ Mbps, $A_2=8$ Mbps, $A_3=12$ Mbps. As predicted from the model, the lowest contract rate aggregate receives the largest share of excess bandwidth when all the aggregates have the same number of flows and the model accurately predicts the actual rate of packet transmission of each aggregate. Next we change the number of flows of each aggregate such that $N_1=45$, $N_2=30, N_3=15$. As expected the aggregate with the largest number of flows grabs the largest share of excess bandwidth. Now we change the access links' delay. Again the model accurately predicts the rates of packet transmission. Previous studies, which did not account for the presence of multiple flows per aggregate, have reported the bias of excess bandwidth distribution as being toward lower contract rate aggregates. This has created the presumption that the highest contract rate aggregate receives the smallest share of excess bandwidth regardless of the number of flows it carries. As we pointed out earlier an increase in contract rate is usually accompanied by an increased number of flows sharing that aggregate. Finally we consider this particular scenario. The contract rates of the aggregates are chosen proportional to the number of flows. We have $A_1=12$ Mbps, $A_2=8$ Mbps, $A_3=4$ Mbps, $N_1=45$, $N_2=30$, and $N_3=15$. As our model predicts, defying the common belief, the first aggregate receives the largest share of excess bandwidth despite having the largest contract rate. The effect of the change in number of flows dominates.



Figure 3.14: Aggregate TCP Rate for Different Network Parameters

Chapter 4

Improving TCP Behavior in a DiffServ Network

4.1 Related Work

Early network traffic measurement research [23] showed that TCP was the dominant protocol on the Internet in the early 1990's. Several recent and popular Internet applications, such as multimedia streaming, IP telephony, and multicast, rely predominantly on the User Datagram Protocol (UDP) rather than TCP, and may gradually shift the balance of traffic away from TCP. However, the measurements presented in [95] suggest that TCP is still the dominant traffic force on the Internet, and is likely to remain so for the foreseeable future. The primary reason is the advent of the World Wide Web: the growing number of Internet users, the widespread availability of easy-to-use Web browsers, and the proliferation of Web sites with rich multimedia content combine to contribute to the exponential growth of Internet TCP traffic. Web caching and content distribution networks help to soften this impact, but the overall growth is still dramatic. Given this widespread deployment of TCP, the inability of DiffServ controlled TCP to reach contract rates in realistic network conditions [85, 102, 14, 92, 13] is an impediment for successful deployment of DiffServ. This has motivated several studies [101, 94, 25].

[101] consider modifying (a) the dropping policies at the core router, (b) the marking strategies at the meter and (c) the transport protocol at the sender. They propose modifying the core router packet drop probability to be inversely proportional to the contract rate. The packet drop probability is calculated as

$$p = k/(mk + r_i/r_{min})$$

where k, m and r_{min} are suitably chosen constants. r_{min} is the smallest contract rate. mis chosen based on the target drop probability for a flow with zero reservation. Similarly, the parameter k is chosen based on the target drop probability required for the flow with r_{min} reservation. The DiffServ architecture does not associate any packet with a specific flow or aggregate inside the network core. Moreover, core routers are unaware of each aggregate's contract rate. Therefore, this modification requires changes to the DiffServ architecture. It can also potentially impair DiffServ scalability properties. At the meter they propose a three drop precedence packet marking much like the TRTCM marker proposed in [45]. Apart from the extra burden of tuning new parameters, it is also largely dependent on the performance of multi level AQMs of core routers. It is extremely difficult to tune RED, the AQM most DiffServ core routers deploy, or any other AQM technique to operate without any considerable fluctuations in the queue length. RED invariably exhibits oscillations and that renders a three drop precedence ineffective. They also propose to modify the sender to react differently depending on the lost packet's level of conformance. Within the DiffServ architecture there is no feedback mechanism for the sender to infer the level of conformance its packets receive. Therefore, this modification demands changes at the DiffServ architectural level similar to their proposed changes in the core routers.

Recently, [25] introduced an Active Rate Management (ARM) mechanism. The basic idea is that the edge routers maintain ARMs which are responsible for adaptively setting token bucket rates in order to achieve contract rates in the face of changing network parameters. This is achieved through a feedback structure around a token bucket. The aim of ARM is to regulate the token bucket rate such that aggregate rates converge to the contract rates. ARM compares the aggregate input rate to its contract rate. Though with ARM throughputs converge to contract rates in an exact-provisioned network, in an over-provisioned network the need to exceed contract rates creates a dilemma, namely a persistent non-zero control loop error at the desired network equilibrium. To overcome this drawback, [25] complicates the simple feedback structure such that some of the ARMs deactivate and rely on the native TCP congestion control protocol to regulate the throughput in excess of the contract rate. As most networks would be over-provisioned due to admission control actions, this would be a common occurrence. Ironically this change to make ARM feasible in an over-provisioned network introduces adverse complications. The ARMs that remain active in an over-provisioned network have their rates locked at the contract rates while the deactivated ARMs grab the excess bandwidth. This disparity in excess bandwidth distribution is not seen with the classical token bucket markers. Furthermore, inactive ARMs mark all packets as out-of-profile regardless of their contract rates. Though other ARMs continue marking packets as in-profile, they operate at below the contract rate. Moreover, the information a marked packet carries may not only be used for rate regulation in a DiffServ network. For example, it may also be used to determine the mark a packet carries once it enters a neighboring DiffServ domain, i.e. domains need to trust each other. It could also be used to give in-profile packets other preferential treatments like low latency queuing. Therefore the loss of this information greatly limits DiffServ functionality. Deployment of ARM also requires major changes in the network core as it requires core routers to do ECN marking instead of dropping packets to signal network congestion. As a consequence, end nodes need to be ECN capable. As the aggregates rate of packet arrivals is compared to contract rate in the controller, any subsequent packet drops inside the network core over-estimate actual rate of packet transmissions and can possibly prevent TCP aggregates from reaching their contract rates. In a traditional DiffServ network core out-of-profile packets are dropped before any in-profile packets are marked or dropped. Otherwise, for example in a correctly provisioned network out-of-profile packet transmissions may use the network bandwidth large enough only to accommodate in-profile packets generated at the contract rate.

Another proposal aimed at solving TCP issues in a DiffServ network is TB-REM [94]. It modifies the token bucket such that it proactively signals a depleting token bucket by marking packets out-of-profile before the token bucket becomes completely empty. Basically it avoids too many flows simultaneously responding to network congestion, conceptually similar to RED functionality. In fact this kind of behavior is expected from an idealized core router, so TB-REM can be thought of as aiding core router functionality. Our analysis in the previous chapter which assumed an idealized core router established the failure of TCP flow aggregates to reach contract rates. Therefore a mechanism that just aids core router functionality simply cannot prevent TCP flows falling short of contract rates. The marking of packets with a non-empty token bucket can actually increase the likelihood of a token bucket overflow, which is precisely what should be avoided. For example a half-full token bucket only takes half the time to overflow for the same drop in the congestion window as compared to an empty token bucket.

4.2 Our Contributions

None of the techniques proposed so far provides an effective solution that aligns with the DiffServ architecture. We propose two algorithms that are scalable and effective. More importantly they can be incrementally deployed without any changes to the DiffServ architecture. Our contributions are as follows;

• We investigate the benefits of using a packet queue at the token bucket. According to our analysis in Chapter 3 the required size of the token bucket grows exponen-

tially with the contract rate. We show that a packet queue needs to be only linearly proportional to the contract rate to prevent TCP flow aggregates falling short of contract rates.

• We propose improvements to ARM. We show that the ARM's performance can be drastically improved by comparing the rate of only in-profile packet transmissions to the contract rate as opposed to using the total rate of packet transmissions. This modification also simplifies network dynamics. It allows us to develop a network model in which standard techniques are applied for choosing optimal Proportional Integral (PI) controller parameters of the feedback controller.

In the next section, we introduce our first algorithm, Token Bucket with Queue (TBQ). Its analysis is given in section 4.3.1. Section 4.3.2 proposes an improved version of TBQ. Simulation studies that compare TBQ to classical token bucket are presented in section 4.3.3. An improved version of ARM, termed Continuous Active Rate Management (CARM), is detailed in section 4.4 followed by its associated simulation studies.

4.3 Token Bucket and a Queue

Our analysis in Chapter 3 reveals that TCP flow aggregates fail to reach contract rates when tokens are lost and any subsequent out-of-profile packet transmissions fail to compensate for the lost tokens. As the rate of packet transmissions drop in response to a congestion event the token buckets are likely to overwhelm with excess tokens leading to an overflow. Our proposed mechanism tries to avoid this by inflating the congestion window over its normal equilibrium value. To achieve this we use a finite sized packet queue at the token bucket that holds packets arriving at an empty bucket. In the classical token bucket marker, for example the SRTCM, when a packet arrives at an empty bucket, the arriving packet is marked out-of-profile. That behavior in our scheme is changed such that the packet is instead held in a queue. Packets are marked out-of-profile only if an arriving packet encounters a full queue. The arriving packet is held in the queue by releasing, marked out-of-profile, the packet at the head of the queue. Otherwise, packets in the queue are released, marked in-profile as tokens become available. While the queue is being filled with packets, no out-of-profile packets are generated. Therefore the contract window size is equal to the congestion window size during this period. However, once the queue reaches its capacity and as each arriving packet dequeues the packet at the head of the queue, packets are drained from the queue faster and as a result decreases the RTT. This in turn decreases the contract window size. This delayed generation of out-of-profile packets effectively inflates the congestion window. As a result the congestion window in response to a congestion event does not drop as much as without TBQ. This prevents the possibility of a token bucket overflow. Our algorithm improves TCP performance at the expense of an increase in the RTT experienced by some packets. Such an impact on latency is not significant for the type of traffic relying on AF PHB. For this type of traffic the ability to reach contract rates is much more important. In fact the increase in latency can potentially be used to the advantage for TCP. Within the DiffServ architecture a sender is unaware of the marked profile of its packets. The increase in latency effected by TBQ can potentially be used to infer a particular flow's packets exceeding contract rates. Many service providers offer capped data rates. TBQ can also be used very effectively in this scenario. When used in that context, each arriving packet at an empty token bucket and a full queue is simply dropped. With TBQ, TCP flows can maintain a rate close to the allowed maximum rate. Moreover, the increase in queuing delay can also be used as a congestion signal. A pseudo code representation of TBQ is given in Algorithm 4.3.1.

Algorithm 4.3.1: $TBQ(A, B_T, B_P)$

comment: At the arrival of packet k

```
if (Queue is empty)
```

$ ext{then} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	$\mathbf{if} (\text{tokens} > \text{packet size})$	
	then $\left\{ Mark \text{ the packet in-profile and release.} \right.$	
	else	
	then $\left\{ \text{Hold the packet.} \right.$	
else if (Queue is not full)		
$ ext{then} \prec$	Hold the packet.	
else		
$ ext{then}$	Mark the packet at the head of	
	the queue out-of-profile and release.	
	Hold the arriving packet.	

while (Queue is not empty)

$then \left\{ \right.$	A timer is pending. At the expiration if tokens generated
	exceed the size of the packet at the head of the queue,
	mark it in-profile and release.

4.3.1 Network Model and Analysis

We adopt a very similar network model as used for modeling TCP behavior in a DiffServ network in Chapter 3.

We consider an over-provisioned DiffServ network with single rate two color token

buckets at the edge and a two drop precedence core. Figure 4.1 depicts a TCP renewal cycle at steady state with TBQ. Let m_a denote the number of RTTs for this TCP renewal cycle. The total congestion window size of aggregate a is denoted by the variable $w_{a,i}$, where $i \in [0, m_a]$. We call $W_{a,i}(=A_a T_{a,i})$ the contract window size of the ath aggregate, where A_a is the contract rate and $T_{a,i}$ the round-trip-time (RTT) of flows belonging to that aggregate. Unlike the analysis in section 3.4, $T_{a,i}$ is no longer considered a constant. Let T_a denote the component of RTT assumed to be constant that excludes the increase in RTT introduced by delayed packet transmissions in TBQ. Let $W_a = A_a T_a$. \check{w}_a and \hat{w}_a denotes the deviation of $w_{a,i}$ from W_a at the beginning and end of each cycle. n_a denote the number of flows of the ath aggregate and p_g and p_r denote, respectively, the in-profile and out-of-profile packet dropping probabilities at the core router. Token bucket depth is equal to B. TBQ is capable of holding up to B_P packets. We consider TCP steady state behavior for

$$A_a > \frac{(2n_a - 1)\sqrt{2n_a \left(\frac{1}{p_r} + B\right)} + 2n_a \sqrt{2n_a B}}{T_a},$$

in which TCP flows fail to reach contract rates. To simplify the analysis we make the following further assumptions as in section 3.4 of Chapter 3.

- Flows of each aggregate are TCP. We adopt an idealized TCP congestion avoidance behavior. Each flow simply increases the congestion window by one per RTT in the absence of any packet loss and halves the congestion window in response to a packet loss, without invoking slow start or fast retransmit/recovery mechanisms.
- 2. All flows experience the same RTT ($=T_a$). Therefore the increment in the total congestion window per RTT of an aggregate is n_a .
- 3. The core router has non-overlapping packet dropping curves for green and red packets. This implies that $p_g = 0$ and $p_r \ge 0$ as the network is over-provisioned. We also assume that p_r does not change over time.



Figure 4.1: The Aggregate TCP Congestion Window

- 4. Each aggregate gets through a total of $1/p_r$ of red packets before experiencing a packet loss. This is actually the mean number of red packet transmissions between consecutive packet losses [85].
- 5. $w_{a,i}$ is shared equally among flows within that aggregate. This assumption simplifies calculation of the reduction in $w_{a,i}$ in response to a packet loss.

To simplify the analysis the TCP renewal cycle is partitioned as shown in Figure 4.1. We have $w_{a,i\in I_1} \leq W_a$ and as a result the token bucket generates more tokens than packet arrivals and the token bucket is filled with excess tokens. We have $w_{a,i\in I_2} > W_a$. However, the queue remains empty as tokens accumulated previously continue marking packets in-profile. For $i \in I_3$, packets are enqueued as some arriving packets see an empty token bucket. We have $T_{a,i\in I_3} \leq T_a + B_P/A_a$ and $W_{a,i\in I_3} = w_{a,i\in I_3}$. Once the queue reaches its capacity each arriving packet triggers a dequeue. We have

$$w_{a,i\in I_4} \ge A_a T_a + B_P.$$

If $B_P < \sqrt{2n_a B}$, the token bucket has enough excess tokens to continue generating in-

profile packets past $w_{a,i} = A_a T_a + B_P$ and as a result, delays the queue from reaching its capacity. The queue is drained at a rate faster than the token generation rate when packets at the head of the queue are released and marked out of profile, in order to accommodate packets arriving at an empty token bucket. Indeed, it drains at the packet arrival rate. Let r denote the rate at which packets are drained from the queue. Since the maximum window size is $W_a + \hat{w}_a$, and the round trip time is bounded below by T_a we have

$$r < \frac{\hat{w}_a + W_a}{T_a}.\tag{4.1}$$

We also have

 $\check{w}_a < 0.$

This requires, from Equation (3.4),

$$\frac{1}{2n_a} (W_a + \hat{w}_a) > \hat{w}_a,
\hat{w}_a < \frac{W_a}{2n_a - 1}.$$
(4.2)

From equations (4.1) and (4.2) we have that

$$r < \frac{2n_a}{2n_a - 1}A_a.$$

With the upper bound of r derived above, we have

$$\begin{array}{lll} T_{a,i\in I_4} &> & T_a + \frac{(2n_a - 1)B_P}{2n_a A_a}, \\ W_{a,i\in I_4} &> & A_a T_a + \frac{(2n_a - 1)B_P}{2n_a} \end{array}$$

This can be used to derive an upper bound on the number of generated out-of-profile packets, N, as depicted in Figure 4.1.

$$N = \frac{\left[\frac{(\hat{w}_{a} - B_{P})}{n_{a}}\right] \left[\left(\hat{w}_{a} - \frac{(2n_{a} - 1)B_{P}}{2n_{a}}\right) + \left(B_{P} - \frac{(2n_{a} - 1)B_{P}}{2n_{a}}\right)\right]}{2}$$
$$= \frac{(\hat{w}_{a} - B_{P})\left(\hat{w}_{a} - \frac{(n_{a} - 1)B_{P}}{n_{a}}\right)}{2n_{a}}.$$
$\frac{1}{p_r}$ out-of-profile packets are generated per TCP renewal cycle. Therefore we have,

$$\frac{1}{p_r} \le \frac{\left(\hat{w}_a - B_P\right) \left(\hat{w}_a - \frac{(n_a - 1)B_P}{n_a}\right)}{2n_a}.$$

Simplifying we get,

$$\hat{w}_a \ge \frac{(2n_a - 1)}{n_a} B_P + \sqrt{\frac{B_P^2}{n_a^2} + \frac{8n_a}{p_r}}.$$
(4.3)

The number of tokens accumulated for $i \in I_1$ is equal to,

$$\frac{\check{w}_a^2}{2n_a}.$$

Specifically, if this is contained below the token bucket size, the loss of tokens is avoided. We need

$$\frac{\check{w}_a^2}{2n_a} \le B. \tag{4.4}$$

We have

$$W_{a} - \check{w}_{a} = (W_{a} + \hat{w}_{a}) \left(1 - \frac{1}{2n_{a}}\right),$$

$$\check{w}_{a} = \frac{W_{a}}{2n_{a}} - \hat{w}_{a} \left(1 - \frac{1}{2n_{a}}\right).$$
 (4.5)

From equations (4.4) and (4.5) we get,

$$\left[\frac{W_a}{2n_a} - \hat{w}_a \left(1 - \frac{1}{2n_a}\right)\right]^2 \leq 2n_a B,$$
$$\hat{w}_a \geq \frac{AT_a - \sqrt{8n^3B}}{(2n_a - 1)}.$$
(4.6)

As implied by equations (4.3) and (4.6), to prevent any token loss B_P should be chosen to satisfy

$$\frac{(2n_a-1)}{n_a}B_P + \sqrt{\frac{B_P^2}{n_a^2} + \frac{8n_a}{p_r}} \ge \frac{AT_a - \sqrt{8n^3B}}{(2n_a-1)}.$$
(4.7)

For example

$$B_P = \frac{AT_a - \sqrt{8n^3B}}{2(2n_a - 1)},\tag{4.8}$$

prevents any token loss, and as a consequence TCP flows achieve their contract rates. The dependence of B_P on A is approximately linear. Interestingly, the token bucket depth can also be made zero without materially affecting the performance. Usually the token bucket does not keep track of the number of flows per aggregate. Therefore, a more conservative choice of B_P that is invariant to the number of flows can be obtained by choosing n = 1;

$$B_P = \frac{AT_a - \sqrt{8B}}{2}$$

4.3.2 Low Delay Packet Marker

One of the drawbacks of TBQ is the imposed requirement for delayed transmission of some packets. The target traffic profile of AF PHB, mainly transactional TCP flows, does not have stringent delay requirements. It is mostly UDP flows, which form multimedia sessions that are sensitive to any increase in latency. This type of traffic relies on EF PHB. Therefore it is unlikely that the increase in queuing delay affected by TBQ adversely affects applications relying on AF PHB. Nevertheless, it is possible to further refine the marker in terms of reducing queuing delay.

From equation (4.8) it is clear that an idealized core router at the presence of many flows per aggregate significantly reduces the required size of the packet queue. The above proposed algorithm can generate bursts of out-of-profile packets. Given that it is extremely difficult to rely on the core router to realize the benefits of many flows per aggregate, we propose probabilistic packet marking much like in TB-REM to aid the core router to realize the advantage of multiple flows. We use a marking scheme very similar to that used in RED [38]. At the arrival of each packet, the packet at the head of the queue is marked out-of-profile and released with a probability determined by the queue length. For simplicity we use the instantaneous queue length rather than an exponentially averaged value as in RED. Also, we mark the DSCP rather than dropping or marking the ECN bit. With RED, every mark or drop is an indication of network congestion and signals flows to slow down. Therefore the probability of packet marking/dropping needs to be kept low. The RED curve has a discontinuity, at which the marking probability jumps to one from a fairly small value. The queue stabilizes around a point away from this discontinuity. In our scheme, marking the packet out-of-profile only increases the likelihood of a flow rate reduction when the network is congested. Thus we choose a scheme in which the marking probability, beyond a threshold called *MinThresh*, increases linearly all the way from zero to one as the queue reaches capacity. When the queue length is below *MinThresh*, an arriving packet does not trigger marking out-of-profile the packet at the head of the queue. One of the most important and influential parameters is the *MinThresh*. On one hand, a small threshold decreases the average queue length at the marker and cuts down delay but, on the other hand, it is an indication of many flows and therefore has the risk of overestimating the number of flows, which usually continues varying. Its influence in RED is also critical as it trades off delay with link utilization. More generally the parameter target queue length, in other AQMs such as REM [5], PI [47] has a similar effect. Interestingly, studies on the choice of this critical parameter in different contexts are quite limited. The presence of different varieties of congestion avoidance schemes as well as the increased number of short-lived flows hinder such an investigation. A pseudo code of this low delay marker is presented in algorithm 4.3.2.

It is the presence of multiple flows that made possible this low delay variant. That dependence makes it less robust. However if the number of flows can be estimated, this weakness can be eliminated by an adaptive marker, which adjusts the minimum threshold as the number of flows change.

4.3.3 Simulation Studies - TBQ

In this section we present ns-2 simulation studies that compare TBQ to the classical token bucket. The network topology is shown in Figure 4.2. TCP aggregates feed into a congested core with service differentiation ability. Each TCP flow is running FTP over Algorithm 4.3.2: LOW DELAY TBQ $(A, B_T, B_P, MinThresh)$

comment: At the arrival of packet kif (Queue is empty) \mathbf{f} (tokens > packet size) then $\begin{cases} \text{If (tokens > packet size)} \\ \text{then } \begin{cases} \text{Mark the packet in-profile and release.} \\ \text{else} \\ \text{then } \end{cases} \\ \text{Hold the packet.} \end{cases}$ else if (Queue length is less than MinThreshold) then $\left\{ \text{Hold the packet.} \right.$ else if (Queue is not full) compute packet marking probability p. if (Uniform[0, 1] < p)then $\begin{cases} \text{if } (\text{Uniform}_{[0, 1] \ \sim P}) \\ \text{Mark the packet at the head of} \\ \text{then} \\ \begin{cases} \text{Mark the packet at the head of} \\ \text{the queue out-of-profile and release.} \\ \text{Hold the arriving packet.} \\ \text{else} \\ \text{then} \\ \end{cases} \\ \text{Hold the packet.} \end{cases}$ else $\label{eq:market} {\rm the \ packet \ at \ the \ head \ of} \\ {\rm the \ queue \ out-of-profile \ and \ release.} }$ Hold the arriving packet.

while (Queue is not empty)

then <	A timer is pending.
	At the expiration if tokens generated
	exceed the size of the packet at the head of the queue,
	mark it in-profile and release.



Figure 4.2: TBQ Performance: Simulation Network Topology

TCP SACK. The start times of the flows are uniformly distributed in [0,50] sec. The RIO queue management technique [27] provides the differentiation ability at the core. It has minthresh_{in} = 150, maxthresh_{in} = 300, minthresh_{out} = 50, maxthresh_{out} = 250, maxprobability_{in} = 0.1, and maxprobability_{out} = 0.15. We used a packet size of 500 Bytes. Each edge router has a token bucket marker with a depth of 50 packets. TBQ uses a token bucket with a depth of 20 packets and a 30 packets long packet queue.

Experiment 1

In the first experiment we compare the performance of TBQ and the token bucket for different contract rates. We consider two TCP aggregates of which one aggregate has no contract rate. It emulates background traffic. We vary the contract rate of the DiffServ controlled TCP aggregate. Each aggregate consists of 30 flows. The propagation delays of access links T_{pi} are all uniform in the range [15-25] ms. For each value of the contract rate we select the core link capacity to provide 20 Mbps of excess bandwidth for background



Figure 4.3: TBQ Performance for Different Values of A.

traffic. This minimizes any change in the packet drop probability at the congested core as the contract rate of the DiffServ controlled TCP aggregate is varied. Simulation results are presented in Figure 4.3. The Figure clearly shows the marked improvement the packet queue of TBQ generates.

The remainder of the simulation studies have three TCP aggregates with non-zero contract rates. The propagation delays T_{pi} are all uniform in the ranges: $T_{p1} \in [50 - 90]$ msec, $T_{p2} \in [15 - 25]$ msec and $T_{p3} \in [0 - 10]$ msec. Each sender consists of N_i FTP flows, all starting uniformly in [0, 50] sec, with $N_1 = 20, N_2 = 30$ and $N_3 = 25$. The edge routers have contract rates equal to 8 Mbps, 2 Mbps and 5 Mbps. For TBQ we use 64, 16 and 40 packets long queues, proportional to their contract rates. The token bucket depth is chosen such that the total of packet queue length and the token bucket depth is 50 packets. The classical token bucket depth is 50 packets. The parameter settings remain fixed in all experiments.



Figure 4.4: TBQ Performance in an Exact-Provisioned Network

Experiment 2

In this experiment we compare the dynamics of TBQ and the classical token bucket for an exact-provisioned network, i.e the core link capacity is 15 Mbps. Figure 4.4 presents simulation results. With just the token bucket the TCP aggregate with the highest contract rate fails to reach its contract rate. On the other hand its rate is very close to contract rate with TBQ.



Figure 4.5: TBQ Performance in a 20% Over-Provisioned Network

Experiment 3

We repeat the same experiment as above except for an increase of 20% in the core router egress capacity making the network over-provisioned. The simulation results are presented in Figure 4.5. Again with the token bucket the TCP aggregate with the highest contract rate fails to reach its contract rate while with TBQ it exceeds its contract rate.

Experiment 4

We now consider an under-provisioned network. The experimental setup is identical to Experiment 1 except for a 20% decrease in the core router egress capacity. Simulation



Figure 4.6: TBQ Performance in a 20% Under-Provisioned Network

results are presented in Figure 4.6. Both schemes, TBQ and the classical token bucket perform similarly.

Experiment 5

In this experiment we evaluate the performance impact of background traffic. Short-lived TCP sessions with random size data transfers, Pareto distributed with a shape of 1.5 and a mean of 500 Kbytes, traverse through the congested core. The starting times of these sessions are exponentially distributed with a 1 second average time between arrivals. These flows have round trip propagation delays uniformly distributed in [70,90] msec.



Figure 4.7: TBQ Performance in an Exact-Provisioned Network with Background Traffic

Simulation results are in Figure 4.7. Since the network is exact-provisioned, background traffic should be blocked. Both schemes are successful in driving the throughput of background flows to zero. However TBQ is more responsive.

Experiment 6

This experiment is similar to the previous experiment except for a 20% increase in the core link capacity. The background traffic should receive some share of bandwidth. Simulation results are presented in Figure 4.8. Both schemes perform similarly, i.e. they allow background traffic to share excess bandwidth.



Figure 4.8: TBQ Performance in a 20% Over-Provisioned Network with Background Traffic

4.4 Continuous Active Rate Management

The purpose of ARM is to regulate the token bucket rate such that aggregate rates converge to the contract rates. The following equations give a complete description of ARM at the ith edge:

$$\frac{d}{dt}x_{avg,i} = -kx_{avg,i} + k\widetilde{x}_i, \qquad (4.9)$$

$$\frac{a}{dt}\zeta_i = \max\left[\underline{x} - x_{avg,i}, 0\right], \qquad (4.10)$$

$$\xi_i = k_{Ii}\zeta_i + k_{pi}\left(\underline{x} - x_{avg,i}\right). \tag{4.11}$$

 ξ denotes the token rate, \underline{x} denotes the contract rate and \tilde{x} denotes an estimate of the aggregate rate computed by counting the total number of sent packets in a fixed period divided by that period. This estimate is passed through a low-pass filter with time constant 1/k to produce a smooth rate-estimate x_{avg} . This estimate is the input to the proportional-integral part of ARM.

We propose a feedback structure around a token bucket similar to that of ARM, but using a different error measure. Specifically, it compares the rate of only the in-profile packets to the contract rate. This simple change makes ARM behave as a perfect token bucket marker, i.e. it marks in-profile packets at precisely the contract rate. This is an improvement over the classical token bucket marker with TCP flows. Though the latter generates tokens at the contract rate, due to the complexities of TCP congestion control, many tokens are wasted. Therefore the network sees in-profile packets at below contract rates. The marking of in-profile packets at the contract rate does not disturb the network equilibrium of an over-provisioned network. Indeed it allows TCP aggregates to exceed contract rates in an over-provisioned network. Importantly, the information a marked packet carries can be used for purposes other than rate regulation. We call this mechanism Continuous Active Rate Management (CARM) due to the absence of deactivation, in contrast to ARM. The following equations give a complete description of CARM at the ith edge:

$$\frac{d}{dt}x_{avg,i} = -kx_{avg,i} + k\breve{x}_i, \qquad (4.12)$$

$$\frac{d}{dt}\zeta_i = (\underline{x} - x_{avg,i}), \qquad (4.13)$$

$$\xi_i = k_{Ii}\zeta_i + k_{pi}\left(\underline{x} - x_{avg,i}\right). \tag{4.14}$$

where \breve{x}_i denotes an estimate of the aggregate in-profile packet rate computed by counting the total number of sent in-profile packets in a fixed period divided by that period. Similar to ARM, this estimate is passed through a low-pass filter with time constant 1/kto produce a smooth rate-estimate $x_{avg,i}$ which becomes the input to the proportionalintegral part of the CARM. Because with the classical token bucket, the actual TCP throughput is less than the token rate (due to TCP congestion control action), what is needed is a token rate that is sufficiently higher than the contract rate so that the TCP throughput becomes equal to the contract rate. The required higher rate may be achieved by integral control action, equation (4.13), which produces a token rate that is a weighted integral of the difference (error) between the contract rate and the in-profile (green) TCP packet throughput. Adding a term that is proportional to the error, as done in equation (4.14), yields proportional-integral (PI) [4] control which is known from control theory to be more stable than pure integral control. PI control action is also present in (4.11) but with an error measure that results in deactivation of any control loop where the aggregate TCP throughput exceeds the contract rate, as seen in equation (4.10). Thus CARM may be viewed as an adaptive version of the classical token bucket with a token rate that automatically adjusts to the rate required to make the in-profile TCP packet throughput equal to the contract rate. In ARM, however, the difference between the contract rate and the sum of both in-profile and out-of-profile TCP packet throughputs is integrated, which achieves a different outcome from the goal of the classical token bucket.

We present an analytical design of the PI controller employed in CARM. First we model the TCP aggregate using our DiffServ controlled TCP model in chapter 3. We use



Figure 4.9: The Aggregate TCP Congestion Window.

that to design the PI controller analytically.

4.4.1 Network Model

We use the same network model and notation as in section 4.3.1. We again consider the steady state TCP behavior for

$$A_a > \frac{(2n_a - 1)\sqrt{2n_a\left(\frac{1}{p_r} + B\right)} + 2n_a\sqrt{2n_aB}}{T_a},$$

in which TCP flows fail to reach contract rates. Figure 4.9 depicts the aggregate TCP congestion window. Once the token bucket starts marking packets out-of-profile, $1/p_r$ of them are transmitted before the first packet gets dropped at the congested core router. Therefore we have

$$\begin{aligned} \frac{\hat{w}_a^2}{2n_a} &= B + 1/p_r, \\ \hat{w}_a &= \sqrt{2n_a(B + 1/p_r)}. \end{aligned}$$

When a packet is lost, the congestion window of the corresponding flow is halved. Therefore with assumption (5), the aggregate TCP congestion window is reduced by $\hat{w}/2n_a$ and we have,

$$\dot{w}_{a} = \frac{W_{a}}{2n_{a}} + \hat{w}_{a} \left(1 - \frac{1}{2n_{a}}\right) \\
= -\frac{W_{a}}{2n_{a}} + \left(1 - \frac{1}{2n_{a}}\right) \sqrt{2n_{a}(B + 1/p_{r})}.$$

If $\check{w}^2 > 2n_a B$, the token bucket cannot accommodate all of the excess tokens and some tokens are dropped. The required size of the token bucket, which prevents any token loss, grows approximately exponential with the aggregate window size. On the other hand the token bucket size should be chosen small to prevent any bursts of in-profile packets that could destabilize the network. Therefore token loss is common in realistic network scenarios. Let *C* denote the number of lost tokens. We have

$$C = \frac{\check{w}_{a}^{2}}{2n_{a}} - B,$$

= $\frac{\left(W_{a} - (2n_{a} - 1)\sqrt{2n_{a}(B + 1/p_{r})}\right)^{2}}{8n_{a}^{3}} - B.$

The rate of in-profile (green) packets transmission, r_G , averaged over a TCP congestion window cycle is equal to

$$r_G = A_a - \frac{n_a C}{(\hat{w} - \check{w})T}.$$

To simplify the calculations, we assume that $1/p_r$ is negligible compared to B, i.e. the network is almost exact-provisioned. Therefore we have

$$r_G = A_a - \frac{\left(W_a - (2n_a - 1)\sqrt{2n_aB}\right)^2 - 8n_a^3B}{4n_a T (W_a + \sqrt{2n_aB})},$$
(4.15)

Taking small deviations, the above simplifies to

$$\delta r_G = \left(1 - \frac{1}{4n_i}\right) \delta A_i. \tag{4.16}$$

On the other hand, if $\check{w} \geq W_a$ or $\check{w} < W_a$ but $\frac{(W_a - \check{w})^2}{2n_i} < B$ no tokens are lost and we have

 $r_G = A_i.$



Figure 4.10: CARM: Feed Back Control System.

4.4.2 Controller Design

As the rate is computed by counting the number of sent packets over a fixed time period, T_{TSW} , and smoothed by a low pass filter, equation (4.12), the s-domain representation of the rate estimator is:

$$F(s) = \frac{\hat{r}_G(s)}{r_G(s)} = \frac{\rho}{s+\rho} e^{-sT_{TSW}},$$

where $T_{TSW} \gg T_a$ and $\rho \ll \frac{1}{T_a}$. From the system model derived in the above section we have

$$G(s) = \frac{r_G(s)}{r_T(s)} = \left(1 - \frac{1}{4n_a}\right).$$

 r_T denotes the rate of token generation. Therefore, the complete plant dynamics can be represented as

$$\frac{\hat{r}_G(s)}{r_T(s)} = \left(1 - \frac{1}{4n_a}\right)\frac{\rho}{s+\rho}e^{-sT_{TSW}}$$

The s-domain representation of the the PI controller is

$$C(s) = \frac{r_T(s)}{e(s)} = K_C \left(1 + \frac{1}{T_I s}\right).$$

Figure 4.10 is a representative block diagram of the complete feed back control system. Several techniques are available for tuning a PI controller. We compute K_C , T_I of the PI controller using the Ziegler-Nichols design rules [103], which are known to be appropriate



Figure 4.11: CARM Performance: Simulation Network Topology

for the type of system transfer function at hand. To apply these design rules we need to first find analytically the K_C that makes the system unstable without integral control, i.e. $T_I \to \infty$, and record the corresponding oscillation period. Clearly the oscillation frequency is the root of the following equation in angular frequency ω ,

$$\omega T_{TSW} + \tan^{-1} \left(\frac{\omega}{\rho}\right) = \pi.$$
(4.17)

Let $\omega = \omega_0$ satisfy the above. For $\rho \ll \frac{1}{T_I}$, this can be approximated as

$$\omega T_{TSW} + \frac{\pi}{2} - \frac{\rho}{\omega} = \pi$$

This yields a quadratic equation in ω that has the positive solution

$$\omega = \frac{1}{T_{TSW}} \left(\frac{\pi}{4} + \sqrt{\frac{\pi^2}{16} + \rho T_{TSW}} \right).$$

The Ziegler-Nichols rule then gives the appropriate integral time as

$$T_{I} = \frac{1}{1.2} \frac{2\pi}{\omega_{0}},$$

= $\frac{2\pi}{1.2} \frac{T_{TSW}}{\left(\frac{\pi}{4} + \sqrt{\frac{\pi^{2}}{16} + \rho T_{TSW}}\right)}.$ (4.18)

To find the corresponding appropriate value of K_C , we need to determine the value K_u of K_C that makes the system unstable with $T_I \to \infty$. This is obtained by setting the magnitude of

$$\left\|\frac{\left(1-\frac{1}{4n_a}\right)K_u\rho e^{-sT_{TSW}}}{1+\rho s}\right\| = 1.$$

As $s = j\omega$, this yields

$$K_u = \frac{\sqrt{1 + (\rho\omega_0)^2}}{\rho\left(1 - \frac{1}{4n_a}\right)}$$

where ω_0 is given by equation (4.17). The Ziegler-Nichols rule then gives the following value for K_C :

$$K_{C} = 0.45 K_{u},$$

= $0.45 \frac{\sqrt{1 + (\rho \omega)^{2}}}{\rho \left(1 - \frac{1}{4n_{a}}\right)}.$ (4.19)

The above value of K_C yields a system that is fast but under-damped. A less aggressive response can be obtained by adopting a smaller value of K_C . Usually $n_a \gg 1$, so a good approximation, that is invariant to the number of TCP flows, is obtained by replacing $\left(1 - \frac{1}{4n_a}\right)$ by 1. This approximation is conservative with regard to stability because it slightly decreases the controller's gain.

Finally, for practical implementation, we obtain the discrete-time versions of the above estimator and controller using Tustin's approximation, $s \leftarrow \frac{2}{h} \frac{z-1}{z+1}$. where h is the sampling interval. The token rate update becomes,

$$r_T[k] = r_T[k-1] + \Delta r_T[k]$$
(4.20)

where

$$\Delta r[k] = K_c \left(1 + \frac{h}{2T_I}\right) e[k] - K_c \left(1 - \frac{h}{2T_I}\right) e[k-1],$$

$$e[k] = A - \hat{r}_G.$$

When the network is under-provisioned, the resulting rates of green packet transmission fall below contract rates regardless of the controller. The persistent error keeps increasing the input to the controller and can possibly overshoot the system response when excess bandwidth becomes available. To prevent this, we constrain the controller output. The revised update is given in equation (4.21). This update, which is in the so-called velocity form, prevents any integral windup due to saturated system outputs.

$$r_T[k] = \min(A_a^{max}, \max(A_a^{min}, r_T[k-1] + \Delta r_T[k]))$$
(4.21)

4.4.3 Simulation Studies - CARM

In this section we present *ns-2* simulation studies that evaluate the performance of the CARM token bucket. The network topology is shown in Figure 4.11. TCP aggregates feed into a congested core with service differentiation ability. Each TCP flow is running FTP over TCP SACK. The start times of the flows are uniformly distributed in [0,50] sec. The RIO queue management technique [27] provides the differentiation ability at the core. It has minthresh_{in} = 150, maxthresh_{in} = 300, minthresh_{out} = 50, maxthresh_{out} = 250, maxprobability_{in} = 0.1, and maxprobability_{out} = 0.15. We used a packet size of 500 Bytes. Each edge router has a token bucket marker with a depth of 50 packets. Estimated rates are generated by counting the number of packets in a 1 second interval. We choose $\rho = 1$ rad/sec in the estimator. A sampling rate of 37.5 Hz is used in the discretization. We have $A^{max} = 1.25A$ and $A^{min} = 0$. ARM adopts the same parameters as in [25]

Experiment 1

In the first experiment we compare the performance of CARM and the token bucket for different contract rates. We consider two TCP aggregates of which one aggregate has no contract rate. It emulates background traffic. We vary the contract rate of the DiffServ controlled TCP aggregate. Each aggregate consists of 30 flows. The propagation delays of access links T_{pi} are all uniform in the range [15-25] ms. For each value of the contract rate we select the core link capacity to provide 20 Mbps of excess bandwidth for background traffic. This minimizes any change in the packet drop probability at the



Figure 4.12: CARM Performance for Different Values of A.

congested core as the contract rate of the DiffServ controlled TCP aggregate is varied. Simulation results are presented in Figure 4.12. It clearly shows the marked improvement CARM generates.

The rest of the simulation studies have three TCP aggregates with non-zero contract rates. The propagation delays T_{pi} are all uniform in the ranges: $T_{p1} \in [50 - 90]$ msec, $T_{p2} \in [15 - 25]$ msec and $T_{p3} \in [0 - 10]$ msec. Each sender consists of N_i FTP flows, all starting uniformly in [0, 50] sec, with $N_1 = 20$, $N_2 = 30$ and $N_3 = 25$. The edge routers have contract rates equal to 8 Mbps, 2 Mbps and 5 Mbps. The parameter settings remain fixed in all experiments.

Experiment 2

Here we compare the response in packet transmission rates for different values of α , where $K_c = \alpha K_u$. Figure 4.13 plots the packet transmission rates for $\alpha=0.45$, 0.2 and 0.05. We



Figure 4.13: CARM Performance for Different Values of K_c .

have the core link capacity equal to 15 Mbps resulting in an exact-provisioned network. A less aggressive damped response is achieved with the lowest value of $\alpha(=0.05)$.

Experiment 3

We consider an exact-provisioned network. Figure 4.14 plots the rates of total and inprofile packet transmission rates seen at each edge, averaged over 1 second time intervals. With ARM, the total rates of the aggregates slowly converge to the contract rates, but packets are marked in-profile at a reduced rate. For CARM the total rates of packet transmission seen in the figures are slightly over-estimated as we plot the rates of packet transmission seen at the edge, which includes packets that may subsequently be dropped at the congested core. However this does not affect the rate of in-profile packet transmission as these packets are not dropped in either over-provisioned or exact-provisioned networks. This is not seen with ARM; as described above it relies on ECN marking to signal congestion as compared to dropping packets. With CARM the rate of packet transmission of the aggregate, that has a contract rate of 8 Mbps, exhibits more oscillations for the exact-provisioned network as compared to the over-provisioned network. Out-of-profile packets are dropped with a probability close to one in an exact-provisioned network. Given that flows of this particular aggregate maintain very large windows, close to 50 packets, the dropping of out-of-profile packets mostly in bursts is likely to generate oscillations. Therefore this kind of behavior is expected.

Experiment 4

Experiment 4 compares packet transmission rates in a 20% over-provisioned network. Figure 4.15 presents simulation results.With ARM we clearly see excess bandwidth being accessed by just one aggregate. Moreover, aggregates mark packets at a reduced rate. In contrast, CARM lets all aggregates share the excess bandwidth and continues marking packets as in-profile at precisely the contract rate.

Experiment 5

Performance for an under-provisioned network is quite similar for the two token bucket variants. Simulation results are presented in Figure 4.16.

Experiment 6

Experiment 6 investigates the effects of introducing background traffic. Short-lived TCP sessions with random size data transfers, Pareto distributed with a shape of 1.5 and a mean of 500 Kbytes, traverse through the congested core. The starting times of these ses-



Figure 4.14: CARM Performance in an Exact-Provisioned Network.



Figure 4.15: CARM Performance in a 20% Over-Provisioned Network.



Figure 4.16: CARM Performance in a 20% Under-Provisioned Network.



Figure 4.17: CARM Performance in an Exact-Provisioned Network with Background Traffic.

sions are exponentially distributed with a 1 second average time between arrivals. These flows have round-trip times uniformly distributed in [70,90] msec. The first simulation run is for an exact-provisioned network. The rate of background traffic tends to zero as expected with both token buckets, but takes a considerably longer time with ARM. When the network is over-provisioned as presented in Figure 4.18, background traffic grabs a sizable portion of the excess bandwidth with ARM, whereas CARM distributes excess bandwidth among all the aggregates. This disparity seen in excess bandwidth distribution with ARM is a major limitation.



Figure 4.18: CARM Performance in an Over-Provisioned Network with Background Traffic.

Experiment 7

We investigate network dynamics when it transitions from an under-provisioned network to an over-provisioned network. We increase the contract rate of the second aggregate to 6 Mbps when the core link capacity remains at 15 Mbps, resulting in an under-provisioned network. At 120 sec the second aggregate stops sending any traffic. We consider two scenarios with the contract rate of the third aggregate equal to 5 Mbps and 7 Mbps. This results in over-provisioned and exact-provisioned networks, respectively, beyond 120 sec. Figure 4.19 plots the rate of in-profile and total packet transmissions averaged over 10 second intervals. The results show the ability of CARM to quickly adapt to varying overall network subscription levels with the designed controller.



Figure 4.19: CARM Performance under a Varying Network Load.

Chapter 5

Promoting Conformance to TCP

For the most part, the Internet still remains a best effort network. Despite the phenomenal growth the Internet has experienced over the years, it has been able to successfully meet the demands of most of its users. At the heart of this success is the ability to deliver service at times of extremely high demand. The key reasons for this are the congestion control mechanisms of TCP. The many flavors of the additive increase multiplicative decrease (AIMD) type of TCP algorithms at end-nodes and Tail-Drop (TD) or RED queues at links, have been the central feature of the successful Internet Congestion Control mechanisms. Recent measurements [95] reaffirm the continued dominance of TCP as a transport layer protocol. Therefore, most Internet traffic is thus congestion controlled. This is remarkable given the lack of widespread deployment of any mechanisms that provide incentives for end-nodes to be TCP conformant. However, it cannot be anticipated that this state of affairs will remain unchanged as the Internet accommodates the needs of more and more users and applications.

The packet delivery mechanisms of TCP cannot meet the demands of a range of applications, in particular, real-time applications. As a result, an increasing number of applications avoid TCP, and leave the congestion control responsibility to the application layer software. This has resulted in either limited or no congestion control mechanisms in a large number of applications. Therefore end-nodes react to congestion differently depending on the algorithm employed, and as a result achieve different bandwidths for the same level of congestion. Given the fundamental heterogeneity of the Internet, and its enormous scale, it is impossible to impose constraints directly on the end-nodes to be TCP conformant. But routers at the edge and inside of the network can deploy mechanisms that discourage and penalize end-nodes that are not conformant.

Algorithms such as CHOKe (CHOose and Keep for responsive flows and CHOose and Kill for non-responsive flows) [71], RED with Preferential Dropping (RED-PD) [60], Core-Stateless Fair Queuing (CSFQ) [91] provide such mechanisms. But as we detail later they inherently have major limitations. We propose a mechanism that is similar in computational complexity to CHOKE and RED-PD but is fairer and effective.

The rest of the chapter is structured as follows. Next we highlight our contributions. Section 5.2 reviews related work. The proposed algorithm is presented in section 5.3 followed by simulation studies in section 5.4.

5.1 Our Contributions

We make the following contributions.

- We identify limitations in current algorithms designed to protect TCP flows from congestion non-responsive flows. We show that the use of buffer occupancy as a means of detecting misbehaving flows as done in [71] can limit TCP throughput. On the other hand the use of packet drop history [60] does not form an accurate measure of bandwidth share when packets are of different sizes.
- We propose an algorithm that accurately estimates bandwidth share of flows and incorporates mechanisms that encourage conformance to the throughput of an idealized TCP flow.

5.2 Related Work

Best effort networks deploy various techniques to improve efficiency and fairness of packet delivery. Predominantly this includes AQM and Packet Scheduling algorithms. AQMs such as RED [38], REM [5] and others [56, 96, 70, 47, 68, 58, 12] have improved performance over traditional TailDrop queues. AQM help increase link utilization but lacks any per-flow bandwidth allocation mechanisms. On the other hand packet Scheduling algorithms such as Weighted Round Robin (WRR), Deficit-Weighted Round Robin (DWRR) [87], Weighted Fair Queueing (WFQ) [72, 73], Self Clocked Fair Queueing (SFQ) [30, 40], Worst Case Fair Weighted Fair Queueing (W²FQ) [15], Worst Case Fair Weighted Fair Queueing + (W²FQ⁺) [16], Start-time Fair Queueing [41], Frame-based Fair Queueing [90] and Starting Potential-based Fair Queueing [90] provide fine control of bandwidth allocation.

Queue management algorithms estimate congestion and feed that information back to end-nodes either through packet dropping or ECN. They were designed under the assumption that end nodes are cooperative, reacting to congestion by decreasing their sending rates. Hence they don't have mechanisms to avoid non-responsive flows from grabbing an unfair share of the bandwidth. These flows simply increase congestion at the link and in turn the congestion measures of these algorithms. But being non-responsive to congestion, their rates remain constant while conformant TCP nodes contract.

For example, consider a case in which both TCP conformant and non-responsive flows share a link that has a queue management scheme such as RED or REM deployed. Consider N TCP conformant end-nodes that have round trip times equal to d_s and packet size l_s , and M constant rate non-responsive sources that have sending rates equal to r_s sharing a link of capacity C. We assume that this link is the only bottleneck link in its path for all the sources and $\sum_{s=1}^{M} r_s < C$. TCP conformant nodes react to congestion that they experience along the path by adjusting their rates. We assume that for such a node, the congestion measure p_s (packet dropping probability) relates to its sending rate x_s according to

$$x_s = \frac{l_s}{d_s} \sqrt{3/2p_s}.$$
(5.1)

This can be derived by modeling TCP's congestion avoidance phase, ignoring other aspects such as slow-start and fast retransmit/fast recovery. All sources experience the same level of congestion, and hence packet dropping probability p, due to this link being the only bottleneck link in their path. Hence, at equilibrium, we have

$$\sum_{s=1}^{N} \frac{l_s}{d_s} \sqrt{3/2p} + (1-p) \sum_{s=1}^{M} r_s = C.$$
(5.2)

In summary, when TCP conformant and non-responsive flows coexist, TCP conformant nodes are left to compete for the bandwidth share unused by the non-responsive flows. As the rates of the non-responsive flows increase, the congestion measure keeps increasing in tandem. As a result, the throughputs of TCP conformant nodes go down.

Scheduling algorithms, which are computationally more complex than queue management schemes, provide a fair allocation of bandwidth among competing connections. They achieve this through flow isolation, which requires per flow state maintenance. The high computational complexity of these algorithms limit their applicability to slow speed interfaces.

Schemes such as CHOKe, RED-PD and CSFQ try to bridge the gap between simple queue management schemes and computationally complex packet scheduling algorithms.

CHOKe [71] uses buffer occupancy to detect the presence of misbehaving flows and penalize them. However buffer occupancies do not necessarily reflect the true bandwidth share of connections. The sending rates of TCP connections with large window sizes exhibit large variances. This shows up as a flow buffer occupancy with a commensurately large variance. When global synchronization effects are no longer present, it is possible, at a given moment, for a TCP conformant flow to have a large buffer occupancy while other connections account for only a small fraction of the buffer. The bursty nature of Internet traffic further aggravates this situation. This disproportionate buffer occupancy can trigger false detections, and, as a result, conformant TCP nodes may back-off unnecessarily. The mechanisms of TCP are such that the reaction to packet loss is drastic, leaving TCP nodes with only a small bandwidth share under CHOKE. Using a deterministic model of TCP, we shall illustrate this in more detail.

In CHOKe, when a packet arrives at a congested router, it draws a packet at random from the FIFO (First In First Out) buffer and compares it with the arriving packet. If they both belong to the same flow, then they are both dropped; else the randomly chosen packet is left intact and the arriving packet is admitted into the buffer with a probability that is computed exactly as in RED. In [93] it is shown that CHOKe can bound the bandwidth share of a single non-responsive flow regardless of its arrival rate under some conditions. However, as we explain below, CHOKe in doing so overly restricts the bandwidth share of conformant TCP flows. When buffers are not large, it makes TCP flows operate in a very low window regime where timeouts are frequent. We consider a TCP conformant node that shares a one-way congested link operating CHOKe. We make a few assumptions. We assume that the links' propagation delays are negligible compared with the queuing delays at the links. This allows us to assume that close to a full window of packets resides in the link buffer. We also assume that congestion at the link persists and as a consequence the average queue length always exceeds min_{th} . This implies that CHOKe is always active at the link. For simplicity we assume that the computed probability using RED is negligible when compared to the CHOKe induced probability. In [93], it is shown that the overall probability that packets of flow i are dropped before they get through, either by CHOKe or congestion based dropping, is equal to:

$$p_i = 2h_i + r - 2rh_i, (5.3)$$

where h_i is the probability of an incoming packet being dropped by CHOKe for flow *i* and *r* is the congestion-based (RED) dropping probability. h_i is equal to b_i/b , where b_i is flow *i*'s buffer length and *b* is the total buffer length. With the assumptions made above, the packet dropping probability equals $2h_i = 2w_i/b$, where w_i is the window size of flow *i*. This is the probability that an arriving packet is matched with a randomly drawn packet from the buffer, and the resulting loss of both packets. The effective probability of congestion window reduction is w_i/b , since multiple packet losses within a single window will only halve the window once. This probability in turn determines the equilibrium window size, hence we have:

$$w_i = \sqrt{\frac{3b}{2w_i}} = (3b/2)^{1/3}.$$
(5.4)

This approximation is very conservative, since we have neglected any causes of packet drops other than CHOKe, such as buffer overflow and RED. Moreover, in calculating the window size we used the equation that models the congestion avoidance phase ignoring the slow start. The above expression (5.4) for window size implies that with CHOKe large buffers need to be maintained to avoid the window size getting too small, and keep it away from timeouts. Since CHOKe drops two packets in a row, the minimum window size to avoid a timeout becomes five, if a TCP Reno like implementation is used. However, maintaining large buffers increases queuing delay. Moreover, the queuing delay increases linearly with the buffer size, but as equation (5.4) implies, the growth of the window is slower than linear. This has an overall effect of reducing the rate of TCP flows. Beside this weakness, as simulation results in Section 5.4 show, CHOKe's performance degrades as the number of misbehaving flows increases, even though the aggregate load remains unchanged.

A different approach is adopted in RED-PD [60]. Rather than using the buffer occupancy, it relies on the packet drop history to detect non-responsive flows and regulate their rates. High-bandwidth flows are identified using the RED packet drop history and flows above a configured target bandwidth are monitored. RED-PD controls the throughput of the monitored flows by probabilistically dropping packets belonging to them at a prefilter placed before the output queue. As we show below, the RED packet drop history cannot itself give an unbiased estimate of the flow rate. As in equation (5.1) the rate of a TCP node depends on the packet size. To mitigate this effect, many AQMs, including RED, adopt the byte mode of operation when the packet sizes differ among flows. In this mode of operation, a packet's dropping probability gets scaled by the ratio of l_s/l^{mean} , where l^{mean} is the average packet size. Hence the rate becomes:

$$x = \frac{l_s}{d_s} \sqrt{\frac{3l^{mean}}{2pl_s}}.$$
(5.5)

Due to the rate's non-linear dependence on the congestion measure, effects of packet size do not diminish even in this mode of operation. As a consequence, the flow rate cannot be estimated by packet drop history alone. In addition to different flows with varying packet sizes, it is also common to have different packet sizes within a single flow. Apart from this, as [66], [46] show, RED queues are known to oscillate wildly in many instances. A wildly oscillating queue often produces bursty packet drops, making packet drop history an unreliable reference.

CSFQ tries to achieve a fair bandwidth allocation within a network of interconnected edge and core routers. CSFQ is based on the interdependence between edge routers and core routers. At ingress, edge routers mark packets with an estimate of their current sending rate. A core router estimates a flow's fair share and preferentially drops a packet from a flow based on the fair share and the rate estimate carried by the packet. This interdependence is a major limitation of CSFQ, because it is a deviation from the Internet architecture where each node makes independent decisions on how to react to congestion. If an edge router either maliciously or by mistake underestimates some of the rates, then core routers will drop less packets from these flows based on the probabilistic drop decision. CSFQ also requires an extra field in the packet headers.

We present a mechanism called Protective Queue Management (PQM) that falls between simple queue management techniques and complex scheduling algorithms, much like CHOKe or RED-PD, but one that avoids the inherent limitations of these techniques.
5.3 Protective Queue Management

We build the mechanisms on top of REM, which achieves high link utilization while maintaining low queues. We keep limited flow states thus avoiding an increase in computational complexity. The packet arrival rates of likely misbehaving flows are measured, using the packet's arrival time and size as done in [91]. It gives an accurate estimate of the flow's rate irrespective of the packet size, unlike in RED-PD. Given the congestion measure at the link, the upper bound of a TCP conformant flow's rate is computed. This together with the estimated rate of the flows traversing the link are used to detect non-responsive flows and penalize them. By using the flow's arrival rate, we don't rely on buffer occupancies and hence avoid problems associated with schemes such as CHOKe.

Using equation (5.1) that models the congestion avoidance phase of TCP, the rate of a TCP conformant end-node can be estimated using its RTT d_s , packet size l_s and the congestion measure p at the link. Assuming a lower bound on the round trip time (e.g. target queuing delay plus twice the link propagation delays) and an upper bound on the mean packet size, we can derive an upper bound on the sending rate of a TCP conformant end-node. It may be considered to be the fair rate of a flow traversing the link at its current level of congestion. This knowledge allows easy detection of non-responsive flows. All the flows that inject packets at a rate exceeding the fair share need penalizing. Otherwise the non-responsive flows are not enjoying an unfair share of the bandwidth at the current level of congestion and need not be penalized.

To estimate the arrival rate, we use the same exponential averaging formula as in CSFQ. Let t_i^k and l_i^k be the arrival time and length of the k^{th} packet of flow *i*. The estimated rate of flow *i* is calculated as:

$$r_i^{new} = (1 - \exp^{-T_i^k/K}) \frac{l_i^k}{T_i^k} + \exp^{-T_i^k/K} r_i^{old}$$
(5.6)

where $T_i^k = t_i^k - t_i^{k-1}$ and K is a constant. If the Exponentially Weighted Moving Average (EWMA) formula with constant weights is used instead, it artificially increases the esti-

mated rate when T_i^k becomes smaller than the average. This is a common occurrence due to bursty sources present in the Internet. In the above formula the term $(1 - \exp^{-T_i^k/K})$ counteracts such an effect. A small K increases the system response, while a large Kfilters noise and avoids system instability. However, K should be no larger than the average flow duration.

On each packet arrival, the rate of the flow that owns the packet is computed and compared against the fair rate. If the computed rate is more than the fair rate, the arriving packet is discarded. Two entirely different bandwidth allocation schemes among competing connections result, depending on whether the flow state is updated when a packet is discarded. If it is updated, all packets of a constant rate flow that exceeds the fair rate get discarded at the queue. We call this Protective Queue Management with a Penalty Box (PQM-PB). This implies that a flow needs to be responsive to congestion for it to receive a continuous non-zero share of the bandwidth. Since the level of congestion continuously changes, so does the fair rate. Unless an end-node sending at a rate close to fair rate, responds to congestion and reduces its rate, it may receive zero bandwidth because the new fair rate falls below its current rate. If the flow state is not updated when a packet is discarded, the flow's rate approaches the fair rate. This is similar to the behavior of traditional scheduling algorithms. The former approach looks attractive for many reasons. It encourages end-nodes to be responsive and, on the other hand, when a large fraction of a connection's data is lost and never gets retransmitted, as with multimedia applications, whatever is left may not constitute a comprehensible message.

Algorithm 5.3.1: Link Algorithm (r_i, T_i^k, l_i^k)

At the arrival of packet k belonging to flow i

if flow i is monitored

omment: compute flow arrival rate $T_{i}^{k} \leftarrow t_{i}^{k} - t_{i}^{k-1}$ $r_{i} \leftarrow (1 - \exp^{-T_{i}^{k}/K}) \frac{l_{i}^{k}}{T_{i}^{k}} + \exp^{-T_{i}^{k}/K} r_{i}$ **comment:** penalize misbehaving flows then $\begin{cases} \mathbf{if} \ (r_i(1-p) > r^{fair}) \\ \mathbf{then} \\ \mathbf{goto END} \end{cases}$ update flow state if Buffer is full $\mathbf{then} \begin{cases} drop packet \\ goto END \end{cases}$ $\mathbf{if} \; (uniform[0,1] < pl_k/l^{mean})$ $\mathbf{then} \begin{cases} drop \; packet \\ include \; i \; in \; \mathcal{U} \\ roto \; END \end{cases}$ enqueue packet :END

periodically

comment: Update dropping probability p

$$p_{l} \leftarrow p_{l} + \gamma(in + \alpha(b_{l} - b_{l}^{target}) - capacity)$$
$$p_{l} \leftarrow max(0, p_{l})$$
$$p \leftarrow 1 - \phi^{-p_{l}}$$
$$r^{fair} \leftarrow l^{mean} d\sqrt{\frac{3}{2p}}$$

Saved variables

 r_i : estimated arrival rate of flow i, t_i^k : arrival time of

packet k of flow i, r^{fair} : fair rate of a flow, b_l : buffer level at the link, p_l : link price,

p: current dropping probability, \mathcal{U} : list of monitored flows

Fixed variables

 γ : stepsize in price adjustment, α : weight of buffer in price adjustment

 $b_l^{\textit{target}}:$ target queue length, $l^{mean}:$ average packet size

Temporary variables

 $T_i^k:$ packet (k,k-1) interarrival time of flow $i,\,l_k:$ length of packet k,

in: aggregate input rate estimate

Clearly we only need to compute and compare the arrival rate of congestion nonresponsive flows. Moreover, computing the arrival rate of each and every flow, including TCP conformant short-lived flows, adds unnecessary computational overhead. A large number of flows that traverse the link can be short lived, with only few packets in them; hence excluding these flows from the monitoring process potentially leads to considerable computational savings. To achieve that, we keep a list of likely misbehaving flows whose rates need to be computed and compared against the fair rate. Several methods can be used to construct such a list, such as examination of a flow's packet drop history as done in [60]. We adopt a similar method, since it requires only a small processing power and can be run in the background. Periodically we run through the packet drop history over a few past round-trip times, and identify flows that have lost more packets than the congestion measure at the link would indicate, because a misbehaving flow gets a large share of the bandwidth, it would also lose more packets than a conformant TCP end-node. This also avoids flows from being monitored unnecessarily, if they become conformant after being detected and penalized previously. Since the identification process needs to be continuously run at the link, such a simple method is more suitable. However, the method adopted does not affect the performance of the algorithm but only its processing requirements. Pseudo code is presented in algorithm 5.3.1. PQM can also be used for protecting protocols other than TCP, by using the corresponding relation of transmission rate to packet drops for the specific protocol, in calculating the fair share.

Another application of this scheme can be rate estimation on a per-subnet or per ISP granularity and to apply fair allocations at that level. This also means using a different utility function [59] to that of a TCP conformant end-node, in calculating the fair rate.

As we mentioned previously, an effective identification process can reduce the state and processing requirements of PQM. Unlike schemes such as CSFQ, not every flow under all conditions need rate estimation, rather only the non-responsive flows present at a congested link. When PQM starts monitoring flows, packets belonging to these flows can be removed from the fast forwarding path of other flows and go for rate computation and comparison, thus having a minimal effect on conformant flows.

5.4 Simulation Studies

Extensive simulation studies are conducted using a single bottleneck link shared by congestion responsive TCP and congestion non-responsive constant rate UDP flows. Simulations are done using ns-2.26. The link has a bandwidth equal to 64 Mbps. Throughout the simulation run, 20 TCP flows with a round trip time equal to 30 ms share the link.

5.4.1 Experiment 1

In this simulation study we examine the effectiveness of each scheme in protecting TCP flows under an extreme load of non-responsive flows. During 20 to 60 seconds of simulation time, a UDP blast is present. It has a total accumulated rate of 96 Mbps, which is 1.5



Figure 5.1: PQM Performance: Extreme Traffic Load

times the link rate. There are four simulation runs with the UDP blast consisting of two 48 Mbps, four 24 Mbps, six 16 Mbps and eight 12 Mbps UDP flows, respectively. Both UDP and TCP flows have a packet size equal to 1000 bytes. Following the parameter settings of [71], we have for both RED and CHOKe, min_{th} equal to 100 packets, max_{th} equal to twice that and the queue size fixed at 300 packets. For PQM, we have REM parameter settings as used in the simulation studies presented in [5], $\gamma = 0.005$, $\alpha = 0.1$, and $\phi = 1.001$. As for the extra parameters required in PQM we use 30 ms as the upper limit of round-trip-time and 1000 bytes as the upper limit of packet size. Figure 5.1 presents simulation results. Among the four schemes considered, RED, CHOKe, PQM and PQM-PB, RED has the worst performance. This is expected as RED incorporates no techniques to protect TCP flows in the face of a UDP blast of this scale. Consistent with the expressions derived in equation (5.2) RED's performance is similar for all four different types of the UDP blast, since only the aggregate UDP flow rate affects it. However, the performance of CHOKe is not far different from that of RED: the TCP end-nodes receive only a small fraction of the bandwidth share consistent with the analysis presented in section 5.2. In contrast, TCP end-nodes receive a significant share of the bandwidth (0.3-0.5) when PQM is operating and an even bigger share (0.9) with PQM-PB.

5.4.2 Experiment 2

This simulation is identical to the first, except for the presence of a less intensive UDP blast. Here the aggregate rate is the same as the link rate. Again we do four runs of the simulation with the UDP blast consisting of two 32 Mbps, four 16 Mbps, six 10.66 Mpbs and eight 8 Mpbs UDP flows, respectively. The simulation results are very similar to the previous ones, except for a small increase in the TCP throughput share under all schemes due to the less intensive UDP blast.

5.4.3 Experiment 3

We consider the effectiveness of each scheme when connections have different packet sizes. We make the packet size of the TCP flows 400 bytes and of the UDP flows 800 bytes. Everything else is kept the same as in the first simulation. The simulation results show that RED and CHOKe favor flows with large packets whereas PQM is unbiased, as expected.



Figure 5.2: PQM Performance: Moderate Traffic Load



Figure 5.3: PQM Performance: Different Packet Sizes

Chapter 6

Conclusion

The central motivation of this thesis was to investigate and improve TCP performance in a DiffServ network. We developed a deterministic model of a DiffServ controlled TCP congestion window. Our model, derived from first principles, intrinsically captures Diffserv flow aggregation. It allowed us to account for an important network parameter, the number of flows per aggregate. Previous models, being extensions of TCP models of a best effort network, fail to account for this important network parameter. Using our model we derived more complete expressions of TCP steady state throughput. We showed that the number of flows per aggregate has a profound effect on aggregate TCP throughput. It can potentially override the effect of other network parameters such as contract rate and round trip delay. Another important byproduct of our model is the characterization of TCP transient behavior. We represented DiffServ controlled TCP dynamics in a classical control system model. It allowed use of standard techniques to analyze various mechanisms and propose improvements to algorithms as well as analysisbacked guidelines for choosing parameters of the algorithms.

Our results reconfirm the issues TCP encounters in a DiffServ network, i.e. TCP fails to realize contract rates under certain conditions. It cannot be expected that changing the TCP stacks running on hundreds of millions of end nodes would be a viable solution

CHAPTER 6. CONCLUSION

to these issues. DiffServ itself needs to incorporate mechanisms that mitigate these issues while being simple and scalable to be consistent with the DiffServ architecture. We proposed two DiffServ markers that help TCP realize contract rates in a DiffServ network. We proved their superior performance both analytically and experimentally. Traditional DiffServ markers are based on token buckets. Our analysis showed that the required token bucket depth increases exponentially with the contract rate. We proposed augmenting the token bucket with a packet queue that holds packets arriving at an empty token bucket. The required size of this packet queue was shown to have a linear dependence on the contract rate. Our second marker, CARM, is an enhanced version of ARM, a PI controller around the token bucket. It adapts the rate of token generation, in response to the measured aggregate TCP in-profile packet transmission rate. We presented an analytical design of the proposed PI controller, and validated the performance of our proposed algorithms through extensive ns-2 simulation studies.

QoS networks like DiffServ are becoming increasingly popular. However, most parts of the Internet still only provide a best effort service. Nodes rely on various QoS functions run locally. We looked at one such QoS function, i.e. the ability to survive against flows that are non-responsive to congestion. We highlighted deficiencies of existing mechanisms and proposed an alternative mechanism.

It is always exciting to look ahead. We now conclude by discussing some possible future directions of our research.

Our deterministic model of TCP can equally be applied for analysis of other congestion reactive transport layer protocols. One obvious application is studying the performance of new generation TCP protocols, e.g. scalable TCP, FAST TCP, in both DiffServ and best effort networks. The model can also be extended to a three drop precedence core. The model can be further enhanced by relaxing the assumptions we made.

TCP remains unaware of the different levels of service tags each packet receives, and is partly responsible for its poor performance in a DiffServ network. Our proposed packet queue at the token bucket holds packets arriving at an empty token bucket. This effectively increases the RTT of packets likely to be marked out-of-profile. This increase in RTT can potentially be used by TCP to infer packets being marked out-of-profile in its forwarding path. Subsequently this can be used to improve TCP's response to congestion.

Simulation studies done for an exact-provisioned network showed increased oscillations in packet transmission rates. This is due to the equilibrium packet drop probability being close to the discontinuity present in the packet drop probability curve of a multiple drop precedence core. Most networks are likely to be over-provisioned. Nevertheless this is an area of DiffServ that requires further investigation. Though studies [88] exist for tuning RED, the same cannot be said for multi-level RED curves used in DiffServ.

Our performance validation was confined to ns-2 simulation studies. A natural extension of this is to integrate our mechanisms into a real network testbed. This can be accomplished using a QoS control tool like Traffic Control (TC) [49] available with the Linux operating system.

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